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### MEMBERSHIP

# AMERICAN SOCIETY OF CIVIL ENGINEERS

Founded November 5, 1852

# PAPERS

# EFFECT OF SECONDARY STRESSES UPON ULTIMATE STRENGTH

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By John I. Parcel, M. Am. Soc. C. E., and Eldred B. Murer, Jun. Am. Soc. C. E.

#### SYNOPSIS

An analysis of the action of members of a bridge truss subjected to axial stress and secondary bending that arises from the deflection of the truss in its own plane, is given in this paper. The study is devoted primarily to the question of the effect of secondary stress in reducing the ultimate strength of such members, and, therefore, particular attention is given to the redistribution that occurs when the outer fiber stresses approach the yield point. As a supplementary study, a series of laboratory tests was made to determine the actual behavior of compression members with thin walls subjected to high secondary stresses and loaded to failure.

From the general analysis, and from these tests, it is concluded that for types of members and loading conditions investigated (which are believed to simulate closely the essential conditions for most bridge members), the ultimate strength is practically unaffected, even by high secondary stresses, if, in the case of compression members, the relative wall thickness is maintained at the ratio ordinarily required by the leading standard specifications.

#### INTRODUCTION

The problem of secondary stresses has occupied a prominent place in the theory of structures since the original investigations of the subject by Winkler, Asimont, Engesser, and Manderla in the late Seventies. A correct and complete analysis was presented by Manderla in 1879. Throughout the half

NOTE.—Discussion on this paper will be closed in February, 1935, Proceedings.

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<sup>&</sup>lt;sup>1</sup> "Die Berechnung der Sekündarspannung welche im einfachen Fachwerke infolge starrer Knotenverbindungen auftreten", Allgemeine Bauzeitung, 1880.

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century following, the problem has been the subject of many researches, both analytical and experimental, directed in the main toward clarifying and simplifying the analysis and to its experimental verification. To a considerable extent this effort has been successful. The theory of secondary stress analysis is now generally accepted by most authorities on the same footing as other phases of statically indeterminate stress analysis, and although the numerical calculations involved are tedious, various permissible simplifications have rendered the method quite workable for office design.

American engineers became generally interested in the secondary stress problem much later than European engineers, probably due in some degree to the predominance of the pin-connnected truss (for which, if all connections are true hinges, the secondary stresses are negligible) in American practice, and in part to a general distrust of the refinements of statically indeterminate stress analysis which at an earlier period was rather widespread. However, the last two decades (1914 to 1934) have witnessed a striking change in bridge engineering practice. The pin truss is no longer the dominant type; all spans from the smallest to the largest are being built as partly or fully riveted trusses, and the problem of secondary stresses has become a leading question in structural design. Most specifications now require such stresses to be computed for all sub-paneled trusses and for other cases in which there is reason to suspect that they may be large. That for many riveted bridge trusses of the massive type the secondary stresses are high is well established, theoretically and experimentally. In many cases the unit stresses due to secondary bending will reach 60 to 100% of the primary unit stresses, and in certain extreme cases they may exceed these limits.

The present method of providing for secondary stresses in design is subject to rather wide variations. Usually, a considerably increased unit stress (25 to 35% above the normal) is allowed for combined secondary and primary stresses and the member is proportioned by,

$$f = \frac{S}{A} + \frac{Mc}{I} \dots (1)$$

in which, f = unit stress; S = primary tension or compression; A = cross-section area; M = bending moment; c = distance from the neutral axis to the extreme fiber; and I = moment of inertia. More commonly, perhaps, a blanket allowance, applied alike to all members, is provided in the prescribed unit stresses.

In a number of monumental riveted bridges (notably the Quebec (cantilever), the Sciotoville (continuous truss), and the Hell Gate (arch) Bridges), elaborate and more or less expensive special devices in fabrication and erection were used to reduce the secondary stresses to a point at which little or no excess material was required.

While it is thus clear that the possible occurrence of high secondary stresses has been widely recognized and the best standards of practice have required that these shall either be provided for in the design or largely eliminated in fabrication and erection, it does not appear that any considerable attempt has been made to evaluate the effect of secondary stress upon the actual ultimate strength of a member.

It is clear that the action of combined primary and secondary stress is a different phenomenon from that arising from direct stress and flexure due to applied loads. This will be elaborated later in the paper; it may be noted here that (a) secondary stresses are not required to maintain the equilibrium of a bridge truss; and (b) that they are induced by the relative joint displacements of the structure, which, in turn, are conditioned by the distortion of the truss as a whole; and when these displacements have occurred, there is no further tendency for the stresses to increase. This clearly is quite a different condition from that which obtains in, say, an eccentrically loaded column in which the deflection and moment, at high stresses, increase much faster than the load. This peculiarity of secondary stress action has been noted.4 Indeed, the opinion has been advanced5 that even a high percentage of secondary stress, resulting in extreme fiber stresses beyond the proportional limit, will have little effect in reducing the ultimate strength of the truss, since the increased fiber deformations occurring in the neighborhood of the yield point tend largely to relieve the secondary stress. While this extreme view has not been generally accepted by the profession, the subject is believed to merit more attention than it has thus far received.

It is a practically universal principle in structural design that all fiber stresses shall be kept well within the yield point of the material. This, however, is subject to certain exceptions; for example, bearing stresses on rivets and pins are generally permitted to run 50% in excess of the stresses on the main sections. If this specification is sound and if the structure is designed consistently, it means that such local stresses may pass the yield point without endangering the safety of the structure. It is also common practice to permit unit stresses in the stiffening trusses of suspension bridges greatly in excess of the stresses in the towers or in the cable, if comparable material is used in the latter. The logic of this practice is that the stiffening truss is not a main carrying member and that if loaded beyond the yield point, the bridge may still be in no danger of actual failure.

It is scarcely to be presumed that stresses beyond the yield point in either of these cases would ever be regarded as other than undesirable, but since such a condition would not produce structural collapse, it is felt that a smaller margin of safety is permissible than would be the case for the main carrying members.

A somewhat similar argument might well be advanced in regard to secondary stresses if it can be shown that, under the normal range of conditions, such stresses do not actually reduce the ultimate carrying power

for example, "Theorie und Berechnungen der Eisernen Brücken", von F. Bleich, \*See, for example, "Theorie und Berechnungen der Eisernen Brücken", von F. Bleich, pp. 424-486; discussion by Edward Godfrey, M. Am. Soc. C. E., Transactions, Am. Soc. C. E., Vol. 89 (1926). p. 193; and Second Progress Report of Special Committee on Steel Column Research, Transactions, Am. Soc. C. E., Vol. 95 (1931), p. 1220 et seq. A clear statement of the limitations of secondary stresses will be found in "Modern Framed Structures", by Johnson, Bryan, and Turneaure, Pt. III, p. 14. No use is made of this, however, in the later discussion of the reduction in ultimate strength of columns due to secondary bending (see pp. 57-59).

<sup>&</sup>quot;Theorie und Berechnungen der Eisernen Brücken", von F. Bleich.

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of the members. It may still be regarded as undesirable to have any considerable portion of the section stressed beyond the yield point, but it may be permissible to tolerate much higher limits for such stresses if this in no way endangers the safety of the structure. The remainder of the paper is devoted to a consideration, in some detail, of the relation of secondary stress to ultimate strength.

#### ANALYSIS OF PROBLEM

General.—Secondary stresses, as considered in this paper, arise from the displacement of the joints in the plane of the truss when the latter is subjected to external loads. If the members are connected by perfectly smooth hinges (and are non-continuous at all joints) no secondary stresses can develop. If, however, the members are connected by riveting (or welding) to gussets so as to form a practically rigid joint, there will be, in general, some degree of restraint at the ends of each member, and corresponding bending moments will be developed. The secondary end moments in any truss member, m-n, may be expressed by the well-known slope-deflection equation:

$$M_{mn} = \frac{2 EI}{L} (2 \theta_m + \theta_n - 3 R) \dots (2)$$

in which,  $\theta$  represents the angular displacements of the joints referred to their original positions, and  $R = \left(\frac{\Delta}{L}\right)$ , the angular displacement of the line, m-n, each in radians. If  $\tau_m$  and  $\tau_n$  represent the angles between the end tangents and the line, m-n, at m and n, respectively, the equation for the secondary moment becomes,

$$M_{mn} = \frac{2 EI}{L} (2 \tau_m + \tau_n) \dots (3)$$

which is the form originally proposed by Manderla.

It may be well to call attention here to two basic characteristics of secondary stress action:

(a) Even when the secondary unit stress is a high percentage of the primary, the secondary moments offer no appreciable assistance in carrying the loads, and the members are always designed on the basis of full hinge action at the ends.

(b) The quantities,  $\theta$  and R, in Equation (2) are computed from the linear displacements,  $\Delta$ , of the truss joints, and for all cases of any practical importance they are directly dependent upon the axial distortions of the various truss members and, therefore, are linear functions of the loads.

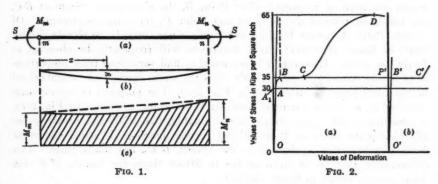
The influence of secondary bending upon the ultimate strength of members depends importantly upon the type of stress acting on the member concerned. The several classes are considered separately in the following discussion.

<sup>6&</sup>quot;Abhandlungen aus dem Gebiete der Technische Mechanik", von O. Mohr, 1906. p. 422 et seq; see, also, "Statically Indeterminate Stresses", by John I. Parcel and George A. Maney, Members, Am. Soc. C. E., Chapter VII.

7 See "Modern Framed Structures", by Johnson, Bryan, and Turneaure, Pt. II, pp. 427-428.

Tension Members.—In Fig. 1 is shown a tension member, m-n, acted upon at the ends by the moments,  $M_m$  and  $M_n$ . At any point, x, distant from the left end, the moment is (considering clockwise moments positive),

$$M_{(x)} = M_m - \frac{M_m + M_n}{L} x - Sy \dots (4)$$



For the particular case in which the end moments are equal, and oppositely directed,

$$M = M_m - Sy \dots (5)$$

It is clear that the maximum fiber stress occurs at the end of the member where the larger moment is applied, and (if this is the m-end) is equal to,

$$f = f_{\text{axial}} + f_{\text{bending}} = \frac{S}{A} + \frac{M_m c}{I} \dots (6)$$

Since the relation,  $f_b = \frac{Mc}{I}$ , is derived on the assumption of linear

stress variation, Equation (6) is not strictly correct beyond the proportional limit. When the yield point is reached and a large plastic flow takes place, the formula becomes quite inapplicable. The general tendency of the readjustment is toward an equalization of the tensile and compressive fiber stresses, respectively, such that a given maximum extreme fiber stress corresponds to a larger resisting moment.

Assume that Equation (3) is valid, then, as long as no stresses exceed the proportional limit, the behavior of the member is practically the same whether the end moments are due to eccentricity of axial loading  $(M_m = S e_m; M_n = S e_n)$ , or to secondary bending. When the region of plastic flow is reached, however, the behavior is fundamentally different. In the first case, while the extreme fiber stress is relieved by the stress-strain re-adjustment, a total resisting moment equal to S e must be developed regardless of the state of strain. In the latter case, since it is the tangential displacements that are invariably proportional to the loads (as long as  $\frac{S}{A}$  remains within the proportional limit), and since a given angular displace-

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ment corresponds to a smaller bending moment when the stresses in the outer fibers approach the yield point, it is clear that within this region the secondary moments increase more slowly than the loads. Some elaboration of this point may be desirable.

Fig. 2(a) is a typical stress deformation curve for mild steel. Point A marks the limit of proportionality; Point B, the yield point; Segment B-C, the region of marked plastic flow; and Point D, the ultimate strength. Of course, Point A cannot be fixed accurately since there is no clearly defined limit of linear elasticity; slight deviations will frequently be observed at fairly low stress. However, it is not usual to find variations from proportionality of any considerable magnitude until the stress reaches the neighborhood of the yield point, as indicated in Fig. 2(a). For purposes of approximate calculation, a conventionalized stress-strain diagram, as shown in Fig. 2(b), is sometimes used. This graph shows, roughly, that when the stress reaches the yield-point value at Point B', no further increase in stress can occur until a deformation equivalent to the length, B' C', has taken place. This deformation may be as much as ten to fifteen times the length, P' B', the value corresponding to linear elasticity.

It is evident from the foregoing relations that in the case of a beam in flexure, if plane sections are assumed to remain plane, the outer fiber cannot be stressed beyond the yield point until the fiber stress,  $f_b$ , over the greater part of the depth of the section has reached this stress limit. Referring to Fig. 3, a beam of symmetrical cross-section is assumed to be

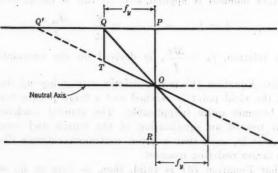


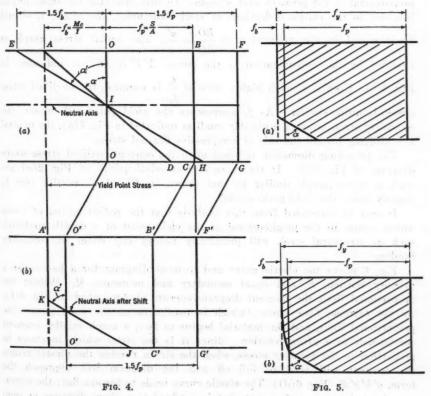
FIG. 3.

loaded so that the outer fiber stress, QP, is just up to the yield point value (Line O'P' in Fig. 2(b)). If the load is further increased, the stress curve takes the form of Area OPQT in Fig. 3. It is particularly to be noted that the contribution to the beam deflection of a vertical slice of thickness, dx, at Section POR, in the two cases will be in the proportion of PQ' to PQ, while the moments will have the proportion of PQTO to PQO. It is clear from this illustration that when the outer fibers reach the yield point, a wide range of beam deflection is possible without any appreciable increase in the

<sup>&</sup>quot;Excentrische beanspruchte Säulen", von A. Ostenfeld, Mitteilungen No. 3, Lab. für Baustatik, Technische Hochschule, Copenhagen, p. 20.

extreme fiber stress. Since the angular rotations at the ends of a member can increase no more rapidly than the axial loads, it will be impossible even with high secondary stresses for the extreme fiber stress to exceed the yield-point value without the distortion increasing far beyond any value reasonably to be expected in a truss in service. A simple example may be taken to illustrate the point.

It will be assumed that a truss member, m-n, of symmetrical cross-section, is subjected at the end, m, to an average axial tensile stress  $= f_p = \frac{S}{A}$ , and a secondary stress  $= f_b = \frac{M_m c}{I}$ , in which,  $M_m$  is the larger of the secondary end moments. Then, the maximum stress in the member will be at the end, m, on the side of the tensile flexural stress and will be given by Equation (6).



The stress graph is indicated by Curve ABCD in Fig. 4(a). Let it be assumed as a particular case that  $f_p = 20\,000$  lb per sq in.;  $f_b = 0.75\,f_p = 15\,000$  lb per sq in.; and that the yield-point stress,  $f_y$ , is 35 000 lb per sq in. The maximum fiber stress, AB, is then just at the limit beyond which plastic flow takes place.

A

Let it now be assumed that fp receives an increment of 50%, bringing it to 30 000 lb per sq in. If the linear relation of stress to strain was to hold,  $f_b$  would become 1.5  $\times$  15000 = 22500; the total maximum extreme fiber stress would be 52 500; and the stress graph would be the curve, EFGH, as shown in Fig. 4. On the other hand, assuming a yield-point stress of 35 000 lb per sq in., it is clear that this value cannot be exceeded until the extreme tensile fiber has suffered a stretch of approximately ten times that corresponding to 35 000 lb per sq in. It is obviously impossible, in a section of ordinary depth, for any such extreme deformation to take place unless the entire section is stressed to the yield point. Therefore, a redistribution of stress must be expected on the tensile side similar to that shown in Fig. 3. Again, it is noted that, as long as the average axial stresses are below the yield point, the tangential deflection angles (τ of Equation (3)) are strictly proportional to the primary unit stresses. In this case (for the small angles involved in the elastic deflections of steel structures), the angle, \u03c4, should be increased in the proportion of  $\frac{EO}{AO} = \frac{\alpha'}{\alpha}$ . The actual stress graph as

modified by the redistribution is the curve, A' F' G' JK, as indicated in Fig. 4(b). Even if a much higher ratio of  $\frac{f_b}{f_b}$  is assumed, the modified stress graph is quite similar. As  $f_p$  approaches the yield point still closer, the secondary stress becomes negligibly small as indicated in Fig. 5(a), the neutral axis shifting toward the side of compressive flexural stress.

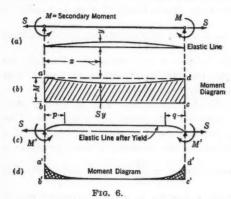
The preceding discussion is based upon the conventionalized stress-strain diagram of Fig. 2(b). If the more correct relationships of Fig. 2(a) are used, a stress graph similar to that shown in Fig. 5(b) results (for  $f_0$ slightly below the yield-point stress).

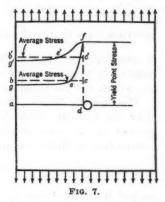
It may be concluded from this analysis that the redistribution of stress which occurs in the neighborhood of the yield point of a ductile material, such as structural steel, will practically nullify any effect of secondary bending.

Fig. 6 shows the elastic curve and moment diagram for a bar under a primary tension, S, and equal secondary end moments, M. Within the proportional limit the moment diagram appears as Area abcd in Fig. 6(b). As the extreme fiber stress (which is maximum at the end) passes the proportional limit, and the material begins to flow, a much smaller moment corresponds to a given rotation. Since it is the latter which increases in proportion to the primary stress, when the strain reaches the plastic range, the moment will tend to fall off and the diagram will approach the form, a'b'c'd' (Fig. 6(d)). The elastic curve tends to become flat; the curvature (and the region of over-strain) is confined to a short distance at each end (p and q, Fig. 6(c)).

There is precedent for ignoring over-stress of this type when strictly localized. Mention has been made of higher unit stresses allowed in bearing on rivets and pins (see "Introduction"). It may also be noted that most riveted end connections are productive of considerable local over-stress.

Reference may also be made to the fact that the presence of a hole in a plate, otherwise uniformly stressed, results in a heavy stress concentration at the edge of the hole. If the diameter of the hole is so small that the width of the plate may be assumed infinite in comparison, analysis shows that the stress at the edge of the hole is three times the average. For normal ratios of diameter to widths, tests have shown stresses 2.3 times the average. However, the re-adjustment that occurs when the highly stressed region reaches the yield point, practically nullifies any effect on the ultimate





strength. The two stress graphs are shown in Fig. 7. Below the elastic limit relatively high local stress concentrations must occur in all plates composing riveted members; but, for reasons just stated, these are properly ignored in all normal cases.

If the ultimate strength of a tension bar is understood to be its extreme effective strength as a bridge member, this value is limited to an average

stress,  $\frac{S}{A}$ , equal to the yield point of the material. The preceding discussion

tends to show that this effective strength is unchanged by any degree of secondary bending that may be expected in a well-designed structure.

Compression Members.—It is well known that flexure combined with compression produces a different behavior in a member from that which occurs under flexure and tension. The axial stress in the latter case tends to decrease the bending where in the former case it increases it; the moment represented by the axial stress times the deflection adds to the normal flexural moment, and in moderately flexible members at high stresses the total moment builds up rapidly. When the more highly stressed fibers pass the proportional limit, and the deflection begins to increase faster than the stress, the member proceeds rapidly to failure.

Most of the compressive chords (and frequently other compression members) in a bridge truss are of a stocky type which, even when subjected to

Observation of the theory (originally due to Kirsch): see, also, "Applied Elasticity" by Timoshenko and Lessells, p. 9; and "Theorie und Berechnungen der Eisernen Brücken", von F. Bleich, pp. 249-252.

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bending stresses of from 50 to 100% of the axial stresses, shows relatively slight deflections from a straight line. The ultimate strength of such members is reached when the average stress over the section reaches, or approaches, the yield point of the material.

In considering the strength of compression members under primary and secondary stresses, the secondary end moments may be either of the same or of opposite signs. When the moments are of the same sign and of nearly the same magnitude, the member is bent into an S-shaped curve, the moment near the center is zero, and the deflections are so small that in any ordinary

case buckling action for the member as a whole (giving rise to an  $\frac{L}{r}$  failure)

is practically negligible. When the moments are oppositely directed, the member is bent in single curvature, the maximum deflection occurs near the center, and the buckling tendency may be considerable.

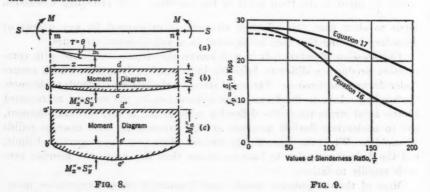
Compression Member Bent in Single Curvature.—For simplicity consider the case in which the end moments are equal in magnitude. One analysis of the effect of secondary bending on the ultimate strength of a column bent in single curvature proceeds on the assumption that the action is

analogous to the case of a virtual eccentricity  $=\frac{M}{S}$  at each end. By this

method it is found that a considerable reduction in column strength results from the secondary bending. For example, 40% secondary stress reduces the strength of a short column about 28%, assuming the limit to be determined

by the maximum fiber stress,  $\frac{S}{A} + \frac{Mc}{I}$ . A column with a slenderness ratio,

 $\frac{L}{r}=75$ , however, is reduced 35%, due to the added buckling tendency from the end moments.



This theory is open to serious criticism as applied to members that develop any considerable curvature of the central line before failure, because, in such

<sup>&</sup>lt;sup>16</sup> See "Modern Framed Structures", by Johnson, Bryan, and Turneaure, Pt. II., pp. 57-59.

cases, the effect of the moment, Sy, is such as to cause the angle,  $\tau$ , to increase more rapidly than the loading. This effect is ignored in the common (as distinguished from the exact) theory of secondary stresses.

Moment diagrams for two successive loading stages are shown in Figs. 8(b) and 8(c). It is clear that: (1)  $\frac{\tau}{\tau} = \frac{\text{Area } abcd}{\text{Area } a'b'c'd'}$ ; and (2), that these ratios, due to the effect of the moment, Sy, cannot be in the proportion of  $\frac{M'n}{M''n}$ . A more thorough analysis presented elsewhere shows that if  $q = \sqrt{\frac{S}{EI}}$ ,  $\phi = \frac{qL}{2}$ , and  $\alpha = \text{percentage of secondary stress}$ ,

$$f_b = \alpha f_p \frac{\phi}{\sin \phi} \dots (7)$$

This remarkably simple form admits of a ready comparison with the case in which  $M=S\ e$ ; thus:

$$f_b = \frac{e c}{r^2} f_p \sec \phi \dots (8)$$

from which is derived the ordinary "secant" formula for columns:

$$f_p = \frac{f}{1 + \frac{e c}{r^2} \sec \phi} \dots (9)$$

Similarly, by means of Equation (7):

It will be found that, since  $\frac{\phi}{\sin \phi}$  increases much more slowly than sec  $\phi$ , the effect of secondary bending on the buckling of a column is relatively much less than for end moments that increase in direct proportion to the load (as would be the case for eccentric loading). Since  $\alpha = \frac{f_b}{f_p}$  in the first case, and  $\frac{e\,c}{r^2} = \frac{f_b}{f_p}$  in the latter case, if the same values are taken for these terms (say,  $\alpha = 25\%$  and  $f = 36\,000$ ) the curves for Equations (9) and (10) will be as shown in Fig. 9.

This analysis is not strictly correct in that, while it seeks to make the tangential angle, and not the end moment, proportional to the load, it assumes the correctness of Equation (3). The correct relation, however, is:<sup>18</sup>

$$M_{mn} = \frac{2 EI}{L} (2 a \tau_{mn} + b \tau_{nm}) \dots (11)$$

<sup>11</sup> Transactions, Am. Soc. C. E., Vol. 95 (1931), p. 1221 et seq.

<sup>12</sup> Loc. cit., p. 1223.

<sup>13 &</sup>quot;Modern Framed Structures", by Johnson, Bryan, and Turneaure, Pt. II, p. 512.

$$a=1+\frac{(q\,L)^2}{30}-\frac{11}{25\,000}\,(q\,L)^4+\ldots(12)$$

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A rigorous analysis of the problem is possible, but the resulting equations are exceedingly involved and are not readily applied. Their interest is largely academic, since a glance at the graph of the approximate equation in Fig. 9 will show that, for all values of  $\frac{L}{r}$  less than 70, the effect of secondary stress

on buckling action, measured in this case by the ratio,  $\frac{1+0.25}{1+\frac{0.25\ \phi}{\sin\phi}}$  , is slight,

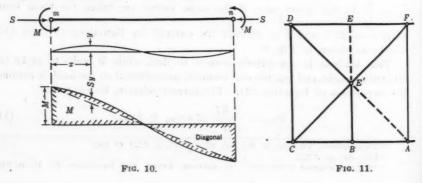
and for values less than 50, it is quite negligible. This holds true regardless of the value of  $\alpha$  (herein assumed as equal to 25 per cent). Two further facts are to be noted:

(1) Extremely high secondary stresses nearly always occur in members bent in an S-curve. The lower section of the end post in sub-paneled trusses, or trusses with a collision strut, is practically the only exception to this rule.

(2) From a consideration of the properties of bridge trusses and the manner in which secondary stresses arise, it is virtually impossible for a high secondary stress to be developed in a member bent in single curvature which, at the same time, is slender enough to develop any considerable buckling action. The exceptions to this rule are too few to be of importance in ordinary design. With a percentage of secondary stress of 35, or less, the dotted curve on Fig. 9 shows that, as far as buckling is concerned, columns with values of  $\frac{L}{r}$  ranging from 50 to 80, have practically the same strength as

similar pin-ended columns with  $\frac{ec}{r^2} = 0.25$ .

Compression Members Bent in Double Curvature.—When the secondary end moments are in the same direction, the bar will be bent into an S-curve for which the moment diagram is as shown in Fig. 10. (It is again assumed for simplicity that the moments are equal.)



The deflections in this case will be much smaller than for bending in single curvature, and the points of maximum deflection will fall outside the quarterpoints. Obviously, in such a case, the effect of secondary bending on the buckling action of the column as a whole is distinctly favorable since it forces the member to bend in double curvature, and the added bending moment due to axial stress is practically negligible. The high flexural stresses are near the ends of the member, and, in general, the effect of the secondary stresses on ultimate strength is the same as for tension members previously discussed; that is, a high extreme fiber stress occurs over a limited region, and in the neighborhood of the yield point the re-adjustment of stress due to plastic flow reduces the effect to negligible proportions before the average stress reaches the yield point.

Local Buckling in Thin-Walled Compression Members.—Most bridge trusses of the massive type for which the secondary stresses reach high per-

centages will have relatively stocky chord members  $\left(\frac{L}{r} \stackrel{=}{\leq} 40\right)$ . Built-up mem-

bers of such proportions show little or no transverse deflection until the average unit stress passes the proportional limit, and their ultimate strength is ordinarily from 80 to 100% of the yield-point stress of the material. It is generally considered that, for columns of this type, failure is imminent when any considerable part of the section is stressed to the yield point (although the average stress may be considerably less). More often than not the failure occurs through the local buckling of one of the comparatively wide, thin plates that make up the section.

Consider the top chord of a bridge of the conventional box type of section. Assume the material to have a yield point of approximately 35 000 lb per sq in. and the maximum permissible primary unit stress to be 17 000 lb per sq in. The secondary stress will be assumed as 100% of the primary. Under maximum working loads, then, the material on the most stressed side is loaded approximately to the yield point. If the bridge should be subjected to a 50% over-load, and the secondary moments are taken as proportional to the angular changes (that is, if Equation (3) were still to hold), the extreme fiber stress would be 51 000 lb per sq in., although the average would be only one-half this value. It has already been shown that beyond the proportional limit important re-adjustment of stress and strain takes place, resulting in a large percentage decrease in the actual secondary stress. None the less, if the member is assumed to be bent so as to throw the upper side into compression, the entire cover-plate and a portion of the top angles and web (amounting perhaps to 25% of the entire section) will be stressed to the neighborhood of the yield point. It would appear reasonable to suppose that the cover-plate, considered as an independent piece, would be on the verge of buckling as soon as the yield point is reached, and since the high secondary bending causes this state of stress to be reached much sooner than otherwise, it is pertinent to ask whether this may not hasten failure and thus reduce the ultimate strength of the member.

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The analysis of the buckling of plates due to loads in their own plane is now well developed. The theory was initiated by Professor G. H. Bryan<sup>14</sup> many years ago; it has been further developed and its applications (particularly to structural problems) greatly extended by Professor S. Timoshenko<sup>15</sup> in his classic memoir on elastic stability. Further important contributions to the subject have been made by Professor H. Reissner,<sup>16</sup> the late Hans H. Rode,<sup>17</sup> M. Am. Soc. C. E., and H. M. Westergaard,<sup>18</sup> M. Am. Soc. C. E.

The most comprehensive analysis of the buckling of plates as parts of bridge members that has yet appeared, so far as the writers know, has been presented by Professor F. Bleich.<sup>19</sup> Professor Bleich attempts to include in his analysis the effects of partial restraint at the edges of the plate and also to extend the results into the "plastic" range.

Some results of these analyses may be summarized briefly. If a plate of length, a, width, b, and thickness, t, is considered to be loaded in the direction of a, with a uniformly distributed compression,  $P = f_p t b$ , and restrained against linear (but not angular) displacement along the edges parallel to the loading, Bryan's formula for buckling in a single wave is,

$$f_p = \frac{\pi^2 E}{12 (1 - m^2)} \left(\frac{t}{b}\right)^2 \left[\frac{a}{b} + \frac{b}{a}\right]^2 \dots (13)$$

in which, m = Poisson's ratio (usually 0.25 to 0.3 for steel).

Bleich proposes using a variable factor,  $\tau$ , a function of the stress,  $f_p$ , to modify the value of E for stresses beyond the proportional limit. For conditions assumed in Equation (13), he derives,

$$f_p = \frac{\pi^2 E \sqrt{\tau}}{12 (1 - m^2)} \left(\frac{t}{b}\right)^2 \left[\frac{a}{b \sqrt[4]{\tau}} + \frac{b \sqrt[4]{\tau}}{a}\right]^2 \dots (14)$$

For  $\tau = 1$ , this reduces to Bryan's formula.

From Equation (13), for a fixed ratio of  $\frac{t}{b}$ ,  $f_p$  will vary with the quantity in the square bracket and will be a maximum for a = b, giving,

$$f_p = \frac{\pi^2 E}{3 (1 - m^2)} \left(\frac{t}{b}\right)^2 \dots (15)$$

Taking m = 0.3, Equation (15) gives 67 900 lb per sq in., and 43 400 lb per

sq in., respectively, for 
$$\frac{t}{b} = \frac{1}{40}$$
 and  $\frac{t}{b} = \frac{1}{50}$ 

If the edges are fully fixed, the foregoing buckling loads are practically doubled. Undoubtedly, the true condition is intermediate between these ex-

<sup>14</sup> Proceedings, London Math. Soc., 1891, p. 54.

<sup>&</sup>lt;sup>15</sup> "Sur la Stabilité des Systèmes Elastiques", Annales des Ponts et Chaussées, 1913.
Vol. 3, p. 496 et seq.

<sup>19 &</sup>quot;Uber die Knicksicherkeit ebener Bleche", Zentralblatt der Bauverwaltung, 1909, p. 93.

Beitrag zur Theorie der Knickerscheinungen", Der Eisenbau, 1916, p. 281 et seq.
 Buckling of Elastic Structures", Transactions, Am. Soc. C. E., Vol. LXXXV (1922), p. 576.

<sup>19 &</sup>quot;Theorie und Berechnungen der Eisernen Brücken", pp. 216-239, Berlin, Julius Springer, 1924.

tremes. These results tend to show that for normal proportions of a compression chord, buckling of the cover-plate will not take place within the elastic limit of the material. Beyond this point, of course, the formula does not apply.

In evaluating his expression for the buckling load in the more general case in which some of the material may be strained beyond the proportional limit, Bleich, after a lengthy analysis, obtains for  $f_p$  (in tons per square centimeter),

$$f_p = \frac{\phi}{2} - \sqrt{\frac{\phi^2}{4} - 9.61} \dots (16)$$

In which, 
$$\phi = \frac{\left(\frac{b}{t}\right)^4}{E \times 10^4} + 6.2.$$

For 
$$\frac{t}{b} = \frac{1}{40}$$
,  $f_p = 36\,600$  lb per sq in.; and, for  $\frac{t}{b} = \frac{1}{50}$ ,  $f_p = 32\,800$  lb per

sq in. Again, it should be noted that these values are for the case of no edge restraint.

Any attempt to take into account the variation in E beyond the proportional limit is attended with much difficulty; hence Equation (16) cannot be regarded as more than roughly approximate, and is scarcely applicable in the region of large plastic flow.

In applying the buckling formulas to the secondary stress problem, consideration must be given to the important difference between a plate with freely supported edges, loaded in its plane, and, say, a cover-plate of a chord member under combined primary and secondary stress. In the former case, when the stress reaches, or closely approaches, that corresponding to the point, B, on the stress-strain curve of Fig. 2, any further increase will result in distortions many times as great as those previously sustained. Such distortion has the effect of grossly exaggerating any slight imperfection in material or manufacture, and since no plate is perfectly straight or homogeneous, relatively large transverse deflections are developed which lead to immediate collapse.

In the case of a cover-plate subjected to combined primary and secondary stress causing the extreme fiber to reach the yield-point value, it is equally true that any material increase in the stress will probably result in a buckling failure. As has been shown, however, this increase cannot take place as long as the average stress on the section is well below the yield point, since it must be accompanied by a large plastic flow, and, due to the restraint of the adjacent material, such large flow cannot possibly occur in one part of the section until practically the entire area is stressed to the yield-point region. It appears reasonable to suppose that what actually happens is that when the yield-point stress is reached in the cover-plate, a practically constant state of stress is maintained under increasing load, while the deformation (which in this region of large plastic flow may vary widely with almost no change in the stress) varies only as is required to produce the necessary secondary displacements. As long as the average primary stresses are within the proportional limit, these

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secondary displacements will increase no faster than the applied loads. In other words, the free flow (accompanying a stress reaching the yield point) which would take place in an independent plate, is restrained to comparatively small limits by the action of the neighboring material in the case of axial stress and secondary bending, and this, it may be expected, will have a large effect in reducing the buckling tendency in the cover-plate.

When the average stress over the section passes the proportional limit, the cover-plate distortion begins to increase rapidly, and somewhere between this and the yield point of the column as a whole, local buckling of the cover may be anticipated.

One further point deserves some emphasis. When the common theory of secondary stresses is applied, it is assumed, of course, that the law of linear elasticity applies and that the effect of bending due to Sy is negligible. When, therefore, as discussed previously, an average primary stress of 26 000 lb per sq in., and a secondary stress equal to 100% of the primary, are computed for any member, what really happens is that the member is distorted at the end so that the tangential angle is such as would correspond to 26 000 lb per sq in. flexural extreme fiber stress, assuming E to be constant and the effect of axial stress on bending negligibly small. If the stress-strain diagram of Fig. 2(a), is examined, however, it will be noted after the limit of strict proportionality is passed (that is, when E becomes variable and a function of the load), that there is a considerable deviation from linearity before the region of free plastic flow is reached. The actual deformation at Point B (the beginning of marked plastic flow) will ordinarily be equivalent to that which would be produced by a stress of 40 000 to 50 000 lb per sq in., if the material followed the linear stress-strain law. In other words, the variation in E, before the actual yield point is reached, is sufficient to take care of a nominal extreme fiber stress due to combined primary and secondary effects considerably greater than the yield point of the material, and probably equal to any value to be found in well-designed trusses, even of the heaviest and most rigid type.

The possible effect of stresses beyond the elastic limit upon local buckling, especially of the cover-plates in the standard type chord sections, is the one point upon which the deductions from rational analysis are rather indecisive, and, if the preceding analysis is sound, the only manner in which there is any reason to suspect that the ultimate strength of a compression member may be affected appreciably by secondary stress. These facts seemed to justify an experimental study of the phenomena of failure in a built compression member of the box type subjected to a high percentage of secondary stress, with particular emphasis on the behavior of the cover-plate in the region of high local stress. In the following section, an account is presented of a limited group of laboratory tests undertaken to throw some light on this particular phase of the secondary stress problem.

#### EXPERIMENTAL STUDY

Model Simulation of Conditions.—The experimental study consisted of the testing of four columns of symmetrical section of standard types, giving in all

eight separate tests of columns under the action of secondary stress and direct axial, or primary, stress. Column No. 1 was made up in the shop of the Experimental Engineering Laboratory, University of Minnesota, Minneapolis, Minn., and the remaining sections were fabricated in the Minneapolis Plant of the American Bridge Company. All specimens were of relatively small cross-section as the testing machine available was not of sufficient capacity to handle a full-sized normal bridge chord.

Because of the difficulty of simulating the partial fixity of the ends of a member in a riveted truss, introducing as it would the problem of controlling and measuring the induced rotations, all specimens were tested with hinged ends. Such a member is closely analogous to the top chord member in a pin connected sub-paneled truss with the members continuous over the sub-panel points (see Fig. 11). A truss of this type, while nominally classed as pin-connected, may show high secondary stresses at such places as Point E. However, it should be emphasized again, the object of the experiments was to study the behavior of built compression members under high local stress due to combined primary and secondary action. As long as the essential features of such action are maintained, it is immaterial for the purposes of the test whether or not all details correspond to those which obtain in the case of an actual truss member under high secondary stress.

It is true, of course, that ordinarily the highest percentages of secondary stress occur in trusses with fully riveted chords. In Fig. 11, Joint E' will deflect about the same amount regardless of the end conditions of Member D-F. If the end joints are fully riveted, the added stiffness of the member due to the partial restraints at Points D and F will cause (for approximately constant center deflection) considerably higher secondary stress at Point E than would be the case for pin connections. As long as the fundamental characteristics of secondary stress behavior are preserved, however, high stresses, artificially produced, will have the same local effect on a member of given cross-section as if these same stresses were brought about by exact simulation of all the details of riveted truss action. This remark applies also to the method of loading which was followed in the test.

Again referring to Fig. 11, it will be noted that if Member EE' is removed, there will be no secondary stress at Point E, since this latter is caused by the displacement of Point E' relative to Line DF. This displacement tends to be transmitted to Point E, through Member EE' (the blank strut), developing a considerable tension in the latter. The action is identically that of a beam, DEF, with a transverse load at Point E, with this exception: The deflection of Point E' (and, therefore, of Point E) is strictly limited by the relative displacement arising from axial distortions, and which may be computed analytically or by means of a Williot diagram. Quite contrary to the case of a free transverse load at Point E, when the displacements have reached the prescribed value, Point E is rigidly held in position, no further deflection being possible. This is the unique characteristic of secondary stress action. Clearly, it can be simulated accurately in the case of a column by applying the axial loads, together with a certain controlled deflection. If, in

such case, one wishes to study the behavior of the member at a given stage of combined primary and secondary stress, it is immaterial whether (a) a given primary stress is applied, and then the desired deflection is induced; (b) the desired deflection is induced and then the direct stress is applied; or (c),

the two are developed simultaneously. The second method was followed in this investigation.

The columns tested were made to conform to the foregoing condition by being subjected to a constant bending deflection and consequent secondary stress as the axial stress was increased. This combination gave maximum effects due to combined secondary and primary stresses at the center line. with primary stresses only acting at the ends. In order to realize this condition the columns tested were placed inside a rectangular frame of rigid I-beam sides with thin flexible ends. The bending deflection of the column was then maintained at a constant value by the use of a toggle extending about the sides of the frame. The flexible end plates were sufficient to transfer the transverse thrust, but not stiff enough to cause appreciable moment on the end of the member or to interfere with the axial loading of the column by the testing machine. In this manner a combination of stresses was maintained in the coverplate of the column analogous to the combined primary and secondary stresses at the stay connection of Member DEF in Fig. 11. The actual amount of the secondary stress was thus dependent upon the transverse



SET-UP OF EXPERIMENTS ON SECONDARY STRESSES.

deflection given the specimen and was varied somewhat for different sections, depending upon their properties. Reference to the general photograph of the set-up (Fig. 12), and to the detail drawing of Column No. 2 (Fig. 13), will help to clarify the description of the specimen and testing frame.

Column Dimensions and Properties .- Column No. 1, Table 1, was similar to the standard top chord section of a bridge, consisting of plates and angles with a top cover and open bottom (see Fig. 14).20 Because of the limited

<sup>&</sup>lt;sup>20</sup> The proportions follow closely the top chord of the typical truss given in "Modern Framed Structures", by Johnson, Bryan, and Turneaure, Pt. III, Pl. III.

capacity of the testing machine and the difficulty of providing the necessary transverse bending force in the toggle, the model was made one-fifth the area

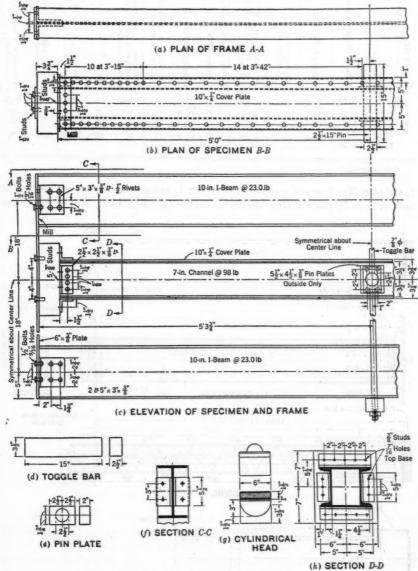


FIG. 13.—DETAILS AND DIMENSIONS OF COLUMN No. 2.

of the chord member referred to, as closely as commercial material would allow. (The diameter of the rivets was 0.17 in., the rivet holes being drilled. The rivet spacing in the angles is the same as in the cover-plate.) For Test

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TABLE 1.—CHARACTERISTICS OF TEST COLUMNS

Column No.	Test	Area, A, in square inches	Length, L, in inches	Moment of inertia, I, in inches *	Distance, c, from neutral axis to extreme fiber, in inches	Radius of gyration, r, in inches = $\sqrt{\frac{I}{A}}$	Slenderness ratio, $\frac{L}{r}$	Thickness, t, of cover- plates, in inches	Distance, b, between center lines of rivet rows, in inches	Ratio, $\frac{b}{t}$	Thickness, w, of web, in inches	Rivet spacing, p, in inches at center line	Diameter of rivets, D, in inches,
1 2 3 4	End Center Line	3.91 10.70 9.82 9.82 10.99	86.3 80.6 128.2 128.2 128.2	23.5 108.2 91.2 91.2	3.04 3.75 3.69 3.69	2.45 3.18 3.13 3.13	\begin{cases} 35.2 \\ 33.0 \\ 40.3 \\ 41.0 \\ 41.0 \\	1/6 1/4 1/6	. 51/8 8 9	41 32 48 48*	3/8 0.24 0.24 0.24	2 3 21/4 21/4	0.17 3/8 3/8 3/8

<sup>\*</sup> Reinforced.

2, Column No. 1 was the same as for Test 1, except that it was shorter. The only change in the riveting was in the cover (see Fig. 14(d)) for which a new

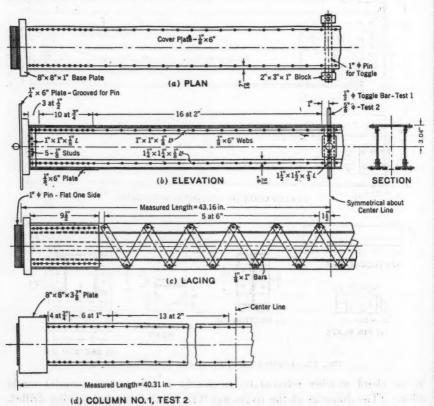


FIG. 14.—DETAILS AND DIMENSIONS, COLUMN NO. 1.

base plate was provided; otherwise, the details at the center line and ends were the same in both cases. Columns Nos. 2, 3, and 4 were of slightly different section, being made of two standard channels with two cover-plates (closed). Because of the symmetry of the section, two tests could be made from each specimen. They were fabricated in the standard manner using punched holes and  $\frac{3}{8}$ -in., hot-driven rivets, while Column No. 1 had small cold-

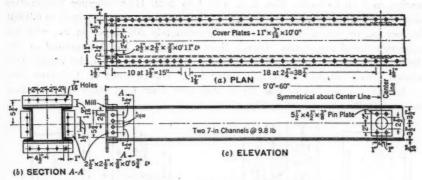


FIG. 15 .- DETAILS AND DIMENSIONS, COLUMN No. 3.

driven rivets in drilled holes. The ends of the members were milled to provide full bearing. The properties and detail drawings of the various column sections are shown in Figs. 13 to 16. Column No. 4 was the same as Column No. 3 (Fig. 15) except for the welded bars shown in Fig. 16.

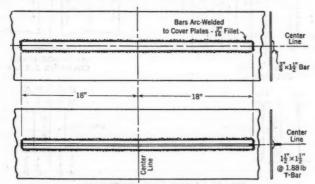


FIG. 16 .- BARS WELDED TO COVER-PLATES, COLUMN NO. 4.

Test Procedure.—The axis of the member was set as nearly vertical in the testing machine as could be done with a hair wire and weight. The pins were placed at the centroid of the section as closely as this could be measured and transferred to the base plate. Pins were flattened on one side to fix the point of rotation and to give a definite value of L in the plane considered. They were supported on cylindrical heads in the other plane to fit them to any angularity between the column ends and the testing machine. The detail drawing of Column No. 2 (Fig. 13) will make the test set-up clear.

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The initial loading used in all cases was 1 000 lb and the increments of axial loading were equivalent to 2 500 lb per sq in. on the section for the first test, and 5 000 lb per sq in. for the second test, on each specimen. Strain readings were taken at all increments of loading and, in many cases, loadings were repeated several times to establish the behavior of the member more definitely. Strains were obtained on Column No. 1 by the Whittemore straingauge, and on Columns Nos. 2, 3, and 4 by both Huggenberger tensometers and the Whittemore gauge. Consistent deformations were obtained to 0.00001 in. per in., or equivalent stresses of approximately 300 lb per sq in., with the aforementioned apparatus. Gauge lines on Column No. 1 consisted of five 10-in. lines on the compressive face, and six 10-in. lines on the tensile face placed symmetrically about the center line. Gauge lines on Columns Nos. 2, 3, and 4 consisted of one 10-in. line and four 1-in. lines on each face symmetrically placed. (See Fig. 17.)

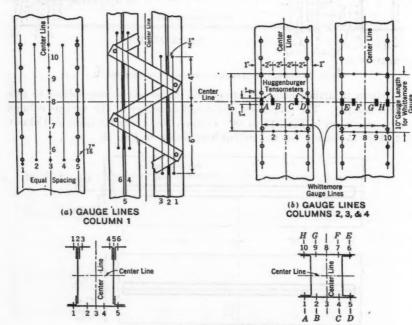


FIG. 17 .- GAUGE LINE DIMENSIONS.

As the deflection of the column was to be maintained at a constant value such that the nominal secondary stress remained constant throughout the range of primary loadings below the material yield point, it was necessary to measure the deflection value accurately. This was accomplished by means of an optical micrometer in the case of Column No. 1 and an electrical contact screw micrometer for Columns Nos. 2, 3, and 4, measuring the deflection between a hair wire and a point on the specimen center line in the web. It must be noted that the actual column deflection was not measured in any

case, as the hair wire was not fastened to the point of rotation of the column ends, but to some point on the deflecting structure. This had no effect on the problem because it was only necessary to have a relative value that could be measured and maintained. The deflection was not used directly for stress calculations, but was kept at a constant relative value in order to give a certain nominal secondary stress. In the case of Columns Nos. 2, 3 and 4, the wire was fastened to the one-tenth points on the specimen. This fastening the actual deflection values were read, while in the case of Column No. 1 the wire was fastened to the one-tenth-points on the specimen. This fastening necessitated a calculation of the elastic curve of the column so that an approximate value of the relative deflection between the one-tenth points and the center would be available. The elastic curve was calculated carefully, and it was noted that little change occurred in the deflection values for a large range of axial loadings. The equation for the elastic curve based on a constant center deflection and variable axial loading takes the following form:

$$y = \frac{\Delta}{\frac{\tan\left(\frac{qL}{2}\right)}{q} - \frac{L}{2}} \left[ \frac{1}{q} \frac{\sin\left(qx\right)}{\cos\left(\frac{qL}{2}\right)} - x \right] \cdot \dots (17)$$

in which,  $\Delta = \text{center deflection and } q = \sqrt{\frac{S}{EI}}$ .

It was decided to use a secondary stress of approximately 13 000 lb per sq in. for Column No. 1, Test 1, giving roughly 50% secondary stress at the material yield point. Since this test indicated that such a value was insufficient to cause local failure to develop before the normal ultimate strength of the columns was reached, in all later tests a value of 20 000 lb per sq in. was used in an attempt to produce a more marked local effect. Using approximately a secondary stress of 20 000 lb per sq in., the required deflection of the column was calculated and this value used as a basis for the approximate measurement in the tests. Table 2 gives calculated deflections and lateral loads corresponding to required secondary stress values. (The action of the column under lateral load was that of a simple beam prior to the application of axial loadings.)

TABLE 2.—CALCULATED LATERAL LOADS AND DEFLECTIONS FOR ASSUMED SECONDARY STRESS

Column No.	Lateral load,	Displacement,	Stress, f', in pounds
	P, in pounds	\( \Delta \), in inches	per square inch
1	4 750	0.0900	13 250
	19 200	0.2685	21 300
	16 200	0.2556	20 000
	16 200+	0.2556	20 000

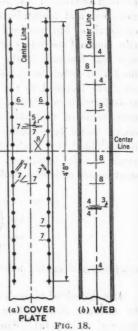
During the testing operations the deflection was checked and corrected if necessary at each increment of axial loading, and when the axial stress

reached a value sufficient to reduce appreciably the lateral force necessary to maintain the deflection, the stability of the columns was assured by stressing the toggle on the compressive face, thereby pre-

venting sudden  $\frac{L}{r}$  -failure in the direction of

the imposed deflection. This additional toggle was also used in adjusting the deflection after the bending resistance of the column had been reduced due to plastic flow and the original transverse force would have caused more than the required deflection.

Before testing, the specimen was painted with a dilute solution of plaster of Paris and water to make the strain lines visible. These are clearly shown in Fig. 19. The strain lines were recorded and sketched as they appeared during the test and a typical set is shown in Fig 18, with Table 3. Determination of the transverse force necessary to maintain the required deflection was accomplished by strain measurements on the toggle bars and subsequent calculation of the force transmitted. As an indication of the reduction in moment and consequent reduction in the transverse force, P, as the material in the column cover-plate approached the yield point,



and stress re-adjustment took place, the measured P-values are given in Table 4 for Columns Nos. 2 and 3.

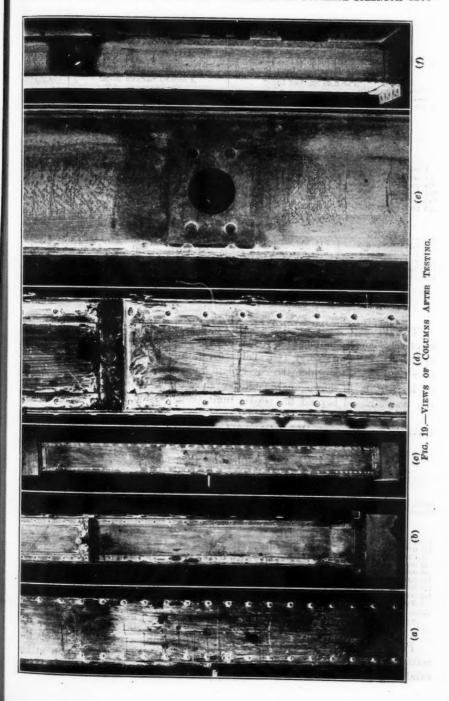
TABLE 3.—OBSERVATIONS OF STRAIN LINES, TESTS 3 AND 4

Test 3		Trer 4							
Strain Line No. (see Fig. 18):	Load, in pounds	Strain Line No. (see Fig. 18):	Load, in pounds						
1	161 500* 188 250* 301 000 339 000	56	157 000 215 000 268 500 322 000 354 000†						

<sup>\*</sup> Lines at Loads 1 and 2 for face not shown in Fig. 18.

† Innumerable lines appeared at this load.

For the purpose of this paper, it was not considered desirable to reproduce all the test data in detail. Tables 5 and 6 present the data from Column No. 1, Test 2, and Column No. 2, Test 3, showing deformations in millionths of an inch per inch for various axial loadings. These data are presented as typical examples of all eight tests, there being remarkably close agreement in all cases.



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TABLE 4.—OBSERVED VALUES OF LATERAL LOAD, P.

 $(E = 30.0 \times 10^6)$ 

Primary		Rods $(\frac{7}{8} - In)$ 0.60 Square			s ( $\frac{5}{8}$ - Inch 0.30 Square		Total
load, S, in pounds	Deforma- tion, in millionths of an inch per inch	Stress, f', in pounds per square inch	Load, P.	Deforma- tion, in millionths of an inch per inch	Stress, f', in pounds per square inch	Load, P, in pounds	load, P, in pounds
			(a) COLUMN N	Vo. 2, TEST 3			
1 000* 54 500* 108 000* 161 500* 188 250* 215 000*†	564 551 538 493 497 495	16 900 16 550 16 150 14 800 14 900 14 850	20 300 19 800 19 400 17 800 17 900 17 800	171 264	5 130 7 930	3 080 4 760	20 300 19 800 19 400 17 800 14 820 13 040
			(b) COLUMN N	No. 3, Test 5		*	-,3
1 000* 50 100* 123 800* 148 300* 197 400†	515	15 500 13 900	18 600 16 700	18.5 40 167	550 1 200 5 010	330 720 3 010	18 600 18 270 16 700 15 980 13 600

\* Column is in deflected position.
† Readings discontinued at this point.

The ultimate loads for Tests 2 and 3 were 167 800 lb and 381 800 lb, respectively, corresponding to a stress of 42 800 lb per sq in. and 35 700 lb per sq in. In Column No. 1 (see Table 5), failure occurred first in the web, near the base, after which the cover-plate buckled. A set of 80 millionths of an in. per in, is shown on the tension side, which indicates that even this side was stressed beyond the elastic limit (compression forces).

TABLE 5.—OBSERVED DEFORMATIONS, COLUMN No. 1 (Test 2), IN MILLIONTHS OF AN INCH PER INCH, FOR VARIOUS AXIAL LOADINGS

(+ = Lengthening (Tension))

Y 1 . C						RE	ADIN	G8	AT G	AUGE	L	NES	(SEE	F	ig. 1	7):			4	tac V	No.	AVERAGES	
Loads, S, in pounds	1	1	2	1	3	1	4	1	5	1 1	l	1	2	1	3	1	4	5	1	6	of	Cover-	Bottom
18			1	Con	ver-F	late					190		Bo	ttor	n An	gles	and V	/eb		1,00	1	plate	angles
1 000 to 140 000° 1 000† 40 000† 80 000† 100 000† 120 000† 140 000† 1 000.	-1 1 -6 -9 -1 2 -1 7 -2 6 -3 5	12 24 73 98 28 66 30	-1 1 -5 -9 -1 2 -1 7 -2 6 -3 5	13 - 81 44 73 - 58 - 17 - 79 -	-5 -9 -1 2 -1 8 -2 8	39 90 36 72 00 19 13	-5 -9 -1 2 -1 8 -2 7	34 76 - 14 - 84 -	-1 16 -58 -94 -1 28 -1 75 -2 66 -3 45	36 + 11 + 35 -	06 -67 -39 +8 -9 -32 -67	4 2 5 8 5	1 09 +83 +55 +23 +5 -17 -55	4 1 7 9 5 4	-1 08 +70 +42 +12 -7 -32 -67 -10	1 4 0 5 1 2	-1 112 +672 +393 +60 115 359 728 133	-1 1 +9 +6 +3 +1 -1 -5	47 47 60 13 41 06 05	-1 132 +700 +412 +74 101 344 718	2 2 2 2 1 2	-592 -945 -1 281 -1 764 -2 710 -3 588	+686 +406 +84 -97 -337 -690 -86

\* Column condition O. K. † Column is in deflected position.

Properties of the Column Material.—The modulus of elasticity of the material was determined from the load-strain relations of the column under axial loadings only, and checked in several cases by similar tests on coupons

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TABLE 6.—Observed Deformations, Column No. 2 (Test 3), in Millionths of an Inch per Inch, for Various Axial Loadings

(+ = Lengthening (Tension))

			READ	INGS	AT G	AUGE	LINES	(SEE ]	71G. 1	7 (b))	:		No.		Avei	RAGES	
Load, S, in pounds	3	Com	pressi	B on Co	-	C	TD.	8 To	E ension	F	G er-Plate	H	of sets	A and D	B and C	E and H	F and G
134 750* 161 500* 188 250* 215 000* 251 000*	7438299151 0031 1041 2411 4362 0882 5573 7965 631	-1 -1 -1 -1 -1 -1 -1 -2	076	1 74	7 -1 2 -1 5 -1 7 -1 2 -1 5 -1	100 175 275 200		. +665 3 +564 0 +458 8 +374 3 +269 5 +171 0 -109 -326	+52 +44 +35 +28 +20 + 9 + 1	7 +59 3 +50 9 +40 4 +30 0 +20 9 + 6 5 - 5	1 — 12 5 —233	0 +563 3 +468 5 +383 2 +297 3 +210 3 + 81 2 + 3 3 -195	4 8 2 2 2 2 2 2 2 2 2 2	-706 -868 -949 -1 042 -1 132 -1 233 -1 598 -3 040	-756 -920 -1 005 -1 111 -1 225 -1 271 -1 216 (Buckle)	+716 +545 +455 +371 +290 +205 +90 +90 -166 -429	+812 +622 +522 +427 +324 +224 +76 -31 -244 -583

<sup>\*</sup> Column in deflected position.

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cut from the column itself. Table 7 gives the moduli for each column as determined by the tests on the columns themselves. These values were used in determining stresses.

TABLE 7.—Moduli of Elasticity, E, in Pounds per Square Inch, as Determined by Tests

Column No.	Instruments used	Range of loading stress, in pounds per square inch	Average modulus of elasticity	No. of sets
1	Whittemore	20 000	30.7 × 10 <sup>6</sup>	14
2	Whittemore Huggenberger	20 000 20 000	$27.7 \times 10^{6} \\ 28.8 \times 10^{6}$	12 24
3	Whittemore Huggenberger	20 000 20 000	$28.8 \times 10^{6} \\ 28.6 \times 10^{6}$	10 32
4	Whittemore Huggenberger	10 000 10 000	$29.0  imes 10^{6} \ 29.0  imes 10^{6}$	6 6

As it was necessary to conduct a part of the test with some of the material stressed beyond the elastic limit, the characteristic stress-strain curves for the material were obtained in order that an estimate of the stress increase after passing the elastic limit could be made. A piece of material from the same rolling was used to determine the relations for Column No. 1 (see Fig. 20, Curve A). For Columns Nos. 2, 3, and 4, a coupon was cut from the cover-plate of Column No. 2 (see Fig. 20, Curves B and C). The modulus of elasticity is seen to check closely that determined from the columns. It is noted that the curve is nearly horizontal beyond the proportional limit even though the deformation was several times that of the yield-point stress. On this basis the stress carried by any material beyond the yield-point was assumed to be a constant and of intensity equal to the yield-point value.

An inspection of Fig. 20 shows that the increase in stress after the proportional limit is reached and before the curve becomes so flat as to make

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the stress nearly constant is approximately 3 500 lb per sq in. for Column No. 1 and from 2 500 to 3 000 lb per sq in. for the remaining columns. The proportional limit for the material of Column No. 1 was taken to be 39 000 lb per sq in., which gave a value of 42 500 lb per sq in. for maximum stress, a close

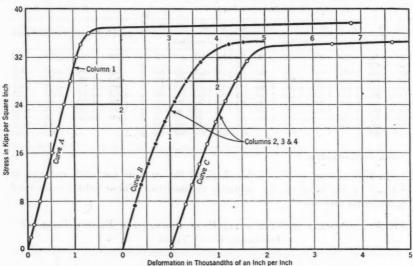


FIG. 20 .- STRESS-STRAIN CURVES FOR MATERIAL IN TEST COLUMNS.

check on the ultimate strength of the column. Similarly, the proportional limit of the materials of Columns Nos. 2 to 4, inclusive, was found to be 32 500 lb per sq in., with a maximum value of approximately 35 000 lb per sq in., which is also a good check on the ultimate strength of the columns.

In computing stresses in the cover-plates from the measured strains, it must be remembered that the deformations obtained by the Whittemore gauge are average values over a 10-in. gauge length. (The Huggenberger gauges have 1-in. gauge lengths.) When the column is deflected under transverse moments these deformations do not represent the maximum strains, inasmuch as the strains due to bending vary from a maximum at mid-length to zero at the end of the column. This results in an appreciable change in the resultant unit deformation within the gauge length of the instrument when long gauge lengths are used. An approximation to the difference between the maximum and the average reading may be estimated on the basis of the moment change. Since the moment is nearly proportional to the distance from the end of the column (concentrated load), the moment diagram approximates a triangle and the deformation decrease is proportional to the average decrease in length from the end. In this case (L=128.2 in. for Columns Nos. 2, 3.

and 4), the percentage of change equals 
$$\frac{\frac{5}{2} \times 100}{\frac{128.2}{2}} = 3.9$$

Since the deformation from bending was approximately one-half the total, the error involved in neglecting this factor was approximately 2 per cent. As this value is approximately the probable error in reading, loading, and sectional area, it has been neglected in the curves and stress calculations.

TABLE 8.—Stresses Determined from Strains in Table 5 (+ = Tension)

Load, S, in pounds	DEFORMATIONS, OF AN INCH	IN MILLIONTHS PER INCH		ips per Square ich
	Cover-plate	Bottom angles	Cover-plate	Bottom angles
1 000*. 40 000*. 80 000*. 100 000*. 120 000*. 140 000*. 167 800*. 1 000.	- 592 - 945 1 281 1 764 2 710 3 588	+686 +405 + 85 - 97 -337 -699	18.2 29.0 39.4 54.2 83.3	+21.0 +12.4 + 2.6 - 3.0 -10.3 -21.5 -40.0†

e S e d t e n e. ie le n \* Column in deflected position. † Estimated from a set of 80 millionths of an inch per inch at 1 000 lb. with specimen not deflected.

Tables 8 and 9 give the stresses for the two tests as determined from the strains given in Tables 5 and 6 and the moduli of elasticity given in Table 7. After the proportional limit has been passed these stresses are incorrect, and the values are only given to show the nominal stresses that would occur

TABLE 9.—Deformations and Stresses Determined from Strains in Table 6 (+ = Tension)

	WE	ITTEMO	RE GAT	GE		Hug	GENBER	ER GA	UGES;	Cover-P	LATE	
	Compre	ession	Ten	sion	(	Compre	ssion		1	Ten	sion	
Load, S, in pounds, with column in de- flected position	Strain, in millionths of an inch per inch, Gauge Line 3	Stress, f, in kips per square inch	Strain, in millionths of an inch per inch, Gauge Line 8	Stress, f, in kips per square inch	Strein, in millionths of an inch per inch, Gauge Lines $A$ and $D$	Stress, f. in kips per square inch	Strain, in millionths of an inch per inch, Gauge Lines B and C	Stress, f, in kips per squere inch	Strain, in millionths of an inch per inch, Gauge Lines E and H	Stress, f, in kips per square inch	Strain, in millionths of an inch per inch, Gauge Lines F and G	Stress, f, in kips per squere inch
1 000 54 500 81 250 108 000 134 750 161 500 188 250 215 000 251 000 301 000	743 — 915 —1 003 —1 104 —1 241 —1 436 —2 088 —2 557 —3 796 —5 631	-57.8 	+742 +564 +458 +374 +269 +171 + 11 -109 -326 -671	+20.55 +15.6 +12.7 +10.4 + 7.45 + 4.7 + 0.3 - 3.0 - 9.0 -18.6	- 868 - 949 -1 042		- 920 -1 005 -1 111 -1 225 -1 271	-26.5 -29.0 -32.0 -35.3 -36.6 -35.0 kle)	+545 +455 +371 +290 +205	+15.7 +13.1 +10.7 + 8.35 + 5.9 + 2.6 + 0.26 - 4.78		+23. +17. +15. +12. + 9. + 6. + 2. - 0. - 7. -20.

in the plate were Hooke's law still operative. The actual values after the elastic limit has been passed, have been discussed previously.

Re-Adjustment in Stress-Strain Relations. - By plotting the measured stresses on the compressive and tensile faces of the column with respect to

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a fixed line, a graph of stress distribution across the section was obtained. After the proportional limit is passed on the compressive side this graph is no longer a straight line, and, finally, the part of the curve beyond the material yield point becomes asymptotic to the line representing the ultimate unit strength of the column. The gauge lines used in determining the stresses plotted are given on the graphs shown, so that by reference to Fig. 17, the section referred to will be readily identified. Fig. 21 contains examples

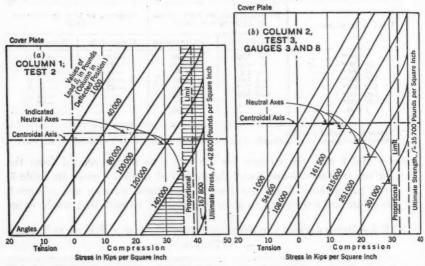


FIG. 21.—STRESS DISTRIBUTION (AVERAGE READINGS), COVER-PLATES AND BOTTOM ANGLES.

of these curves for the data of Tables 8 and 9. It should be emphasized again that the curves presented are nearly identical with those of the other tests.

In Fig. 21(a), the curve for the 140 000-lb load has been shaded for the purpose of illustrating the re-adjustment more clearly. This curve shows a stress on the tensile face of 22 000 lb per sq in. in compression, and if the straight portion were extended, would give a stress of approximately 57 000 lb per sq. in. on the compressive face. Since the yield point was determined as 39 000 lb per sq in., and the ultimate testing strength as 42 800 lb per sq in., it is evident that such a high nominal stress cannot occur and that a re-adjustment consequent upon plastic flow must take place as indicated by curvature of the graph. The direction of the straight portion was made parallel, in all cases, to the last curve on which the end points were within the elastic limit. The shaded area represents the bending stress over the section, while the heavy dashed line (which intersects the curve at the indicated neutral axis) shows the axial stress. Fig. 21(a) shows this section to be almost completely under the action of axial stress at failing load.

Cover-Plate Stiffeners.—The views of Column No. 3, in Figs. 19(e) and 19(f) show a buckle occurring at the point of critical stress. (This column

had a cover-plate relatively thinner than permitted by standard specifications.) The significance of this action will be discussed later. It will suffice here to note that it seemed worth while to investigate the feasibility of the application of a simple stiffening device to the plate. This was done in the case of Column No. 4 which (see Fig. 16) is a duplicate of Column No. 3, except for the plate stiffeners. No special attempt was made to develop the most practical device for commercial use; nor was any attempt made to follow a welding schedule and to reduce heating effects. The object in view was to test the effectiveness of the simplest type of stiffeners in supporting the wide, thin cover-plate when buckling was impending, so that it might suffer a certain amount of plastic deformation without "dishing" out of its original shape. Since little force is necessary to restrain such a plate from bending, small sections were welded to the cover-plate to give the necessary support against displacement normal to its plane, and thus, in effect, to cut down the free width. It was felt that if a simple device could be applied which would make the thin plate as resistant to buckling as a thicker one, this would be a desirable result regardless of the fact that in the specimens tested the plate buckling did not materially reduce the ultimate strength.

#### DISCUSSION OF RESULTS

For specimens of the dimensions and character used in this study, it would be reasonable to expect that a high degree of integrity of section would be maintained under an intensity of stress corresponding to ordinary working values. On Column No. 1, however, a noticeable slip was observed between the web and the flange. The deformation difference amounted to approximately 30% of the bending strain. For the plate and channel sections used in Columns Nos. 2, 3, and 4, no direct measurement of the slip was made as in Column No. 1. However, since the stress-deflection values checked rather closely, it was concluded that no appreciable slip had occurred.

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Fig. 19 shows strain lines occurring on both flanges of the specimen and across the web joining the two flanges. Since the nominal secondary stress due to bending was approximately 20 000 lb per sq in., such strain lines could not have occurred on the tensile side, under elastic conditions, until the average axial loading had reached 52 000 lb per sq in. (the yield point being approximately 32 000 lb per sq in.). As the ultimate axial load was approximately 35 000 lb per sq in., it is evident that the secondary bending was relieved by the plastic condition on the compressive face, which permitted a given angular change to take place with a much lower extreme fiber stress. This angular change, in turn, reduced the tensile flexural stress, with the result that the stresses due to the axial load of 35 000 lb per sq in. were sufficient to cause appreciable yield. That a complete re-adjustment resulting in a nearly uniform distribution over the section was the final state of stress, is evident from an examination of the strain lines on the tensile coverplate, which, while nominally holding a stress of 15 000 lb per sq in., passed the elastic limit despite the fact that the ultimate average axial stress was only a little greater than the value of the elastic limit as measured.

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The stress distribution curves (of which Fig. 21 is characteristic) bear out further the action indicated by Fig. 19. They show a redistribution of stress within the plastic range in complete agreement with the theoretical analysis presented previously. As the loading is increased, the neutral axis is progressively lowered until it lies near the edge of the section; the bending stresses become negligible and the distribution is nearly uniform over the entire section.

Referring to Fig. 2 and recalling that the plastic deformation in the neighborhood of the yield point is approximately fifteen times the elastic deformation at the proportional limit, it is obvious that it would require far greater secondary bending than the value developed in the test to cause the extreme fiber stress to exceed the yield point; that is, to reach Point C, Fig. 2. Assuming elastic behavior, the test loading gave a nominal maximum extreme fiber stress of 55 000 lb per sq in. The corresponding deformation, however, was less than twice the value occurring at the proportional limit; for the stress to reach the value, C, would require six to eight times this deformation.

Another point to be emphasized is the fact that if the stress is assumed to remain at an approximately constant value in the compressive face while the yield is traversing the flat part of the curve of Fig. 2(b), even though the material flows freely without appreciable increase in stress, it can deform only to a limited extent because of the action of the remainder of the section; and, until such time as the entire section is approaching the yield point, it will deform only enough to get relief from additional stress, while continuing to hold its yield-point value. This condition is radically different from that of a specimen subjected to a stress that cannot be relieved in intensity by a slight yield.

In examining the distribution curves it is of interest to note that when yield on the compressive face is shown by a curvature of the graph, the increment of stress received by the tensile plate for uniform increments of loading is constantly increasing. A measurement of this change gives an idea of the "relief" of the bending stresses as plastic flow permits the column to assume the deflected position that originally caused the secondary stresses. A further estimate of this relief is obtained from Table 4, which gives the measured transverse force, P, necessary to cause the original deflection and its value during the test as plastic flow was reached. The reduction shown is quite marked. The amount of bending stress remaining (as shown by the stress diagrams of Fig. 21) may be checked by comparison between the permanent set in the column after test and the deflection used for secondary stress, the difference in deflection being used in an approximate calculation of the bending stresses necessary to cause this small deflection. The values of the permanent set are given in Table 10.

An examination of the data presented in Tables 8 and 9, and in the plotted graphs, shows a deformation along the center line of the column somewhat greater than that at the rivet lines. Since the bending stresses are transmitted to the plate at the rivet lines, such a distribution would appear.

at first glance, to be contrary to what should be expected. As a possible partial explanation, it was noted that on all specimens a marked transverse curvature of the cover-plate (concave outward) developed under bending action alone, somewhat analogous to that commonly observed in wide flanged I-sections. This dishing inward was largely confined to the region of high flexural stress, and apparently resulted in an appreciable accentuation, locally, of the longitudinal curvature of the plate, which would be reflected in a somewhat higher deformation in the outside fibers along the center line of the column, where the gauge readings were taken.

TABLE 10.—PERMANENT SETS AND MAXIMUM LOADS

Column No.	Test	Deflection pro- duced, in inches	Maximum load, S, in pounds (column in deflected position)	Permanent set in inches
1	1 2	0.0900	140 000 167 800	0.0796 0.2033
2	3 4	0.2685 0.2685	339 000 381 800	0.2055
3	5 6	0.2556 0.2556	271 000 344 000	0.1530 0.2360
4	7 8	0.2556 0.2556	295 500 305 000	0.1945 0.2314

It is worthy of note that this dishing action has one distinctly favorable effect on the ultimate buckling strength of the cover in that, by directing the buckling inwardly, it reduces the unsupported width of the plate from the distance between the rivet lines to a value considerably less—probably almost the clear distance between the backs of angles or channels. It will also be observed that the bending of the column as a whole has a tendency to direct the buckling of the cover-plate inward. These facts are of considerable significance for cases in which local buckling is likely to be the criterion of ultimate strength.

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In the general analysis the results of buckling formulas for ratios of thickness to unsupported width of one-fortieth and one-fiftieth were presented.

Reference to Table 1 shows the  $\frac{b}{t}$ -ratios of the specimens tested to have

varied from 32 to 48. The aforementioned results are quite applicable to these cases and clearly indicate that buckling is improbable in such coverplates at stresses under the yield-point limit. The preceding discussion shows that stresses in execess of this limit are not realized under the most extreme conditions herein considered. In connection with this point it must be noted that the general buckling formulas become invalid as soon as the stresses pass the limit of proportionality, and furnish only roughly approximate values. For such cases the yield-point stress is usually considered the buckling stress. It is with regard to the latter point that the tests are significant. It might be reasoned that the wide thin cover is in an unstable condition when the stress reaches the yield point (Point B', Fig. 2(b)), and that local buckling of this cover should cause collapse of the entire section at a value

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slightly greater than the yield-point stress of the cover. However, in all cases except that of Column No. 3, despite the fact that a deformation twice that corresponding to the yield-point (Point B', Fig. 2(b)) stress was realized, there was no sign of buckling until the average stress over the entire section reached the yield point, and unlimited distortion became possible.

In Column No. 3 where the  $\frac{t}{b}$ -ratio was  $\frac{1}{48}$  (well below the limit permitted

by most specifications), incipient buckling action was noticeable shortly after the extreme fiber had passed the proportional limit. However, the development of the buckle was so slow that the column as a whole maintained its integrity until, as in cases of other specimens, the average stress over the entire section attained a value slightly above the yield point.

It is believed that the reason for this action lies in the previously discussed fact that the distortion corresponding to entirely free plastic flow cannot take place in the cover, until the average stress is of sufficient intensity to cause the entire section to behave plastically. It is reasoned, therefore, that as soon as the cover reaches the yield point, and plastic flow takes place, the member assumes the deflected form with a greatly decreased resistance, the secondary stresses largely disappear, and the stress approaches uniform distribution across the section. Simultaneously, the distortion and direction of impending buckle of the cover-plate are controlled so as to permit the necessary deformations without actual buckling, thereby giving approximately the full yield-point stress as the ultimate load-carrying capacity of the section.

It has been noted that indications of buckling of the thin cover-plate in Column No. 3 were observed at an earlier stage of loading than for Columns Nos. 1 and 2, and that for an identical section in Column No. 4 simple stiffening devices were provided. The effectiveness of these stiffeners in holding the thin cover-plate in line in the region of high stress is clearly A comparison of Test 5, Column No. 3, with Test 7, Column No. 4 (the columns being identical except for the cover-plate stiffeners on the latter) shows that at the average unit stress causing a marked incipient buckling in Column No. 3, Column No. 4 showed no sign of such effects. While Test 8 (Column No. 4) showed a lower final value than Test 6 (Column No. 3), this was due to the fact that the former was not loaded to the point of complete collapse. At a load of 305 000 lb axial stress, however, the cover-plate was in better condition than that of Column No. 3 at the same load.

The results of the test indicated some serious defects in the particular stiffening device used. The sudden change in section at the end of the stiffener created a marked local field of stress concentration, the occurrence of which was indicated by the appearance of strain lines at a load well under the proportional limit of the column as a whole. It is clear that if such a stiffener is used, it should be extended farther toward the end of the column, or its section should be gradually tapered off to avoid such a marked change in cross-sectional area of the plate, since in the present case the unit stress in the plate adjoining the stiffener was practically equal to the maximum stress (stiffener and plate) at the center of the column. Further study and tests are required to determine the most effective form of stiffener, but the indications of this test are that a simple and inexpensive device of this type could readily be developed should it appear desirable to do so.

## SUMMARY AND CONCLUSIONS

From the general analysis presented, the following significant features of secondary stress action may be summarized:

1.—Secondary stresses are limited and controlled by certain deflection quantities (see Equation (3)). For any particular loading condition, these deflections are (for primary unit stresses within the elastic limit) approximately proportional to the axial distortions of the truss members, considered as pin-connected, and when, for a given loading, these deflections have been attained, there is no further tendency for the stresses to increase.

2.—As long as both axial and bending stresses remain within the elastic limit and the transverse deflection is small, the behavior of a member under primary stress and secondary bending is closely analogous to a similar member under eccentric axial loading.

3.—If the maximum extreme fiber stresses pass the proportional limit, or if the member is of such type that the transverse deflection is large, the preceding analogy ceases to hold, since, in the case of secondary action, it is the deflection and not the moments that are proportional to the load. In particular, when the extreme fiber stresses reach the neighborhood of the yield point, a radical re-adjustment takes place, greatly relieving the flexural stresses.

4.—As a result of the re-adjustment in stress-strain relations, it may be inferred:

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(a) That any tension member tends, as the load increases, to a condition of uniformity or stress over the cross-section, except for a local over-strain in a short section near each end.

(b) Compression members bent in single curvature may be seriously affected as regards  $\frac{L}{r}$ -failure if the transverse deflections due to secondary bending become large. This can only occur, however, in the case of large secondary moments and flexible members, a combination that is not ordinarily realizable. It was noted previously (see heading "Compression Member Bent in Single Curvature") that for values of  $\frac{L}{r} \equiv 70$ , the effect of secondary action in inducing  $\frac{L}{r}$ -failure is small—well under that corresponding to

a pin-ended column with normal "equivalent eccentricities" at the ends. In such a case the rigid joint action which gives rise to secondary stress acts as a brake on the long column deflection before the point of ultimate column strength is reached.

(c) For a column bent in double curvature, the secondary action, by forcing the curvature into two "waves", may actually have a beneficial effect as regards  $\frac{L}{r}$ -failure.

(d) For "stocky" columns (say,  $\frac{L}{r} = 40$ ), which are ordinarily the only

members that develop high secondary stresses, failure is nearly always due to local over-strain. Until the average stress approaches the yield point, the transverse deflection is negligible, and column action in the ordinary sense cannot occur. For such columns the secondary stresses, whether resulting in single or double curvature (almost invariably the latter will be the case for high secondary stresses) will merely result in high stresses on the compressive face, which are rapidly relieved by plastic flow of the material as the yield point is approached.

5.—It might be expected that a combination of primary and secondary stresses beyond the proportional limit would adversely affect the stability against local buckling of the wide, thin cover-plates commonly used in the compression chords of bridges. An analysis of the problem indicates, how-

ever, that local buckling is unlikely to occur, in plates having a  $\frac{t}{b}$ -ratio

consistent with the requirements of standard specifications, until the average stress over the column approaches the yield point of the material, which, in all compression members, marks the ultimate strength of the member.

The tests made primarily for the purpose of exhibiting the behavior of the box type of compression member with respect to local failure under primary stress and a high percentage of secondary stress, have been discussed rather fully in the previous pages. The test results may be summarized briefly, as follows:

6.—Re-distribution of stress beyond the proportional limit was found to take place in a manner closely agreeing with theoretical analysis.

7.—For combinations producing nominal values of extreme fiber stress as great as 55 000 lb per sq in. ( $f_p = 35\,000$  and  $f_s = 20\,000$  lb per sq in.), it was found: (a) That while strain lines began to appear in the coverplates as the proportional limit was passed, no indications of local buckling appeared until the average stress over the section approached the yield point

of the material, for plates with  $\frac{t}{b} = \frac{1}{32}$  and  $\frac{1}{42}$ ; but, (b) for plates with  $\frac{t}{b} = \frac{1}{48}$ , some evidence of incipient local wrinkling was noticed at a

b 48 load somewhat less than the ultimate capacity of the column, although this had apparently no appreciable effect on that value.

8.—When stiffeners were applied to the cover-plates of Column No. 4 (see heading, "Cover-Plate Stiffeners"), the indications of incipient buckling noted in Column No. 3 (Summary Item 7(b)) were entirely absent.

Although the general analysis of the behavior of bridge members under combined primary and secondary action resulting in local stresses beyond the proportional limit is believed to apply without restriction, it is obviously impossible to draw valid general conclusions from the test results on four specimens. A much more comprehensive program of experimentation would have to be undertaken before a final pronouncement could be made. Subject to these limitations, the following significant conclusions are indicated:

- (a) The ultimate practically utilizable strength of a tension member is not affected by any secondary stress action within reasonable practical limits.
- (b) Compression members sufficiently flexible to develop  $\frac{L}{r}$ -failure before the yield point is reached, will usually exhibit too low a value for the secondary bending to reduce the ultimate carrying capacity of the member materially.
- (c) The rigid type of built column, in which alone high secondary stresses are to be expected, almost invariably fails by local over-stress, usually at a point at which local buckling can readily take place. High secondary stresses have no effect in hastening such local failure, and, therefore, have no effect in reducing the actual ultimate strength of such compression members, providing the section proportions are governed by the limits of present standard specifications.

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The results of the investigation do not justify the conclusion that secondary stresses are of no importance. The fundamental principle which has so largely governed structural design (that no fiber stresses should exceed the yield point of the material), is too firmly established and is supported by too many sound reasons to be lightly ignored. Such a principle, however, cannot be applied blindly; it is of the utmost importance for the designer to know the consequence of overstressing any part of the structure. This may mean general failure, a limited, localized failure not endangering the structure as a whole, or merely undesirable local distortion and permanent set. The practical significance of this investigation lies in the fact that it indicates that overstressing due to secondary bending falls in the latter class. This is of vital importance in fixing the unit stresses and otherwise determining the margin of safety for cases in which high secondary stresses are involved.

The investigation does not cover certain important by-products of secondary bending as, for example, the effect on riveted and welded connections of alternating secondary moments. For certain types of joints, this effect may be quite important. Due to this and perhaps other effects, and the general desirability of avoiding large permanent set, it is highly desirable that the designer should know if and where high secondary stresses occur in a structure. Under certain conditions, he may deem it desirable to modify the design to reduce such stresses or to provide for them specially in the detail design. In any case, it is a matter of great practical designing significance to be assured that an unforeseen and unexpected overload,

producing a combination of primary and secondary stress nominally far above the yield point of the material, will not endanger the safety of the member as long as the average stress over the section is maintained safely below the yield limit.

### ACKNOWLEDGMENTS

All the experimental work was conducted in the Experimental Engineering Laboratory of the University of Minnesota, by aid of funds jointly furnished by the Graduate School, of which Guy Stanton Ford is Dean, and the Engineering Experiment Station, of which O. M. Leland, M. Am. Soc. C. E., is Director. Acknowledgment is also made of the co-operation of R. W. Robinson, Engineer of the Minneapolis Plant of the American Bridge Company, who furnished the test specimens at cost. The grateful thanks of the writers are also due to Professors C. A. Hughes and G. C. Priester for valuable criticisms and suggestions, freely given throughout the progress of the work; and to others who rendered valuable assistance during the conduct of the tests.

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## AMERICAN SOCIETY OF CIVIL ENGINEERS

Founded November 5, 1852

# PAPERS

# THE SPRINGWELLS FILTRATION PLANT, DETROIT, MICHIGAN

BY EUGENE A. HARDIN<sup>1</sup>, M. AM. Soc. C. E.

### SYNOPSIS

The design and construction of a filtration plant and filtered water reservoir at Springwells Station is described in this paper. These units form a part of the additional works constructed during 1929-1932 for the Board of Water Supply of the Metropolitan Area of Detroit, Mich. The filtration plant is of the rapid sand, gravity type, having an ultimate capacity of 300 000 000 gal daily. The reservoir is in two sections each of which has a capacity of 20 000 000 gal, with provision for a third section to be added later. The general basis of design, the data pertaining to the various parts of the plant, the hydraulics of plant flow, the construction program, and the tabulation of both construction costs and engineering costs are outlined herein.

The water supply for the City of Detroit is the largest to be completely filtered by rapid sand filtration, and includes the two largest rapid sand filtration plants in the world—the Water-Works Park Filtration Plant, having a maximum daily capacity of 360 000 000 gal, and the Springwells Filtration Plant, having a maximum daily capacity of 300 000 000 gal (capacities based on a filtration rate of 180 000 000 gal daily per acre).

## HISTORY OF WATER TREATMENT AT DETROIT, MICHIGAN

The City of Detroit has taken its water supply from the Detroit River for more than 100 years. Although privately owned and operated for the first eight years of their existence, the water system and supply works have been owned by the municipality since 1836. Since that time, from a small city of 6 900 inhabitants, the district served has increased in population to more than 2 000 000 and in area to more than 100 sq miles, extending about 10 miles along the river and about 10 miles inland from the river. Improvements for

NOTE.—Discussion on this paper will be closed in February, 1935, Proceedings.

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increasing the quantity of the supply, and its distribution, were the main considerations, except in the location of intakes, until, in 1912, when purification of the supply was first considered and permanent provision was made for chlorination. The quality of the water in the Detroit River at the intake built in 1905 (named 1905 Intake) has been comparatively good, but with increasing pollution and the growing consciousness of the consumers of the value and need of improvement in the quality of the water, the desire for a purer and more palatable supply increased until, in 1917, an experimental filtration plant with a capacity of 200 000 gal per day was constructed and ope ated for more than a year, establishing the feasibility of filtering and developing popular approval by dispensing filtered water to those who came for it. One year of operation (from October 1, 1917, to September 30, 1918) was used as the basis of a report by the late R. Winthrop Pratt, M. Am. Soc. C. E., dated March 1, 1919, outlining the general design of a filtration plant, to treat the entire then existing supply. In 1921, contracts were let for filtration works at Water-Works Park Station (see Fig. 1) and the filtration plant was completed and put in service on December 22, 1923.

While it improved the quality of the water greatly, the filtration plant at Water-Works Park did not add to the quantity. Due to the rapid increase in size of the city in both population and area, it was evident that a farsighted and comprehensive plan of additional supply for the Detroit Metropolitan Area was necessary immediately. Accordingly, a Commission of Consulting Engineers, composed of Messrs. George H. Fenkell, W. C. Hoad, Clarence W. Hubbell, Theodore A. Leisen, and the late Gardner S. Williams, Members, Am. Soc. C. E., was appointed, and reported jointly on January 5, This Commission recommended an extensive program, involving the construction of additional supply works, beginning immediately with (a) the building of a new intake in the river; (b) a raw-water tunnel from intakes to the west side of the city; (c) a complete new supply station at the site selected on the west side; (d) additional distribution mains; and (e) future construction of a third complete supply station at a site to be selected in the northeastern part of the city. Item (c) included recommendations for a lowlift pumping plant, a filtration plant, a filtered water reservoir, and a distribution pumping plant.

## GENERAL DESCRIPTION OF FLOW

The new system provides for the distribution of additional water to the Metropolitan Area of Detroit from three separate stations, each having a filtration plant and the necessary pumping plants (see Fig. 1): (1) The old Water-Works Park Station on East Jefferson Avenue; (2) the Springwells Station on West Warren Avenue; and (3) a future Northeast Station (see Fig. 1). The water is taken from a new, lagoon type, intake built in the Detroit River just northeast of the up-stream end of Belle Isle and not far from the 1905 Intake crib, which will remain in service as an auxiliary intake, and will be carried through a system of gravity tunnels to the old station and across the city to the new stations. The intake, the Springwells Station, and the rawwater tunnel connections to Water-Works Park Station and Springwells Sta-

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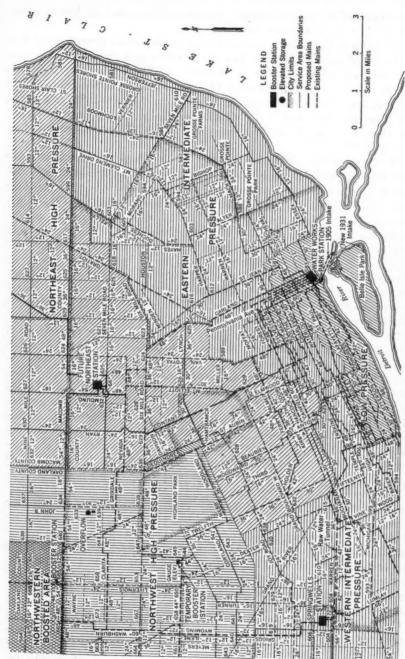


FIG. 1.-LOCATION OF PRINCIPAL WATER SUPPLY WORKS, METROPOLITAN AREA, DETROIT, MICHIGAN

tion are part of the present project. Northeast Station and the branch tunnel to it will be built at a future date.

The water to Springwells Station flows from the intake through 3 568 ft of concrete-lined tunnel, 15.5 ft in diameter, built in rock under the river, to a riser well and screen chamber on the shore at Water-Works Park; thence through 10 633 ft of concrete tunnel, 14.0 ft in diameter, in clay, north to the intersection of Pennsylvania and Forest Avenues; thence west through 44 705 ft of concrete tunnel, 12.0 ft in diameter, in clay, to the Springwells Station site, where it turns and enters the suction well of the raw-water (low-lift) pumping plant.

At this point the pumps elevate the raw water into the mixing chamber of the filtration plant through two 10 by 8-ft (or equivalent section) concrete conduits running behind the pumping plant and under the generator plant floor. The flow through the filtration plant is shown in Fig. 2. (The superstructures of the plant are not shown.) Just before entering the mixing chamber the water is metered through Venturi tubes cast in the concrete conduits. Coagulants or chlorine may be applied to the raw water at the entrance to the low-lift plant, at the entrance or exit of the raw-water meters, or at the entrance to the mixing chamber. Thorough and rapid dispersion of the chemicals through the water is accomplished by the turbulence in the pumps, meters, or entrance gates, as the case may be. In the mixing chamber the water is stirred by mechanical agitators and brick baffles.

The mixing chamber discharges into a conduit running the full width of the four settling basins, from which conduit the water may rise at two junction and gate wells which admit the water into the distributing channels of each basin. Entrance to the basins is through vertical slots spaced to give uniform distribution. After passing through these basins at settling velocities the clarified water is decanted from the surface by weirs, and flows into the filter building at two points through main conduits. At the filter operating galleries these conduits branch into the filter influent mains from which the inlets are connected to the sixty-eight rapid sand-filter units. The water flows on to the filter sand beds from the inlets and passes through 20 in. of sand and 18 in. of gravel to the perforated-pipe grid collector system below.

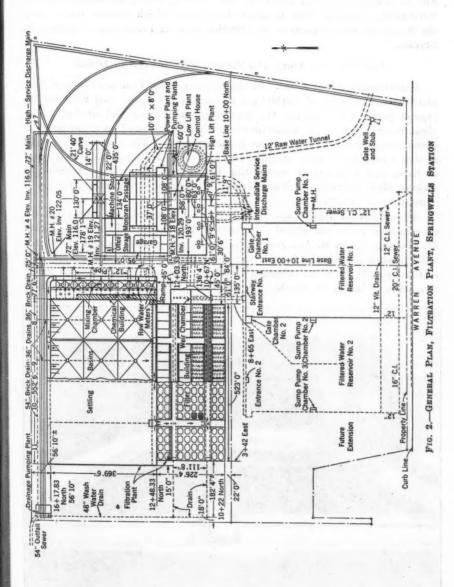
The filtered water that is collected is discharged through automatic rate-offlow controllers into the main filtered-water conduits in each of the two pipe galleries between the four rows of filters. The two filtered-water conduits discharge into a weir chamber at their eastern ends where the water level is controlled to maintain submergence of the filter-effluent piping as well as the high suction level on the distribution pumps when operated according to the shunt system, described subsequently. From the weir chamber the water may flow either directly to the pumping plant or into the filtered-water reservoir, as flow conditions demand.

Circulation in the filtered-water reservoir is induced by a center baffle-wall in each section and inlets and outlets controlled by flap check-gates. Water is drawn from the reservoir through conduits entering the opposite end of the pumping plant to that connected directly to the weir chamber. The dis-

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tribution pumps discharge through steel mains connected to each of two service districts (a high-pressure area and an intermediate pressure area, see Fig. 1), which are served jointly by the Water-Works Park Station and the Springwells Station. The detailed description which follows covers only the design and construction of the filtration plant and reservoir at Springwells Station.

## EXPERIMENTAL WORK AND STUDIES PRELIMINARY TO DESIGN

Experimental Filter Plant.—In the summer of 1925 an experimental filter plant with a capacity of 150 000 gal per day was designed and built for the express purpose of studying the phenomena of mixing and settling. This plant was composed of rectangular wooden tanks supported on a concrete mat foundation and enclosed in a light frame structure. The plant was arranged so that a reasonable range of times and velocities of mixing and a wide range of times and velocities in coagulation basins could easily be obtainable by making slight alterations. Two identical filter units were provided for use as a measure of results.

After about six months' operation in parallel with the large filter plant, the experimental plant was placed in charge of Mr. Roberts Hulbert and Frank W. Herring, Assoc. M. Am. Soc. C. E., who began on the program of settling-basin studies and obtained some very good results; but certain peculiarities in these results led to an intensive search to determine the reason for inconsistencies. Finally, the trouble was discovered in the fact that the two filter

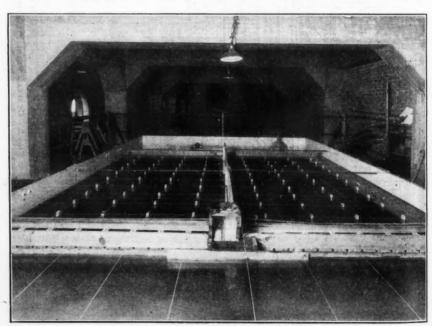


FIG. 3 .- VIEW OF SETTLING BASIN MODEL

units used to measure the results were not washed uniformly. Having become absorbed in the development of better methods of washing filters, the remainder of the time available for the experimental filter plant operation was spent on this subject and a technique was developed of washing them to a certain definite sand expansion, instead of at the usual constant rates of washwater flow.2

Scale Model Tests of Settling Basin Inlets.—Concurrently with the operation of the experimental filter plant, investigations of flow in settling basins were made by the use of a 1:25 scale model replica of the basin proposed to be used at the Springwells Plant. This model (see Fig. 3) was the means of determining the detail of inlet and outlet construction required to give a uniform distribution of flow across the full width of the basin and the longest actual retention period, as determined by floats, dyes, and salt solutions. Potassium permanganate dye was most satisfactory in determining the condition and distribution of flow by observing the advancing cloud of colored water. The time element was denoted by plotting the front edge of the color cloud at the end of each minute after the application of the color until it flowed out at the outlet. This plotting gave a record of each run, such as the typical form shown in Fig. 4.

The outlet conditions were early found to have little effect on the flow distribution. Therefore, attention was concentrated on the inlet detail. From the test results on the model, a vertically slotted wall inlet was adopted, with training walls between pairs of slots. The arrangement of the entrance baffles is shown in Fig. 4, with seventeen slots of the size and spacing indicated. In the entrance chamber the openings are beveled on the down-stream side (see Fig. 4(b) and Fig. 4(c)). Guide-vanes were of  $\frac{7}{16}$ -in. galvanized iron. The basins have "straight-through" flow.

Filter Under-Drain Lateral Experiments.—To determine how uniform the distribution of wash-water flow would be from a tentatively adopted design of filter under-drain lateral and to develop a low-cost brass, or bronze, bushing for the perforations in the under-drain laterals, a testing apparatus was built adequate for one typical full-sized lateral, almost identical in dimensions with those that would go into the actual filters. Several types of pipe materials in this apparatus, were tested, as well as types of perforations and bushings. Incidental to this test, a series of submerged orifices was calibrated and discharge coefficients were obtained.

Analytical Investigations and Studies.—Analytical studies were made to determine the economic size of filter units, economic filtering head, the design of the wash-water supply system (with particular regard to the relationship of the size of wash-water tanks and wash-water pumps supplying those tanks), and the costs of types of filter bottoms, wash-water trough materials, and chlorine-handling equipment.

General Basis of Design.—The ultimate capacity of Springwells Station was determined by a detailed study of the distribution system and the proper

<sup>&</sup>lt;sup>2</sup> "Studies on the Washing of Rapid Filters," by R. Hulbert and F. W. Herring, Journal, Am. Water Works Assoc., Vol. 21, November, 1929, p. 1445.

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division of load among the three plants designated by the consultant's report of 1924. This report and the results of experimental work and preliminary studies, together with previous experience, led to adoption of values given in Table 1, as the basis of design for the Springwells Filtration Plant. The

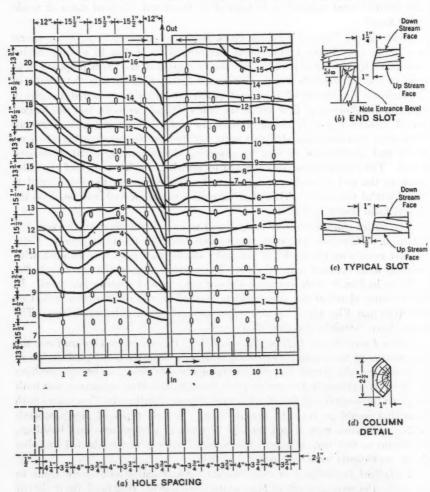


FIG. 4.-DETAILS OF MODEL AND TYPICAL RECORD OF TEST RUN

design required, furthermore, that coagulants should be applied to the initial mix at the pumps or the meters and that the mixing be by mechanical agitators. The design of the details of the settling basins was determined by scale model studies (see Fig. 4). The filter bottom specified was the perforated pipe grid type with a center manifold.

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<sup>&</sup>lt;sup>3</sup> "Trunk Main Water Distribution System for Greater Detroit," by L. E. Ayres, M. Am. Soc. C. E., Engineering News-Record, Vol. 100, No. 22, May 31, 1928, p. 855.

TABLE 1.—Design Factors: Springwells Filtration Plant

Item No.	Description	Value	Item No.	Description	Value
(a) UL	TIMATE CAPACITY (ESTIMATED AS OF	1955)		(d) Filters (Continued)	
1 2 3 4	Net Output, in Million Gallons Daily: (a) Average day. (b) Maximum day. Six filters supplying wash water, in million gallons daily. Required gross capacity, in million gallons daily. Filtered-Water Reservoir, in Million Callons: (a) Ultimate. (b) Present.	206 278 27 305	18 19 20 21 22 23 24 25	Size of Each Unit:  (1) Area of sand, in acres  (2) Filtering rate, in million gallons daily:  (a) Normal  (b) Maximum.  Number of filter units  Maximum velocity of influent, in feet per second  Operating head, in feet  Capacity of wash-water tank, in million gallons.  Capacity of wash-water pumps, in gallons per minute	4.0 4.5 68 9.5 0.1 28 000
7 8	Time of mixing contact at maximum capacity, in minutes	15		(e) STRUCTURAL LOADS AND STRESSE	:8
9 10 11 12 13	(c) SETTLING BASINS  Time of retention at maximum capacity (300 mgd), in hours  Velocity in basins, in feet per minute. Maximum Velocity, in Feet per Second:  (a) Inlets (b) Outlets  Number of basin units	2 to 3	26 27 28 29 30 31	Weight, in Pounds per Cubic Foot: Water. Earth. Concrete. Maximum Allowable Unit Stress, in Pounds per Square Inch: (1) Tension in reinforcement, for: (a) Floors, walls, and foot- ings (b) Roofs and Columns (2) Compression in concrete, for: (a) Floors, walls, and foot-	16 000 18 000
	(d) Filters		32 33	(b) Roofs and tied columns (c) Circular columns with spi-	650 750
14 15	Rate of Filtration, in Million Gallons Daily per Acre: (a) Normal. (b) Maximum. Rate of Washing, in Inches of Rise per Minute:	160 180	34	rals  Maximum allowable load on a bearing pile, in tons  Maximum Allowable Bearing Value of Earth Foundations, in Tons per Square Foot:	1 000
16 17	(a) Normal. (b) Maximum.		35 36	(a) Filtration plant structures. (b) Reservoir	

Horizontal earth pressures were assumed to be equivalent to hydrostatic pressures, plus surcharge when imposed. Live loads were determined by conditions in substructures; in superstructures, live loads were determined by conditions, or by reference to the Detroit Building Code, whichever was the higher.

#### DESCRIPTION OF PLANT

General.—The keynote of the entire design is practical simplicity. Attention was given to each detail to avoid complex situations which would be costly to build, or which later might cause trouble in operation and maintenance. Where auxiliaries have been used, such as master control for filters, summation devices for meters, float-controlled water-level indicators, float controls for pumps, etc., they have been installed so that their discontinuance from service will not interrupt the operation of the plant or affect the functioning of the standard equipment with which they are used. As a rule, automatic devices, such as the differential chemical feed, the automatic filter shut-off, the proportional chlorine feed, etc., have been avoided, preference being given to manual control where practicable.

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The construction of the conduits, chambers, basins, filters, and reservoirs, is of reinforced concrete. The superstructures have structural steel frames encased in concrete (with the exception of the steel frame of the Chemical Building which is only partly encased), reinforced concrete roofs insulated with cork and tar and gravel roofing, and hollow-tile curtain-walls faced on the outside with Indiana limestone and on the inside with terra cotta, glazed brick tile, or glazed hollow tile. The operating floors of the filters are finished with 6 by 6-in., red, quarry tile with dark green terrazzo borders. The floors in the Chemical Building, storage rooms, etc., are finished with concrete hardened with granite chips and ground smooth.

The entire structure is supported on a foundation of wooden bearing piles driven to hardpan through a subsoil of plastic and soft blue clay. The total load averages 20 tons per pile with the piles arranged so that, when the plant is entirely filled and loaded, there is a variation of not more than 5 tons per pile. On account of the unfavorable subsoil conditions, care was taken to avoid excessive concentrations of loads in the plant. Some variation in loading is occasioned by fluctuating live loads, such as in storage bins, basins, filters, and wash-water tanks.

Chemical Plant.—The Chemical Building is over a part of the mixing chambers, and contains the chemical storage tanks, chemical unloading and conveying equipment, the dry-feed machines, and hoppers for dosing ground sulfate of aluminum and ammonium sulfate. The arrangement of chemical equipment is shown in Fig. 5. This equipment is arranged so that, by a minimum of revision, the manufacture of aluminum sulfate may be provided for, at the same time preserving the dry alum equipment for stand-by service. The provision for alum manufacture contemplates making the alum syrup and feeding it as a solution.

The design of the Chemical Plant was based on the following capacities:

- (1) At maximum demand, a storage capacity of 30 days' supply of raw materials.
- (2) At normal demand, a storage capacity in each alum feeder bin, of 1 day.
- (3) At maximum demand, a storage capacity in solution feed tanks, of 1 day.
- (4) At maximum demand, a storage capacity for alum syrup, of 3 days.
- (5) Unloading equipment to handle a 40-ton car in 8 hr.
- (6) Reclaiming conveyors sufficient to handle 1 day's supply in 3 hr.

The equipment installed in the Chemical Plant consisted of the following:

- (1) Suspended steel storage tanks of 390-tons total capacity consisting of:
  - (a) Four storage tanks at 60 tons capacity each.
  - (b) Three storage tanks at 30 tons capacity each.
  - (c) Five feeder hoppers at 12 tons capacity each.
- (2) Pneumatic conveyor for unloading from railroad cars and delivering to storage (capacity 5 tons per hr).

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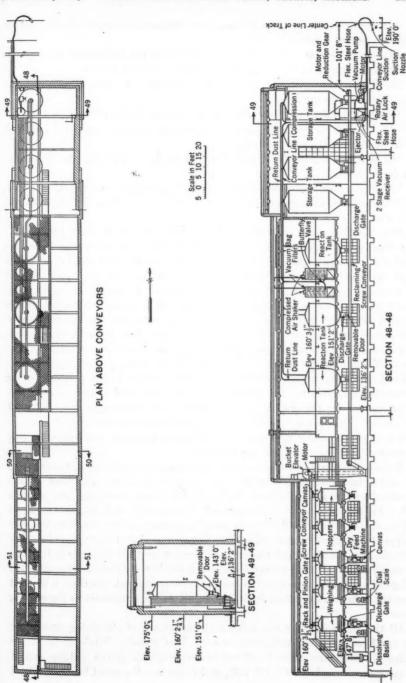


FIG. 5.—ARRANGEMENT OF CHEMICAL EQUIPMENT

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(3) Screw conveyor, 200 ft long, for reclaiming material from storage tanks (capacity 5 tons per hr).

(4) Bucket elevator for lifting material from the reclaiming conveyor to the conveyor above the feeder hoppers (capacity 6 tons per hr).

(5) Screw conveyor for distributing material to the feeder hoppers (capacity 6.6 tons per hr).

(6) Five dry-feed machines suspended from the feeder hoppers.

(7) A weighing scale for each feeder hopper and dry feed machine, with 30-in, indicator dial and recorder.

(8) A dissolving basin for each dry-feed machine, delivering to the chemical dosing lines.

(9) Three 3-in. dosing line headers of 99% pure copper extra heavy tubing, with stream-line fittings and valves of bronze composition resistant to the action of the alum solution.

Raw-Water Conduits and Meters.—The raw water is delivered to the mixing chamber through two 10 by 8-ft concrete conduits which run under the floor of the generator room in the power plant. At the west side of the power plant the conduits change shape to 9-ft square conduits and slope upward on a grade of about 12 per cent. In this section, a distance of about 60 ft, a raw-water meter is installed in each conduit. These meters are of the Venturi type with 9-ft square inlet and outlet ends and 4-ft square throats. The meters are cast of concrete with bronze-lined iron throat and pressurering castings and bronze-lined cast-iron inlet pressure rings set in the concrete. The raw-water meter registers are in a passageway of the building convenient to both alum and chlorine feeders. Dosing points for coagulating chemicals and chlorine are provided at both inlet and outlet ends of the meter tubes. In the design of the meter tubes advantage was taken of the upward slope in the conduits so as to compensate for their convergence in such a way that no air is trapped, on filling the conduits, and all water may be drained out, on emptying the conduits.

Mixing Chambers.—The dosed raw water enters the mixing chambers from the down-stream ends of the two parallel raw-water meters. The mixing chambers are in three units of approximately 5-min retention period, each with a by-passing channel. The general arrangement and details are shown in Fig. 6. The water enters the by-passing channel on the east side which is equipped with gates to shut off or admit water to any of the three chambers. Normally, the water enters through the three 6 by 10-ft sluice-gate inlets to the south chamber, flows northward through the three chambers (the dividing wall-gates of which are normally open) and leaves through the three 6 by 10-ft gates at the northwest corner into the coagulated water conduit to the settling basins.

All the sluice-gates in the mixing chambers are of the rising stem type, and are hand-operated, with worm-geared floor stands. While it is in the mixing chambers the water is stirred by mechanically driven paddles rotated at a peripheral speed of 0.67, 1.0, 1.33, or 2 ft per sec, the speed being regulated

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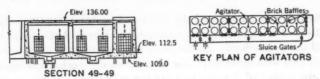
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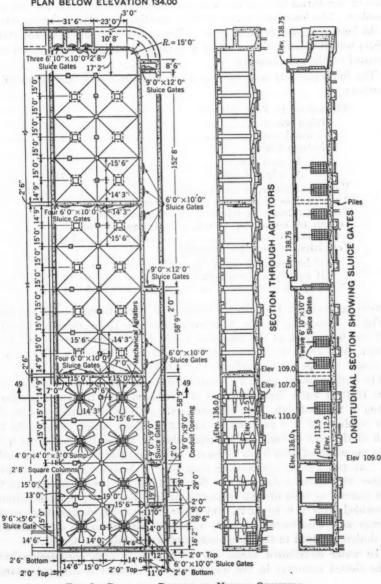


FIG. 6 .- PLAN AND DETAILS OF MIXING CHAMBERS

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to give the best conditioning of the water. At present (1934), only the first mixing chamber is equipped with agitators, and brick baffle walls have been built in all three chambers. As the plant load is increased the other chambers will be equipped with agitators. The location of the mechanical agitator units for the south section of the mixing chamber is indicated in Fig. 6. Steel-plate paddles, 10 ft long, are mounted spirally about a shaft of 12-in. steel pipe hung from a thrust-bearing in a base casting mounted on the cover slab of the chamber. The lower end of the shaft is steadied in a sleeve-bearing attached to the bottom of the chamber sump. This paddle assembly is driven through a 900:1 vertical reduction gear by a four-speed squirrel-cage vertical motor mounted on the gear housing.

The following data will serve as a summarized description of the mixing chamber:

Elevations, in Feet, Above:	
High water	131.6
Normal water	131.1
Bottom Slab:	
At wall line	112.5
At edge of sumps	110.0
Volume of water, in million gallons	3.201
Average dose of alum, in grains per gallon	0.6
Time of mixing, in minutes, at 300 mgd capacity.	15
Length of horizontal travel, with baffles, in feet	
(approximately)	000
Velocities, in Feet per Second:	
Of horizontal flow, at 300 mgd capacity	1.11
Of agitators (peripheral) 0.67	to 2.0
In gates 2.5	

Settling Basins.—The general features of the settling basins are shown in Fig. 7. Referring to Fig. 8, column vanes are 12 in. thick at Elevation 112.5 and 6 in. thick at the top, from Point A to the entrance baffle. Intermediate vanes are 6 in. thick at the top and 12 in. at Elevation 112.5 for their full length and the batter continues to the top of the vane.

The settling basins are in four units each about 135 by 340 ft in plan, with about 18 ft of water depth and 5 ft of free-board from the water surface to the top of the roof slab. The entrance wall, or inlet structure, consists of a lower conduit, 10 ft 8 in. wide by 12 ft 3 in. deep, which extends the full width of the four basins, and an upper channel which distributes the water across the width of each basin by means of vertical slot openings in its inside wall. At two points, one between each pair of basins, there is a junction chamber which allows the water to flow up from the lower conduit into the upper channel or inlet of each respective basin. Each inlet channel entrance is provided with a 9 by 12-ft. sluice-gate. The inlet channel and slotted openings were constructed as nearly as possible similar to the most favorable inlet design obtained in the scale model tests previously mentioned.

The water distributed across the north end of each coagulation basin by the slotted openings in the upper entrance channel is directed straight through the basin by straight vanes or by training-walls about 29 ft long. The water flows at a velocity of 2 to 3 ft per min for the 340 ft to the south end of the basins, where it is taken off over a weir. The weir is normally submerged about 11 ft, into a collecting conduit, 11 ft 6 in. wide by about 10 ft deep. The collecting conduits flow together at two points into junction chambers which admit the water to the Filter Building. Each collecting channel outlet is provided with a 9 by 12-ft sluice-gate for shut-off purposes. Beneath the collecting conduits is a by-pass conduit, 11 ft wide by 6 ft 6 in. deep, extending the full width of the basins, through which water may be by-passed directly from the mixing chamber to the filters. This conduit is also an equalizer of the flow from basins to the two filter influent mains. At the outlet weir there is a skimmer baffle and trough of somewhat unusual design, so constructed that, during short periods of high-water level in the basins, the collected scum will flush off into the drain. The skimmer trough acts also as an overflow.

To facilitate cleaning, the bottom of each basin is shaped into three shallow hoppers, with a sump at the center of each. A hydraulically operated 24-in. mud valve is operated on the basin drain line in this sump. The valves on the pressure lines for operating the mud valves are grouped in the two, outlet, junction-chamber, gate-houses. One basin is equipped with a perforated belt line of small pipe for flushing the floor during cleaning. If this proves efficient the other basins will be so equipped. A water main with hose connections is provided in each basin for use in cleaning.

Structurally, the basins are of simple reinforced concrete design; the side walls and division walls are of the cantilever type; the floor is of the flat-slab type; and the roof is a flat slab supported by cylindrical columns 30 in. in diameter, spaced 30 ft from center to center both ways.

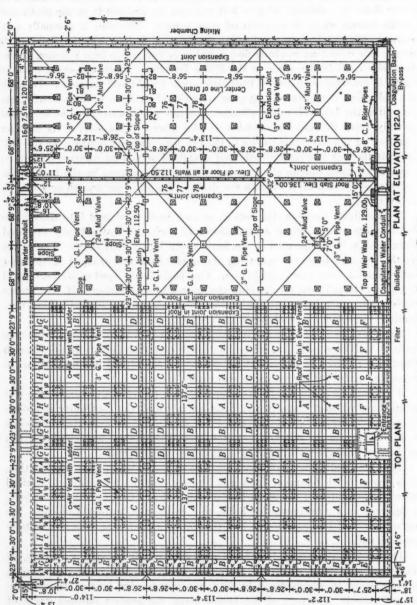
The roof-slab spans are 30 ft square between intermediate panels; the end panels have reduced spans in the direction in which the continuity is broken by walls and expansion joints. Since flat slabs of 30-ft span are quite close to the maximum in common use, the analytical design was checked by a mechanical instrument simulating a model of the structure.

The inlet and outlet wall structures are of somewhat special construction, as typical of such features: Inlet and by-pass conduits are designed as rigid monolithic structures; the slotted inlet wall, subject to little horizontal load, is designed as a curtain-wall or baffle, tied at the top, bottom, and ends; the outlet weir wall is a cantilever; and the junction chambers have horizontally spanned walls.

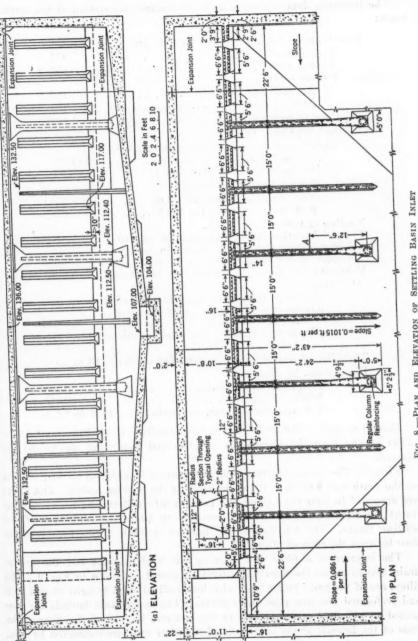
The roof of the basins is covered with 2 ft of fill, consisting of 6 in. of pea gravel and 18 in. of earth. Over each junction chamber is a gate-house superstructure in which the 9 by 12-ft sluice-gates are hoisted by electricity and stored. The part of the basins above the general finished grade of the site (Elevation 130.0) is faced with limestone to match the building group, and the curb wall retaining the basin roof fill is surmounted by an ornamental iron fence with stone posts.

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7.—General Plan of Settling Basin FIG.



8.-PLAN AND ELEVATION FIG.

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The following data will serve as a summarized description of the settling basin:

Elevations, in Feet, above Detroit City Datum:	
High water	131.0
Normal water	130.6
At wall line	112.5
At edge of sumps	107.0
Crest of outlet weir	129.0
Volumes, in Cubic Feet:	
Water in each basin (Elevation 112.5 to	
Elevation 131.0)	844 770
Sludge hoppers, below Elevation 112.5	86 675
Total capacity in four basins:	
With water at Elevation 131.0	3 725 780
With water at Elevation 130.5	3 634 460
Number of basins	4
Time of detention at 306 mgd capacity, in hours	2
Velocity of flow through the basin, in feet per	0.0
minute, at 306 mgd capacity Velocities, in Feet per Second, at 306 mgd	2.8
Capacity:	
Entrance velocity (normal water level) Outlet velocity over weir (normal	1.0
water level)	0.6
channel	1.0
Turbidity of settled water, in parts per million.	10 to 15
Dimensions, in Feet:	
Length of flow in basin	340.0
Width of one basin	135.5
Effective water depth, one basin	18.0 to 18.5

Slotted entrances and 29-ft guide-vanes constitute the baffling system; the outlet of the basin is operated as a submerged weir; and the basins are covered.

Filters.—The group of sixty-eight filter units is adjacent to and centers on the south wall (which is the outlet end) of the settling basins. The filters are arranged in four rows along two parallel pipe galleries with concrete influent conduits connected by cross-conduits to the outlet chambers of the settling basins. The top slab of the influent conduits forms the operating floor between the rows of filters.

The interior of a filter unit showing the wash troughs and the underdrain system before the filtering material is placed, is shown in Fig. 9. The filters are of the front gullet type, with longitudinal wash troughs of cast iron and perforated cast-iron pipe under-drains. The under-drain laterals are connected to a central manifold cast in the concrete bottom of the filter. The ends of the laterals at the side walls of the filter unit are connected by 4-in. cast-iron headers parallel to the walls to eliminate dead ends and to assure more uniform distribution of flow in the under-drain system. These wall November, 1934

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n nhe n. re all headers are perforated also to give a slight excess of wash water along the filter walls, during washing.

The filtering medium consists of an 18-in, depth of specially selected gravel and 20 in. of silica sand. The gravel grades in size from 3 in., maximum



FIG. 9.—VIEW OF INTERIOR OF FILTER, SHOWING UNDER-DRAIN SYSTEM AND WASH TROUGHS

diameter at the bottom, to 18-in. particles at the top of the gravel layer. The sand is 95% pure silica having an effective size of 0.5 mm and a uniformity coefficient of 1.3; 2% of it is composed of particles larger than 1 mm. The sand finer than 0.3 mm was washed out and is disregarded in computing the effective size and uniformity coefficient.

While it is filtering, water normally stands within 6 in. of the top of the filter walls, making about 7 ft of water depth on the surface of the sand bed. In washing, the sand expands 50% and rises to the bottom of the lower ends of the wash troughs.

A typical section of the pipe galleries and the piping for a typical filter unit is shown in Fig. 10. All header conduits are of concrete and are arranged to form the floor of the pipe gallery as well as the filter operating floor above. The filter connections are made with cast-iron fittings and flanged valves of the following sizes (in inches):

Influent	36
Effluent	24
Wash water	24
Sewer	30
Rewash	8

All valves are of the cast-iron, bronze-mounted, double-disk type, actuated by hydraulic cylinders operated from a marble-faced operating table or cabinet located on the filter operating floor at the front of each filter. All hydraulic cylinders are bronze-lined throughout, including the cylinder heads and pistons, and all pressure piping to the valve cylinders is of seamless copper tubing.

Each filter is equipped with a rate-of-flow controller of the Venturi type and a loss-of-head gauge, both actuating an indicating and recording gauge head mounted on the filter operating table above. The rate controllers are arranged for master-control setting or for individual setting as desired. The pipe galleries are heated by steam radiators and ventilated by a line of steel grating along each side of the operating floor of the filter.

The wash-water supply system consists of two pumps with capacities of 6 000 gal per min each, two pumps with capacities of 8 000 gal per min, located in recesses off one pipe gallery, and two 50 000-gal tanks in the cross-monitors of the Filter Building. The pumping capacity is sufficient for washing filters continuously, one at a time, while the tank capacity is sufficient for one single-filter wash. The depth of the wash-water tank and the rate of filter washing are indicated on a large illuminated gauge near the center of each operating gallery.

The following data will serve as a summarized description of the filters:

Rate of Filtration, in Million Gallons per Day, per	Acre:
Maximum Normal	180 160
Number of filter units	68
million gallons daily	4.5
General Dimensions, in Feet:	
Width of sand bed	27.00 40.33
Depth of filter box	11.0 4.44
Height, bottom of wash-water tank above sand surface	35.5
Detail Dimensions, in Inches:	
Diameter of connections:	
Influent Effluent	36 24
Wash water Drain	24 30 8
Re-wash	20
Gravel:	
Thickness of layer	18 3
Height, surface of sand to crest of wash troughs	40

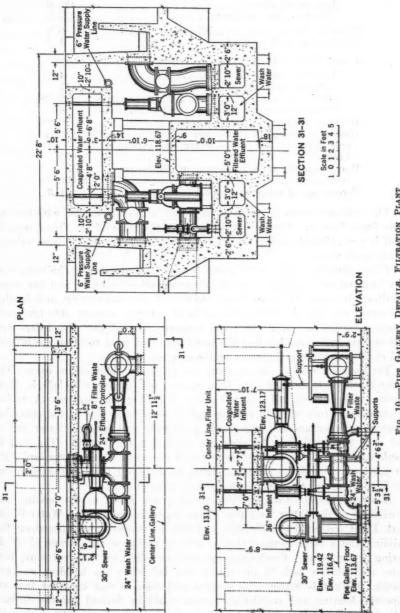


FIG. 10.—PIPE GALLERY DETAILS, FILTRATION PLANT

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Elevations, in Feet, above Detroit City Datum:	
Bottom of filter	$120 \ 0$ $130.5$
Effective size of sand, in millimeters Uniformity coefficient of sand	$0.5 \\ 1.3$
Under-Drains (Dimensions, in Inches):	
Laterals, size	4 12
Orifices, size	0.504
Orifices, spacing, center to center	6
Ratio of orifice area to sand area (× 100)	0.277
Rate of washing, in inches per minute  Tank capacity for wash water, in gallons	30 to 39 .
(net)	95 000
Pump capacity for wash water, in gallons per minute	28 000
Percentage of wash water used (average)	1.3

The strainer system is composed of perforated cast-iron pipe, with perforations brass bushed. The wash gullets are at the front of the filters, and the sand is not agitated during the washing process except by the high velocity of the wash water.

Filter Building.—The filter group housed in a single-story building with two longitudinal monitors, over the filter operating galleries, and two crossmonitors in which the wash-water tanks and air-conditioning and heating equipment are placed. This building is of concrete-encased, structural-steel frame construction, with reinforced concrete roof of the ribbed-slap type. The curtain-walls are of hollow tile faced with buff terra cotta on the interior and chat-sown Indiana limestone on the exterior.

The concrete ceiling and columns are painted a light cream color. The operating floor is finished with 6-in. square, red, quarry tile, laid in black mortar, with borders and spill-rail curbs of dark green terrazzo. A railing of ornamental iron with an oak top rail is along each side of the operating galleries. All ornamental iron work, steel floor gratings, ventilator grilles, and steel sash and door framing are painted a dark green. The roof is insulated with a  $1\frac{1}{2}$ -in. layer of pressed cork on top of which is standard 4-ply tar and gravel roofing. Large skylights of the vault type in the roof over the filters augment the light from the gallery monitors.

Heating System.—Considerable attention was given to the heating and ventilating of the Filter Building. Tests made in the existing Water-Works Park Plant indicated considerable variation in temperatures throughout the building and a large consumption of heat to maintain an average of 50° F during zero weather. Condensate was seen to collect on the steel work, root slabs, and window sash in the spring and fall when the building was not heated. With this example to observe and test, it was expected that an improved heating and ventilating system could be devised for the Springwells Filtration Plant. The uncertain heat loss to the open water surface of the filters complicated the problem considerably. Attempts to measure this loss failed, due to lack of instruments for measuring such a small temperature

change. A heat transfer coefficient of 2.00 was taken as the most probable for heat loss to an open water surface. In collaboration with experienced heating and ventilating consultants, the following outline of a heating system for the Springwells Filter Building was developed.

Heating.—The pipe galleries were to be heated by direct radiation; and the main building (except one room), by re-circulated air. The controlling temperatures, in degrees Fahrenheit, were:

Maximum	average,	contro	lled t	0								. 70	•
Minimum,	average											. 50	
Maximum	allowable	e varia	tion	in	woi	kii	ng	ar	ea			. 20	)
Maximum	temperat	ure of	heate	ed	air.							. 90	•

Ventilation.—The specifications required four changes of air per hour, re-circulated, with one change of fresh air admitted and tempered. Stale air was to be exhausted from the floor, at the ends of the pipe galleries, at the rate of ½ air change per hr. A probable air leakage of ½ air change per hr from the building was expected, due to maintaining inside the building, by means of the fans, a slightly higher pressure than normal atmospheric pressure. Re-circulated air was to be taken from the main roof at the center of the filter group and returned at the four intersections of the operating galleries, and at the cross-galleries. Maximum permissible air velocities, in feet per minute, were established as follows:

In	air ducts.											 			. (			600
At	outlets of	fans	 							 							1	600
Th	rough hea	ters	 							 							1	000

The total heat required to maintain the main part of the building at an average temperature of 50° F, with zero temperature outside, and with water at 32° F in the filters, was computed as 6 846 900 Btu per hr. This heat loss was apportioned as shown in Table 2. The loss in the pipe galleries could

TABLE 2.—HEAT REQUIRED TO MAINTAIN THE FILTER BUILDING AT 50 DEGREES FAHRENHEIT, WITH 0 DEGREES FAHRENHEIT, OUTDOORS

Surface	Area, in square feet	Heat, in British thermal units per hour	Surface	Area, in square feet	Heat, in British thermal units per hour
Glass	7 163 33 681 101 744	526 690 450 510 874 800	Skylights	9 360 80 784 21 960	598 000 2 586 000 131 400
For 1 air change (1 608 000 cu ft) per hr.					1 679 500

be estimated only approximately. Considering the exposed area of pipes as condenser surface and estimating 1 air change per hr due to convection currents, a total of 587 600 Btu per hr was computed as necessary to keep the pipe galleries above 50° F, with water at 32° F in the plant, and the main building at 50° F.

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The heating surface required was computed on the basis of 5-lb steam pressure in the heaters and radiators. An allowance of a 2-lb pressure drop in the steam lines between the source of the steam (the low-pressure side of the turbines in the generator room of the power plant) and the farthest heater, governed the sizes of steam pipes.

The heating equipment consisted of the following principal units, complete with accessories:

Four blower fans of 33 500 cu ft per min capacity of air at 70° F against a back pressure of 7/8 in. of water.

Four batteries of cast-iron heaters having 2 064 sq ft of heating surface each, for re-circulated air.

Four batteries of cast-iron heaters having 408 sq ft of heating surface each, for tempering fresh air.

Four dampered louvers for fresh-air intakes.

Four distributing louvers or diffusers for re-circulated air.

Four exhaust fans of 4 000 cu ft per min capacity of air at 70° F against a back pressure of 0.3 in. of water.

Twenty-eight radiators in pipe galleries, each of 126-sq ft heating surface.

Two vacuum return pumps for pipe-gallery radiation, each of capacity ample for 5 000 sq ft of radiation.

The re-circulating fans and air heaters are installed in the space beneath the wash-water tanks in the cross-monitors of the building. Condensed steam returns by gravity from the air heaters to a vacuum return pump in the basement of the plant office, which is on the route back to the boilers.

The steam main to the air heaters in the monitors is installed on the roof of the Filter Building with the air-recirculating duct. The steam supply lines to the pipe galleries are placed along the walls of the galleries. All steam lines and return lines are insulated with 85% magnesia pipe covering, re-canvassed. An exposed part of the steam main on the roof is also covered with a steel sheath. The heating system was installed during the time of interior finishing and was completed soon after the building was constructed.

Office and Laboratory Building.—This building was constructed complete under one general contract, including heating, ventilating, plumbing, electrical work, and all other trades. Its construction was typical of buildings of this nature.

The first floor contains offices in front for the filter plant superintendent, the power and pumping plant superintendent, the clerical force, and a conference or receiving room. The rear of the first floor contains locker rooms, shower rooms, and toilets for the plant workmen and operators, as well as a time office and storage rooms. The second floor contains the filter plant laboratory, with offices for the chief chemist and bacteriologist.

Weir Chamber.—It was required that the effluent water level be maintained at a height sufficient to submerge the filter-effluent connections and effluent-main conduits and to operate the shunt system. For this purpose, a chamber is provided, at the outlet ends of the filtered-water, effluent-main, conduits,

<sup>4 &</sup>quot;Shunt System of Operating Filtered Water Reservoirs," by E. A. Hardin, Engineering News-Record, Vol. 103, No. 26, December 26, 1929, p. 1011.

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which contains a filter-seal weir with crest at Elevation 118.00 and a reservoir weir, in two sections, with crest at Elevation 119.50, as shown in Fig. 11. This chamber is of reinforced concrete construction. In addition to its operating function it serves as a foundation for the plant office as well as providing

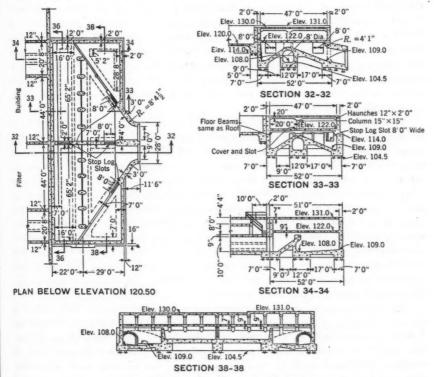


FIG. 11 .- SECTIONS OF WEIR CHAMBER

storage space for stop-logs, spare parts, castings, etc. The two sections of reservoir weir are built diagonally to gain length and also to converge the flow from the filter-seal weir to the entrance of the conduits leading directly to the high-lift pumping plant. A central division wall is provided for use in shutting off one-half the plant. Openings in this division wall and in the reservoir-weir walls (filled by stop-logs) are provided for flexibility in bypassing or running under special operating conditions.

Two 9 by 9-ft conduits which run from the weir chamber to the west end of the high-lift pumping plant, are designed to carry water direct to the pumping plant. An 8 by 8-ft conduit conveys water from the south end of the weir chamber to the filtered-water reservoir. The conduits to the pumping plant take the water that overflows the filter-seal weir, while the reservoir conduit takes the water that overflows the higher reservoir weir.

The Shunt System.—The shunt system is a method of operating the highlift pumping plant so that about three-fourths of the total pumpage is drawn

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directly from the filter plant at about 1½ ft above the level of the effluent-seal weir, while the remainder, which is taken on the daily peak, is drawn from the filtered-water reservoir at a level that may vary with the reservoir stage, from Elevation 120.0 to Elevation 108.0 each day. Thus, considerable head on the suction side of the pumps is conserved for most of the water pumped. This is accomplished by dividing the pumping units into two groups with a division wall in the suction gallery of the pumping plant. A small group at the remote end from the filter plant, comprising about one-fourth of the highlift pumping capacity, draws from the reservoir through Gate Chamber No. 1 and reservoir-outlet conduits connected to the east end of the pump suction gallery, while the remainder of the pumps draw directly from the filter plant, via the weir chamber.

The weir chamber effects the division of the water at the filter plant by a secondary weir, called the reservoir weir, the crest of which is high enough above the seal weir so that the entire flow of filter effluent may pass over it without overtopping the reservoir weir. The direct flow to the high-lift pumping plant is taken off between these weirs. Thus, the entire capacity output of the filter plant may pass directly to the high-lift pumps without affecting the reservoir levels at all. If the pumps taking suction direct from the filter plant do not require the full filter output, the effluent level rises until it overtops the reservoir-weir crest at Elevation 119.5, and the excess is discharged to the reservoir. During peak pumpage hours, when the output of the high-lift plant is more than that of the filter plant, pumps at the remote end are placed in service as required to meet the demand, and the pumpage in excess of the filter output rate is taken from the reservoir.

For convenience in operating the pumps, a water-level gauge is provided in the weir chamber between the two weirs and a control level of about Elevation 119.50 is maintained at this point. If this water level rises above Elevation 119.50, it is known that water is flowing into the reservoir and that, if possible, additional work by the pumps west of the division wall is permissible and less on the east side of the division wall is in order. If the control water level falls to Elevation 119.0, or below, less pumping west of the division wall, and more, east of the division wall, is desirable. To safeguard the operation of the pumps and to insure suction water from the reservoir to all pumps in the high-lift plant, flap-gates are provided in the suction-gallery division wall which are opened by the pressure from the reservoir-water side at any time the water level on the filter-plant side is below that on the reservoir side of this wall.

From the foregoing it is seen that by the shunt system the main flow of water from the filter plant is diverted directly to the high-lift pumps at a normally constant high level, and the reservoir is on a secondary loop, or shunt, feeding a small group of pumps, normally isolated as to suction from the remainder of the station. Experience with the shunt system at the Water-Works Park Station (see Fig. 1) has shown that it causes no inconvenience whatever in the pump operation. The pumps in the reservoir group, as a rule, are put in service only in peak hours and little concern is given the shunt system, which works automatically.

TABLE 3.—Computed Velocities, Head Losses, and Water-Surface ELEVATIONS

	All and the second	AVERAGE	CAPACIT MGD)	Y (210	MAXIMUM	CAPACIT MGD)	rr (306
tem No.	Point	Velocity in feet per sec- ond	Loss of head, in feet	Eleva- tion, in feet	Velocity in feet per sec- ond	Loss of head, in feet	Eleva- tion, in feet
	(a) Entra	ANCE TO M	IXING CH	AMBERS	,		
1	Elevation above Detroit City Da-	1		1	1		1
2 3 4 5 6 7	tum, in feet.  That are gates (two, 6 by 10 ft)  Mixing chamber.  Intermediate gates (four, 6 by 10 ft)  Outlet gates (three, 6 by 10 ft)  Conduit to coagulation basins	2.70 0.29 1.35 1.80 1.70 0.75	0.11 0.01 0.04 0.05 0.12 0.02	131.13	3.95 0.43 1.97 2.63 2.48 1.09	0.25 0.02 0.09 0.11 0.28 0.04	131.60
	(b) INLET I	END OF COA	GULATIO	N BASINS			1
8 9 10 11 12	Elevation above Detroit City Datum, in feet. Coagulation basins Basin outlet weir. Outlet channel and 9 by 12-ft gate. Junction chamber and settled water conduit to gallery (12 by 20 ft). Settled water conduit to Gallery 2	0.03 0.65 0.75 0.68	0.00 0.03 0.03 0.03	130.59	0.05 0.95 1.09 0.99	0.01 0.06 0.05 0.03	130.72
14	Filter influent header	0.7 0.7 to 0	regain		1.05 1.0 to 0	regain	
15	Filter inlets	0.77	0.02	1	0.99	0.04	1
		(c) Filt	ERS				
16 17 18	Elevation above Detroit City Datum, in feet Filters (available operating head) Filter effluent piping and wide-open rate controller	1.72	9.95	130.50	2.22	9.11	130.50
	(d) NORMAL GRADIENT	IN UP-STRE	AM END	of Efflu	ENT HEADEI	3	
19 20	Elevation above Detroit City Datum, in feet		0.26	119.92	0.36 to 4.83	0.55	120.36
	(e) Above Eff	FLUENT WE	IB IN WI	EIR CHAM	BER		
21 22	tum, in feet	1.63	0.16	119.66	3.09	0.31	119.8
	(f) Below Er	FLUENT WE	IR IN WI	EIR CHAM	BER	11 7 1	
23 24 25	Elevation above Detroit City Da- tum, in feet. Conduits to high-lift pumping plant (two, 9 by 9 ft). Entrance to 50-mgd pump suction chamber (6 by 6-ft sluice-gate).	2.0	0.10	119.50	2.9	0.21	119.50
(T)	(g) High-L	IFT PUMPS	ON DIRE	CT DRAFT			
26	Elevation above Detroit City Da- tum, in feet		1	119.20	1	l	119.0
	(h) Normal	HIGH-WATE	R LEVEL	IN RESEI	RVOIR	lo din	
27	Elevation above Detroit City Da- tum, in feet		l	119.00		l	121.0
	(i) Low-	WATER LEV	EL IN R	ESERVOIR			
28	Elevation above Detroit City Da- tum, in feet	1	b. 1	103.00	J	lucot)	103.0

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Hydraulics of Flow Through Plant.—The computed velocities, head losses, and water-surface elevations at governing points throughout the plant are given in Table 3 for both a maximum-capacity flow of 306 000 000 gal daily, and an average-capacity flow of 210 000 000 gal daily. For these computations it is assumed that the water-surface elevations in the filtered-water reservoir are less than 119.5. When the reservoir is at higher stages, up to its normal high-water level of Elevation 121.00, the filter effluent levels will be raised correspondingly (except for the slight effect of the greater submergence of the effluent weir), thus reducing the available operating head of the filters at times of high water in the reservoir.

Under-Drainage System and Main Drains for Plant.—The entire sub-grade area of the filtration plant and reservoir is provided with drains for controlling the elevation of the ground-water under the plant. The drains are of 6-in vitrified sewer pipe laid with open joints in shallow trenches at the surface of the sub-grade and surrounded by open gravel. They are spaced approximately 7 ft from center to center, located so as to clear the piling. Under the coagulation basins and mixing chamber and under the floor-slabs of the filters there is also a layer of open gravel about 4 in. thick for distributing the water between the drains. There is no gravel layer between the drains under the reservoir. There are no drains under the wall footings and the pipe galleries. In addition to the under-drains there is also a belt drain of perforated, 12-in., cast-iron pipe laid completely around each structure at the top of the wall footings to intercept ground-water from the surrounding area.

The drainage system under the structures constituting the filtration plant is connected to the main drain from the plant by an overflow connection which discharges water when the level is above Elevation 118.5. It is expected that, usually, there will be a flow from the drains due to leakage and ground-water; but to assure a ground-water level at sufficient height to cover the timber piling a water-supply connection is provided with a float-operated valve that admits water to the drainage system when the level in it becomes less than Elevation 118.5 (which is 4 ft above the top of the highest pile).

The level in the reservoir drainage system is maintained at desired levels by float-controlled sump pumps which discharge into the sewer.

Filtered-Water Reservoir.—The reservoir for filtered water consists of two sections, each with a capacity of 20 000 000 gal, and each a rectangle, 455 ft long by 313 ft wide (interior dimensions). There will be a third section, eventually, of about the same size. Water flowing to the reservoir is distributed to the sections by a conduit, built along the north wall, which is connected to the sections through a gate-chamber in each one and also through an additional 66-in. inlet valve in the east section. In each gate-chamber are four 48-in. double-disk gate-valves, hand-operated by geared floor stands with cranks. The water may enter or leave through these valves. Flap check-valves are placed on the gate-valve openings in such a manner that the water flows in through the valves on one side of the center baffle-wall and out through the valves on the other side. By this means, water may be circulated through the reservoir sections, if desired. In the east section, the 66-in. valve serves as the inlet, and two of the 48-in. valves equipped with

flap-gates serve as the outlet, to produce circulation around the baffie-wall. Figs. 12 and 13 give the general plan and sections of the existing sections of the reservoir.

The reservoir is constructed of reinforced concrete of standard design. The walls are one-way slabs spanned vertically between the base and the roof. The roof and floor are of typical two-way flat-slab construction with cylindrical columns spaced 20 ft center to center both ways.

The reservoir is completely back-filled and its roof is covered with 6 in. of gravel and 18 in. of earth. It thus forms the front-yard area of the station and will be landscaped and planted. Water is drawn from the reservoir to the pumps in the east end of the high-lift pumping plant through two, 8-ft square, concrete conduits running from Gate Chamber No. 1 to the east end of the suction gallery in this pumping plant.

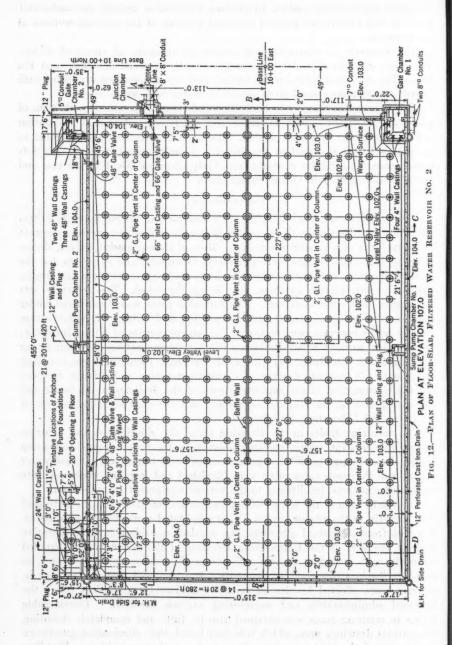
#### Construction

General Plan and Administration.—In constructing the Springwells Filtration Plant and Reservoir, the Board of Water Commissioners acted somewhat in the capacity of a general contractor. Most of the equipment, valves, sluicegates, piping, and castings were purchased separately, and contracts for the construction work and installation were let to building contractors and trades, this equipment, piping, castings, etc., being furnished. The reservoir was constructed under two contracts. The filtration plant was constructed under eight seperate major contracts: (1) Excavation and piling; (2) substructure (mostly heavy concrete construction); (3) superstructure of Filter Building; (4) electrical work in Filter Building; (5) plumbing, heating, and ventilating work in Filter Building; (6) Chemical Building, including alum-handling equipment; (7) masonry facings of coagulation basins and mixing chamber and the construction of the superstructures of the drainage pump house and two gate-houses on the coagulation basins; and (8) complete construction of the Office and Laboratory Building.

The operating tables in the filtration plant, the chlorinators and chlorine piping, the chlorine scales, chlorine hoist, pressure water pumps and sump pumps, drainage pumps, filtered water meters, wash-water pumps, wash-water meters, and the wash-water pipes were furnished and installed under separate equipment contracts, let directly to the various equipment manufacturers.

The subdivision of the work resulted in smaller contracts and the letting of work directly to the proper trades. This eliminated considerable administration cost from the actual contracts, but required considerable administrative work on the part of the Engineering Division of the Board (which handled the work) with attendant expense reflected in the engineering cost figures, as shown in Table 4 discussed subsequently. It is believed that the savings in contract costs effected by this procedure considerably more than offset the increased administrative and engineering expense involved. Considerable saving in contract costs was obtained also by fully and completely detailing the contract drawings upon which bids were based, thus eliminating guesswork on the part of the bidders and resulting in low and close bidding. Dividing the work in this manner expedited the construction since construction was





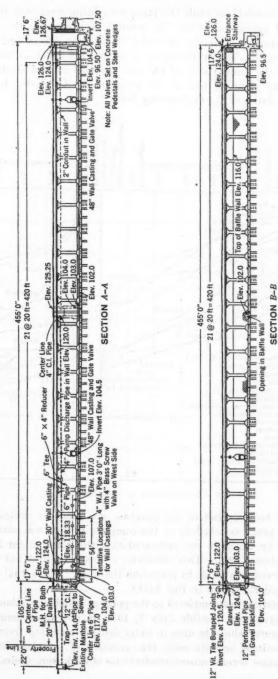


Fig. 13.—General Sections, Filtered Water Reservoir No. 2

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begun on the foundations while the plans were being completed for the superstructures and subsequent work. To schedule and expedite the various purchases and contracts properly, in order to prevent delays and to preserve harmonious working conditions where a number of different contracts were under way on the limited area of the site, involved careful attention both to the preliminary planning and to the progress of the work. It also added greatly to the duties of the engineering force.

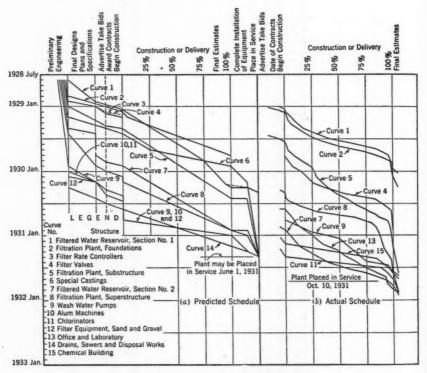


FIG. 14.-PROGRESS OF CONSTRUCTION

Progress Schedule.—Before any purchase was made or contract prepared, a preliminary progress schedule of the complete project was made as shown in Fig. 14(a) by which it was estimated that the plant might be placed in operation by June, 1931. This schedule, of course, could not be followed exactly, but served as a guide in preparing the work. The actual construction schedule is similarly shown in Fig. 14(b).

The construction was completed to the point at which operation of the filter plant would have been possible July 1, 1931, if the water demand had required it. However, since the drop in water demand resulting from the general recession in business activity made the operation of the plant less urgent at the time, and since several miscellaneous items of work were desirable and more

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economical to be done before the plant was put in service, the actual operation was begun on October 10, 1931, about four months later than scheduled.

Construction Methods.—There was nothing particularly special or peculiar about the construction of this project. Standard first-class construction methods were used throughout. Most of the excavation was by drag-line excavators and shovels. Piles were driven by ordinary wooden skid drivers. Concrete was mixed in a central mixing plant for each job and transported to the forms by chutes, belt conveyors, and industrial train, each contract making use of a different transporting method. The mixers were all of about 1 cu yd capacity. The superstructure work was typical of such construction. The major part of the structural work, except the excavation and pile-driving for the Filter Plant, was done by two contracting firms, the W. E. Wood Company and the Bryant and Detwiler Company, of Detroit, Mich. The Whitney Brothers Company, of Duluth, Minn., did the excavation and piling work for the filtration plant.

The construction photographs, Figs. 15 to 18, inclusive, show the magnitude and type of the construction work. They were taken from the same point (the top of the concrete mixing plant) and show the filtration plant in successive stages of construction.

The principal problems of construction arose from the magnitude of the project and the extent of the area covered by the plant structures, and were mainly problems of transportation. Approximately 18 acres were occupied by the actual structures themselves and large volumes of materials had to be handled for considerable distances over this construction area while many large pipe castings, valves, and pieces of equipment had to be installed as the work progressed.

A general idea of the magnitude of the work may be obtained from the following summary of the approximate quantities of the principal construction materials that went into the Springwells Filtration Plant and Reservoir:

Excavation, in cubic yards	420 000
Timber bearing piling, in linear feet	1 500 000
Concrete, in cubic yards	120 000
Reinforcing steel, in tons	7 200
Concrete forms, in square feet	2 000 000
Structural steel, in tons	1 120
Ornamental iron, in tons	70
Iron pipe and castings, in tons	2 000
Gravel fill and drainage material, in cubic yards	15 000
Tile under-drains, in linear feet	56 000
Stone masonry, in cubic feet	42 000
Brick and tile masonry, in cubic feet	77 000
Terra cotta, in square feet	33 000
Steel sash, in square feet	11 000
Metal doors, in square feet	1 000
Tar and gravel roofing (squares)	1 250
Skylights, (vault type), in square feet	11 000
Cork insulation, in square feet	134 000
Copper roofing and flashing, in square feet	35 000
Terrazzo and ground concrete floors, in square feet	30 000
Quarry tile floors, in square feet	22 000

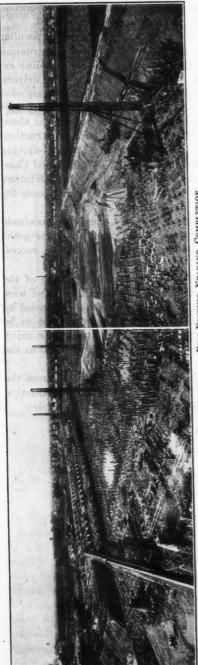


Fig. 15.—EXCAVATION AND PILE-DRIVING NEARING COMPLETION

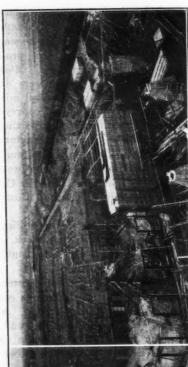


FIG. 16.—CONSTRUCTING FILTER WALLS AND MIXING CHAMBER







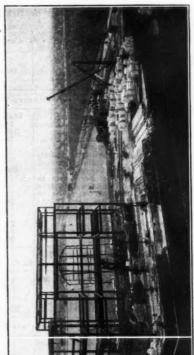
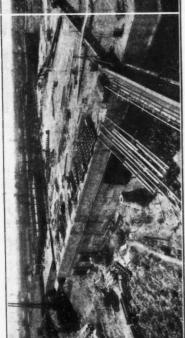


FIG. 18 .- CHEMICAL BUILDING STEEL WORK ERECTED



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### TABLE 4.—Cost of Springwell's Filtration Plant

tem No.	Units constructed						
- 1	Onus constructed	Units constructed Actual Adjust to 1913 costs by Index Number		costs	Date of receipt of bids	index based on the year 1913 as 100	
	(a) FILTE	RED-WATE	R RESE	RVOIR			
1]	Section 1: Contract	\$541 478	\$258	585	January 16, 1929	\$209.4	
2 3	Section 1: Force account work Section 2: Contract	14 055 347 226	176	789 382	December 2, 1930	207.0 196.8	
4	Section 2: Force account work	16 612	8	160		181.3	
5	Section 3: Force account work Section 3: Future construction (esti-	125		74	**************	170	
0	mated cost, including grading,						
7	planting, and roadways). Sections 1, 2, and 3: Equipment, including valves, pumps, and level gauges (installation of valves included in Items Nos. 1 and 3)	400 000	238	300		170	
	Cost of Engineering:	56 971	27	770	May 13, 1929	205.1	
8	Total, exclusive of supervision on Section 3	74 577	36	028		207	
9	Estimated for supervision on Section 3	20 000		1 765		170	
10	Total cost of reservoir (60 mg capac-	20 000	-	. 100		110	
10	ity)	\$1 471 044	\$76	1 853			
11	Cost of engineering (\$94 577), in per-	0.4					
12	centage of total cost	6.43				*****	
	(60), including engineering, inci- dental expense, and contingencies.	\$24 513	7 01	2 698			
	dental expense, and contingencies .	924 31	1 91.	2 090	1	1	
-	(b) Filtra	ATION PLAN	NT STRU	CTURE	8		
	Foundation Work (Excavation and Pile-Driving):						
13 14	Force account labor and miscel-	\$607 03	5 \$28	8 515	February 6, 1929	\$210.	
	laneous expense on foundation	40.00				000	
	workSubstructure Construction:	19 69	2	9 512		207.	
15 16	Force account labor and miscel-	1 518 57	4 74	1 600	July 10, 1929	204.	
10	laneous expense on substructure						
1	construction	55 68	0 2	7 449		202.	
17	Contracts	604 75	4 29	1 982	April 30, 1930	207.	
18	Force account labor and miscel-	25 91	0 1	2 773		202.	
	laneous expense.  Chemical Building, Including Mechanical Equipment, Chemical-Handling Equipment, Heating, Ventilating, Plumbing, and Electrical Work:						
19 20	Force account labor and miscel-	178 10	0 9	1 577	January 27, 1931	194.	
20	laneous expense	11 71	3	6 459		181.	
21	Contract	46 38		7 318	October 20, 1931	169.	
22	Water conduits to and from pumping	1 74	6	1 032		169.	
20	plant and reservoirs	90 71	0 4	3 796	April 30, 1930	207.	
24	Substructure by force account labor	45 38		5 088	April-September, 1931		
25	Superstructure by contract Plant Drains and Sewers:	18 73	4 1	1 034	October 20, 1931	169.	
26 27	By force account labor By contract	60 72 13 36		3 568 6 527	April-September, 1931 July 10, 1929		
28	Total cost of Filtration Plant (struc-						
	tures)	1\$3 298 49	7  \$1 61	8 230	1	.1	
	(c) Filtr	RATION PLA	NT EQU	IPMEN	T		

# TABLE 4.—(Continued)

		Const	RUCT	TON CO	ST		Cost
tem No.	Units constructed	Units constructed Actual Adjust to 1913 costs by Index Number					based on the year 1913 as 100
	(c) FILTRATION F	LANT E	QUIP	MENT-	(Cont	inued)	
	Sluice-Gates and Valves:					(October 21, 1929	
30	In coagulation basins	\$53	-	\$25		October 21, 1929 January 6, 1930 October 15, 1929	\$206.32
31 32	In mixing chamber	135	970	65	903	October 15, 1929	206.32
33	stalled (estimated)	30	000	17	647	(Future)	170
-	stalled	9 :	326	4	697	November 11, 1930	198.54
34	Filtered water meters and gauges, installed	4 (	096	2	137	April, 1931	191.63
35	Water-level gauges and signal system,	15	545		303	June, 1931	187.23
36	Pressure piping in coagulation basins,						
37 38	Stop-logs and flash-boards, installed Auxiliary equipment, including pres-		338 451		291 766	May, 1931 May, 1931	189.33 189.33
	sure pumps and sump pumps in pipe galleries, installed		947		104	April 14, 1931	191.63
39 40	Sample pumps and piping		868		453		191.63
41	cluding meters and valves, installed Chlorinating equipment and piping, including feeders, scales, and all dosing lines, installed.	79	921	39	772	July 15, 1930	200.98
	dosing lines, installed	33	257	17	098	March 31, 1931	194.51
42	Total cost of Filtration Plant equip- ment, installed	\$386	251	\$195	169		
		FILTER			200		
43	Filter operating tables, including pres-			1		ı	1
20	sure tubing, installed	\$55	547	\$27	952	October 7, 1930	\$198.7
44 45	Filter Rate Controllers and Gauges: Delivered	93 16	958 377		220 998	March 6, 1929 July 10, 1929	207.7 204.7
46	Filter Valves: Delivered	214	569	103	005	March 2, 1929 November 1, 1929	208.1
47	Installed by contract		297		587	November 1, 1929    July 10, 1929	204.7
48	Filter Piping and Special Castings:		614		345		
49	DeliveredInstalled by contract	10	603	5	178	May 16, 1929 July 10, 1929	205.1
50 51	Delivered. Installed by contract		553 773		190 261	May 16, 1929 July 10, 1929	205.1 204.7
52 53	ports: Delivered. Installed by force account labor Filter Gravel:		$\frac{627}{241}$		975 726	January 16, 1931 July, 1931	194.4 174.3
54 55	Delivered		116 668		576 766	May-September, 1931. May-September, 1931.	
56 57	Delivered		264			March 24, 1931	194.5
58 59	Placed by force account labor Miscellaneous general expense Filter sand in place for forty-six filters	2	891 783	1	392	May-September, 1931.	200
60	(estimated)	37	000	21	765	(Future)	170
_	stalled	\$716	874	\$357	186		
61 62	Total cost of Filtration Plant con- struction, fully equipped Total cost of engineering, including	\$4 401	622	\$2 170	585		
	design, supervision, and administra-		518	197	835		\$207
63	Total cost of Filtration Plant (300 mgd capacity)			\$2 368			
64	(including basin-model tests, experi- mental filter plant, filter under-		110	2 508		. 0	4 11
	drain, sand-washing studies, pile testing, soil testing, and roof load						10

TABLE 4-Continued.

		CONSTRUCT	TION COST		Cost	
Item No.	Units constructed	Actual	Adjust to 1913 costs by Index Number	Date of receipt of bids	based on the year 1913 as 100	
	(d) FILTER	EQUIPMENT	-(Continued	)		
65	Engineering cost (percentage of total cost)	8.51				
67	of total cost	1.68	********			
	experimental work)	\$16 037	\$7 895			
	(e) Office .	AND LABORA	TORY BUILDI	NG		
68 69 70	Foundation work. Building construction Heating, ventilating, and plumbing. Electrical work, including clocks and	\$31 928 91 370 39 595	\$15 997 45 781 19 839	September 2, 1930 September 2, 1930 September 2, 1930	\$199.5 199.5 199.5	
72 73	gauges Laboratory equipment Engineering cost, including design, supervision, and administration	19 598 5 018 60 041	9 820 2 423 29 577	September 2, 1930 April 1, 1930	199.5 207 1 \$203	
74	Total cost of Office and Laboratory Building		\$123 437			
		(f) SUMMA	RY			
75 76 77 78	Reservoir (60 mg capacity) Filtration plant (300 mgd capacity) Experimental work. Office and Laboratory Building	\$1 471 044 4 811 140 80 898 247 550	\$761 853 2 368 420 39 081 123 437			
79	Total	<b>\$6</b> 610 632	\$3 292 791			
80 81	Total engineering cost (included in Items Nos. 75 to 78). Engineering cost in percentage of total cost.	\$564 136			1	

#### COST ANALYSIS

Before the beginning of any construction work on this plant, a Cost Accounting Bureau was organized with competent clerks and bookkeepers to keep complete records of the actual cost of the various features of the work as nearly as could be obtained by independently taking the time and material used in the work and checking where possible with the contractors' records. The costs of the main units of the plant as compiled from the account ledger are given in Table 4. These costs represent not only the contract costs, but also all costs incidental to the work, including force account work done by direct labor. The engineering costs include all design work, checking, preparation of plans and specifications, consulting architects' and mechancial engineers' fees, printing of plans and specifications, supervision of construction, time-keeping, clerical work, purchasing expense, checking of shop details, inspection of materials, shop inspection, and general administration of the work. The cost of experimental work is listed separately. For ease in comparing with other projects the costs have also been reduced to the basis as of the year 1913 by using the construction cost index figures of the Engineering News-Record.

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### ACKNOWLEDGMENTS

The design and supervision of construction of the Springwells Filtration Plant was done by the Filtration Bureau of the Division of Engineering formed by the Board of Water Commissioners of Detroit for this purpose. This Division worked under the general superintendence of George H. Fenkell, M. Am. Soc. C. E., General Manager and Chief Engineer, and F. H. Stephenson, M. Am. Soc. C. E., Engineer of Water System, of the Department of Water Supply. The Filtration Bureau was in the general charge of A. B. Morrill, M. Am. Soc. C. E., Assistant Engineer (Filtration), with the writer in charge of design, and J. W. Orton, Assoc. M. Am. Soc. C. E., Assistant Civil Engineer in charge of construction. Mr. J. C. Thornton, Architect, was responsible for the architectural work, and the E. R. Little Company, Mechanical Engineers, consulted on the heating and ventilating design. Mr. E. W. Frey, Accountant, had charge of the keeping of costs and records.

### Conclusions

The execution of this project has contributed to the progress of water purification practice: (1) In the development of knowledge of the flow in coagulation basins and distributing inlet details by experimental model investigation; (2) in the development of higher rates of filter washing and their control by sand expension; (3) in the conception and development of the shunt system of operating filtered-water reservoirs; and (4) in the improvement of details, such as low loss-of-head rate controllers, summation of Venturi meters, perforated pipe filter under-drains, and chemical handling equipment.

# AMERICAN SOCIETY OF CIVIL ENGINEERS

### Founded November 5, 1852

### DISCUSSIONS

# MODIFYING THE PHYSIOGRAPHICAL BALANCE BY CONSERVATION MEASURES

### Discussion

By A. L. SONDEREGGER, M. AM. SOC. C. E.

A. L. Sonderegger, 60 M. Am. Soc. C. E. (by letter). 60a — More than gratifying have been the discussions in that they have brought out many points of interest and importance in stream control and conservation. Like the subject of the paper, the discussions have covered a large range of thought and observation. Most of the discussers appreciate the necessity of a correct evaluation of the effect of modern works on natural processes and the physiographical balance. Engineering science has made great strides in the theoretical analysis of strains, stresses, and forces, and has succeeded in clothing important results of research in convenient formulas for the ready use of a learned and busy profession. On the other hand, the study of natural phenomena and a correct appraisal thereof proves to be a matter of experience rather than of learning and, as a rule, is not acquired without reprimand by failure. Hence, it would not be astonishing if subjects like the disturbance of the physiographical balance would find more appreciation with the older members of the profession than with the recent graduate who is justly proud of his newly acquired knowledge.

The importance of the water-shed cover and its effect on run-off and débris production is touched upon by several discussers. Mr. Lippincott's discussion, is particularly illuminating in this respect, in that it is supported by comparative data relative to the effect of the vegetal cover in its natural condition and after one or more burnings. He concludes that "greater effort should be made than in the past to preserve the brush cover from fire." While this is a desirable objective, it must be borne in mind that the preservation of the brush cover over a long period of years promotes the accumulation of highly inflammable materials which, when set on fire, are difficult of

Note.—The paper by A. L. Sonderegger, M. Am. Soc. C. E., was published in December, 1933, Proceedings. Discussion on this paper has appeared in Proceedings, as follows: March, 1934, by Messrs. H. H. Chapman, and E. B. Debler; April, 1934, by Messrs. Frank E. Bonner, and C. S. Jarvis; May, 1934, by Messrs. W. P. Rowe, and J. C. Stevens; August, 1934, by Gerard H. Matthes, M. Am. Soc. C. E.; and September, 1934, by Messrs. J. B. Lippincott and Rhodes E. Rule.

<sup>56</sup> Cons. Engr., Los Angeles, Calif.

<sup>586</sup> Received by the Secretary September 18, 1934.

control. Fires will continue to occur; in fact, with an ever growing population and greater facilities of access to the water-shed, the odds are in favor of an increasing fire hazard.

These considerations may have induced Mr. Rowe's point of view, namely, that of periodical controlled burning. Possibly the solution to this perplexing problem is already found in the present policy of the responsible authorities, of maintaining efficient fire-fighting organizations and completing the network of mountain roads which will permit the rapid conveyance of crews and apparatus to strategical points while fires are in their incipiency. While the number of fires may continue to increase, the probabilities are that, with improved methods and perfected organizations, damages will be confined to smaller areas. Thus, a system of rotation of burning may evolve which will eliminate major conflagrations, at the same time relieving authorities of the risks and responsibilities that attend controlled burning.

The La Crescenta-Montrose flood discussed by Messrs. Lippincott and Rowe, and referred to by others, has brought out several distinct facts bearing on the flood-control problem of Southern California: (1) That brush fires are a permanent menace at any point; (2) that run-off from tributaries may assume such proportions as to overtax existing flood channels of main streams; (3) that débris production from burnt-over areas may be of such magnitude as to be a menace to foothill areas and to the storage space of flood-control detention reservoirs; and (4) that a material increase in the peak discharge of both water and débris may result from the failure of temporary check dams.

Mr. Jarvis takes exception to the writer's statement that a permanent decrease or increase of 20% of the mean rainfall of semi-arid areas might result in far-reaching climatological or physiographic changes, while Mr. Stevens challenges the general statement that physiographical factors combine to produce a balance, even under existing conditions. The viewpoints are distinctly at variance.

It is admitted that, in the Southwest, cyclic fluctuations of seasonal rainfall in the past, which resulted in wet and dry periods of 10 to 15 yr each, seemingly had no effect on the development of the country, or on the earth's surface. As far as farm husbandry is concerned this is explained, in part, by the utilization of underground storage which, over large areas, yielded abundant supplementary supplies for the relatively short period of droughts. With a permanent reduction of 20% in the mean seasonal rainfall, the periods of relatively low water supply would necessarily be extended and periods of recharge correspondingly shortened, leaving no doubt as to the ultimate effect on the safe water yield of large areas.

The natural vegetal cover of the water-shed, as a rule, is a fair index of the mean seasonal rainfall, expressed in the prevailing species, as well as in the vigor and size of individual plants. In fact, with some experience in these matters, it is feasible to estimate with a fair degree of accuracy, the seasonal rainfall by the character of the vegetal cover. The difference in appearance of water-sheds receiving 12 in., 15 in., and 18 in. of mean seasonal rainfall is striking enough to leave no doubt as to Nature's adjust-

ment to mean climatic conditions. Similarly, general topographic conditions must be the result of some combination of the effect of the controlling causes. If the latter undergo permanent changes, a reflection in effect is inevitable. Nature, like the "mills of the Gods", may grind slowly, yet it grinds exceedingly fine.

Mr. Stevens' standpoint is scarcely justified. Nature's adjustments must be to some mean condition which undergoes only gradual changes; otherwise, human settlement would be forced to make way to a nomadic existence. Exceptions to this rule, due to local disturbances by reason of floods, wind storms, fires, etc., no doubt take place, and may result in radical changes of physiographical features — often temporary, sometimes permanent — but they effect a relatively insignificant portion of the inhabitable areas.

Professor Chapman makes some rather startling assertions in that he claims (1) that the physiographical balance is maintained over large areas in the West by grasses and herbage; (2) that profound disturbances of the equilibrium have taken place through extensive over-grazing; (3) that over-grazing is the principal cause of modern arroyo formation and that the cycle of degradation now operating is of recent origin; and (4) that historical evidence shows that both the Gila and the Colorado were clear streams near Yuma in 1824.

It is not disputed that over-grazing within the water-shed of the Colorado River has reduced the grass carpet over large areas, thus promoting erosion and denudation. This phase has been discussed by Ralph I. Meeker, Assoc. M. Am. Soc. C. E., and F. H. Olmsted, M. Am. Soc. C. E. However, it is questioned whether over-grazing is a major phenomenon affecting the physiographic balance of the West. On the subject of the origin of silt the following quotation from the comprehensive study of silt production in the Colorado River water-shed is submitted:

"The aridity of the climate and the consequent lack of vegetation is one of the main causes. Because the territory is sparsely settled, relatively few climatic records have been kept, and in many parts the precipitation is not known accurately. Roughly estimated, 40% of the total area of the basin has a precipitation of less than 10 inches a year, in 50 per cent the precipitation ranges from 10 to 17 inches, and in the remaining 10 per cent it is from 17 to 25 inches and higher in the high mountains. Fully one-half of the basin is either bare or but scantily covered with desert shrubs and grasses."

Relative to the silt production of the Green River and Upper Colorado, where the major grazing areas are located, as compared with that of the Little Colorado and San Juan Rivers, data given in the report<sup>®</sup> reveal a much greater proportion of silt in the water of the lower tributaries which drain desert areas.

60 Loc. cit., Tables 2 and 3.

<sup>&</sup>lt;sup>57</sup> "Silt in the Colorado River and Its Relation to Irrigation", by the late Samuel Fortier, M. Am. Soc. C. E., and H. F. Blaney, Assoc. M. Am. Soc. C. E., Technical Bulletin No. 67, U. S. Dept. of Agriculture, pp. 7 and 19.

 <sup>68 &</sup>quot;Gila River Flood Control", 1919, Senate Doc. No. 436, 65th Cong., 3d Session.
 69 Technical Bulletin No. 67, U. S. Dept. of Agriculture, p. 5.

Professor Chapman's reference to the diary of the explorer, James M. Pattie, in which the Gila and Colorado Rivers are described as clear streams, can scarcely be accepted as conclusive historical evidence that the muddy appearance of these streams is a modern phenomenon. Other historians have left records which emphasize conditions to the contrary. Quoting from F. S. Dellembaugh<sup>61</sup> who was a member of the Second Powell Expedition through the Colorado River Canyon, in 1872:

"In 1539, the Spanish explorer, Francisco de Ulloa, leaving from Acapulo, sailed to the head of the Gulf of California where he made this observation—'and thus sailing we always found more shallow water and the sea thick, black and very muddy'.

"In 1609, Don Juan de Onate, traveling west from San Juan on the Rio Grande via Zuni, '10 leagues beyond Moki, they crossed a stream flowing northwesterly which was called "Colorado" from the color of its water.' This has been identified as the Little Colorado.

"In 1826, Lieut. R. W. Hardy of the British Navy sailed up the Gulf of California and encountered 'a vein of red water' which later was proved to have been the Colorado.

"On Powell's first trip down the Colorado, the tributary Fremont River, in Southeastern Utah, was given the name 'Dirty Devil' from the character of its water.

"In 1869, Powell's party found the Little Colorado at its mouth 'small, muddy and saline'."

Lieut. R. S. Williamson 62 writes:

"The water [in the Colorado River, at Yuma, in 1853] was highly charged with fine red mud which gave it a decided red color and opacity. \* \* \* The amount thus annually transported to the Gulf of California by this river must be very large, and very considerable additions to and alterations of its delta must result."

Last, but not least, the statement is here presented that the Grand Canyon of the Colorado, cut to a depth of 1 mile into the plateau during past ages, has been the basic cause for the degradation of the tributaries and their water-sheds during the same period, with the great Colorado Delta a silent but potent witness to a process in which the works of Man had no part.

The discussion by Mr. Bonner of the rate of débris production of representative streams, storage depletion through siltation, and annual silt production in the United States, illustrated in Tables 3, 4, and 5, is of general interest and no doubt is widely appreciated by engineers occupied with problems of water supply, conservation, and flood control. Table 3, in particular, has filled a long-felt want relative to the silt load of streams in that it covers a wide range of drainage areas, both as to size and geographical

<sup>61 &</sup>quot;The Romance of the Colorado River", pp. 7, 78, 120, 215, and 218.

<sup>&</sup>lt;sup>42</sup> Report of Explorations in California, 1853, Senate Doc. No. 78, 33d Cong., 2d Session, p. 112.

location. The assumption of a mean weight of 85 lb per cu ft for alluvial deposits furnishes a convenient justifiable ratio for the establishment of the relation between weight and volume and for comparison of data when different methods of measurement have been adopted. The compilation of records of storage reserve depletion is gratifying in that it demonstrates for a large majority of cases a remarkably low rate of depletion.

Reference has been made to the conditions on the South Pacific slope which form rather the exception to this rule. Because of steep gradients of streams and, in many cases, unsuitable foundations, economic reservoir sites are few, and the available storage capacity, almost without exception, is deficient for flood control. Flood regulation, therefore, remains imperfect, being circumscribed by available detention storage. On many streams, the one practical reservoir site has been utilized and the channel capacity below it has been adjusted to the resulting peak flow. Although, under normal conditions of the water-shed cover, débris production may not be a disturbing factor, there remains the ever-present danger of abnormal erosion from burned areas. Under such conditions, a preconceived plan of débris storage for the protection of water storage becomes imperative.

Check Dams.—Mr. Jarvis comments on the relative merits of high débris barriers and check dams for conservation projects. Check dams were an important feature in the La Crescenta-Montrose flood discussed by Messrs. Rowe, Lippincott, and Rule.

These check dams were of a temporary type of construction. Many had been placed in the small canyons of the La Crescenta-Montrose area by the Los Angeles County Flood Control District several years prior ) the fire. Immediately after the fire of November, 1933, other agencies in the vicinity were engaged to build additional checks, both in the canyons and on the débris cones. In Pickens Canyon, checks had been placed on the cone from the State Highway to the mouth of the canyon and from there in the rock formation to upper reaches of the creek. This work was of such magnitude as to be generally known and to create in the local population the conviction that the problem of flood control had been satisfactorily solved. As an added precaution, the Forestry Service had sowed a large part of the burned-over area with a variety of mustard used in Southern California for cover crops. The criticism has been advanced that a widespread use of temporary structures in the mountain areas tends to create a false sense of security on the part of the population of the area below. This unfortunate psychological effect, and the dangers inherent in temporary types of structures have also been brought out by Mr. Debler.

In this particular case, the checks undoubtedly released a considerable quantity of débris which, with permanent structures, might have remained in the mountains. However, with a subsequent flood, their efficiency would have been negligible in any case because they would have been either completely back-filled or buried. The latter effect was observed in 1924 in Sawpit Canyon where the stream bed, raised by a series of checks, assumed its original gradient.

Check dams have been an element in the flood protection and conservation program of Southern California. Thousands have been built and although those subjected to severe tests have failed, the popular faith in and demand for this type of structure has not abated.

The conception has been that check dams "hold the water in the mountains" for future release, affecting not only conservation, but also regulation of flood flow. So firmly has this idea been entrenched in the public mind that check dams have lost their technical significance and in Southern California have become a political issue. For this reason, it is considered justifiable to devote some space to an analysis of the function of this type of structure.

As a flood-control feature check dams were proposed in Southern California after the capital floods of 1914 and 1916, the idea being to regulate the flow of the mountain streams at the source. The prototype of the check-dam system was the débris barrier of the Swiss Alps. Unfortunately, in applying the Swiss system to conditions in Southern California, the true functions of the structures were misunderstood, and the guiding principles of construction disregarded. In the Alps, the barrier systems were utilized to control abornmal débris production in regions where the formation consists of soft slates, marls, and chalks, which are easily erodible. The Alpine barriers were built of massive dry masonry, as a rule, with the two top courses of pointed rock laid in cement mortar, and were from 20 to 100 ft in height. Particular care was exercised to secure the foundation by building on bed-rock, or by providing one or more stilling-basins as a protection.

The purpose of these barriers is first to stop erosion of the stream bed and then to cause the back-fill of the barrier and thereby protect the adjacent slopes from undercutting and slides. After the slopes are stabilized, they are further consolidated by planting. The massive type of dry masonry is well demonstrated in reports of Swiss engineers on the improvement of mountain streams.<sup>63</sup>

In the application of checks to Southern California conditions, the intention was primarily to regulate the flow of water during flood peaks and to effect conservation by holding water temporarily in the back-fill of the dams. This was to be accomplished by the erection of systems of check dams of a nominal height of 6 ft. distributed throughout the length of the stream bed. In some canyons several hundred checks were erected. Débris control, or storage, has not been considered the major objective.

The original plan contemplated the construction of dry masonry arches, built carefully to bring the arch action into play. However, lack of skilled labor, unsuitable materials, and the absence of proper foundations soon caused a modification in design. Arches were abandoned, and the dry masonry degenerated into dry rock walls, built by unskilled labor. Cases are known in which, in the absence of suitable quarry rock, boulders from the bed of the creek were used. After numerous failures, the practice of wrapping the structures with triangular wire netting was adopted, so that, to-day, the strength of the rock wall rests with the strength of the wire mesh. Large

<sup>&</sup>lt;sup>63</sup> "Wildbachverbauungen und Flusskorrektionen in der Schweiz", 1914, and Proceedings, Swiss Engrs. and Archts. Assoc. 1903.

numbers of such dams have been built in Southern California. The contention has always been made that these dams can be built for from \$25 to \$50, although experience has shown that they cost more and that the cost of wire-bound rock check dams may be as high as \$500, depending on the length. It is a feature of this check system that the dams are built approximately the same height regardless of the size of the water-shed and the depth of the stream flow, and that the spacing is more or less arbitrary. The systems, as constructed deviate further from the theoretical plan in that, in many canyons, dams cannot be built in the uppermost and steep parts where the slopes may be from 40 to 60 per cent.

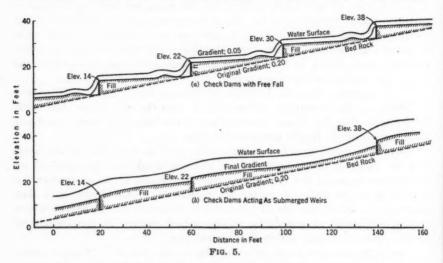
It is apparent that the function of the barrier systems in Southern California is fundamentally different from that in the Swiss Alps and, furthermore, that the rugged construction of the latter has been abandoned for a comparatively fragile and unstable type.

Flood Regulation by Check Dams.—The popular view that "check dams hold the water in the rocky formation of mountains" may be explained by the erroneous concept that the time consumed in transit of the water from the water-shed to the valley is materially increased. It should be clear that checks do not affect the rate at which water collects from the canyon slopes so that the period of retardation is determined mainly by the amount of possible channel storage within the checked area.

Conditions are conceivable in which the construction of a proper number of correctly proportioned small checks may reduce the velocities of a mountain stream to such an extent that a temporary storage in the channel will result and, hence, a material reduction of the peak flow. A first requirement is that the height of check dams is in correct proportion to the depth of overflow (see Fig. 5(a)). Next, comes the spacing of check dams which is determined theoretically by the point of intersection of the original slope (20%) with the slope of the back-fill of the check (5%). In other words, the spacing must be a function (a) of the height of the check; (b) of the original gradient of the stream; and (c) of the gradient normally assumed by the back-fill material. This proportioning holds for a depth of overflow which will produce a free fall and a destruction of the energy by fall and turbulence. However, if the depth of overflow is such as to cause the check to act as a submerged weir, the effect of the drop is largely lost. This, for example, was the case with some of the check dams in the La Crescenta-Montrose area (see Fig. 5(b)).

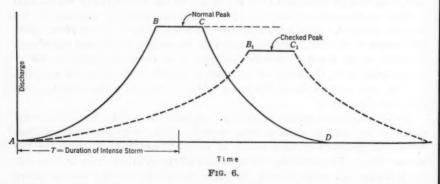
Aside from any question of design, regulation is a function of the total reduction in velocity during peak periods. This reduction results from decrease in gradient, greater width of channel, and loss of energy at the various drops. Theoretically, the reduction of the gradient from 20% to 5% would reduce the mean velocity by about one-third; the flat section above checks tends further to retard the flow, while the increased depth of water in the narrower parts of the channel below the check increases the theoretical gradient. The resulting channel storage will be in proportion to the length of the checked section and the reduction of velocity.

Apparently, the most efficient reduction in gradient compatible with economy would result from high barriers spaced correspondingly, for the reason that the narrow section of the channel would be only a small part of the total length between checks, leaving a large stretch for the adjust-



ment of velocities. With barriers of a height of 20 ft, or more, the width of channel at the check would probably be in excess of 50 ft. Under such conditions, channel storage would attain a maximum.

Assume the theoretical case of a canyon being visited by a rain of maximum intensity. In such an event, the hydrograph of an unchecked canyon would assume the line, A-B, shown in Fig. 6, with a peak discharge represented by Line B-C and the run out by Line C-D, the period of the



storm being indicated by the distance, T. If, as a result of proper checking, peak velocities have been reduced, the time represented by Curve A-B becomes longer and if the peak is delayed beyond Point C, it will also be reduced as indicated by Curve A- $B_1$ - $C_1$ . In other words, factors remaining

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equal, the shorter the time represented by Line T (that is, the duration of the storm), the greater the probability that checking would be effective. On the other hand, if the duration of the storm represented by the distance, T, and the peak flow, B-C, are extended beyond  $B_1$ , checking would have no effect on the size of the peak; the effect would be a delayed peak of shorter duration. In any case, the delay could not be longer than the difference in time of transit for the water from the upper end of the canyon to the mouth.

The effect of checking can best be explained by an example. Assume a mountain stream with hydraulic properties, as given in Table 10. While the total difference in channel storage is 100 000 cu ft, the proportion of

TABLE 10.—HYDRAULIC PROPERTIES OF AN ASSUMED MOUNTAIN STREAM

Description	Unchecked stream	Checked stream	
Length of bed, in feet	5 000	5 000	
Upper end	100	100	
Lower end	500	500	
Mean velocity, in feet per second	10	6	
Upper end	10 50	163 83	
Lower end		83	
Channel storage, in cubic feet	150 000	250 000	
Time of transit, in seconds	500	833	

this extra storage which affects the peak flow depends on the depth of stream flow prior to the period of intense rainfall and, consequently, can be only a portion of the 100 000 cu ft. Furthermore, if the time of the peak discharge exceeds 833 sec, the maximum flow at the canyon mouth remains the same in both instances.

In Southern California, the small tributary canyons, in which checks are placed, are short, ranging in length from ½ mile to ½ miles, with gradients of from 10 to 40%; hence, velocities are high and time of transit relatively short—probably less than 30 min for severe storms. Cases are recorded where two periods of intense rainfall occurred at short intervals. Under such conditions the second peak might catch up with the delayed first peak of a checked canyon, resulting in a greater flood than would happen under natural stream flow.

The difficulty in estimating the effect of check dams lies in the lack of reliable data as to the intensity and duration of storms. It is unwise, therefore, to place too much, if any, reliance on the effective flood protection by systems of checks, even if properly designed and constructed. In fact, it is the writer's opinion that, during capital floods, conditions may be such as to render regulation by check dams ineffective.

Water Conservation by Check Dams.—In an appraisal of the efficiency of check dams for purposes of water conservation, differentiation must be made between streams flowing on bed-rock and those flowing on an alluvial fill.

Mountain streams issuing from bed-rock canyons act essentially as drains, intercepting the water which percolates down the slopes in fissures, cracks,

and in the soil cover. If the creek bed is crossed by deep-seated fissures, the stream will be carrying the unabsorbed water. This function of the stream as a drain is not changed by the construction of a series of check dams, except that the débris behind the checks will hold some of the water temporarily, which then will be exposed to evaporation from the saturated mass, or will promote plant growth. Absorption into deep-seated fissures is assisted by this process only to a small extent.

A stream flowing on porous alluvium, with a water-table at effective depths, is naturally a losing stream. If checked by a system of dams, absorption will increase in proportion to the additional width of the wetted perimeter. In both cases checks should be credited with the storage in the débris which, although small, nevertheless remains an element to be considered. However, the débris storage and its water capacity increase more than the square of the height of the dam; hence, conservation favors the higher dams.

Summarizing on the relative merits of low and high check dams, it is concluded that for the consolidation of the stream bed in an erodible formation, low checks or fixed sills offer a satisfactory solution; that for débris storage, the consolidation of slopes, and, for conservation, high barriers may be found to be more efficient; and that for purposes of regulation, barriers with negligible water storage cannot be relied upon at times of critical discharge.

Unfortunately, the popular conception may attribute flood regulation to a system of checks designed for conservation, or débris control, and induce encroachment on the over-flow areas of a stream. Unless such areas are definitely zoned as dangerous for habitation, destruction of human life and property is inevitable.

Design of Check Dams.—To be effective check dams must have a height in proper relation: (a) To the depth of overflow; (b) to the gradient assumed by the stored débris; and (c) to the distance between checks. These matters would be taken into consideration were the problem one of designing a small number of high barriers; yet they are equally important with small checks.

Another feature of the design would be the correct thickness of the dam relative to the overflow wherein must be considered such forces or combined forces as extreme high water, débris, and mud flow, resulting in an extremely high specific gravity for the material passing over the dam and the impact of large rocks. Depending on the magnitude of slides, the stream may become temporarily blocked or dammed until a small lake is formed. When such slides are topped they may be released suddenly, advancing down the canyon as a mud-flow or débris wave. Such conditions were observed in the La Crescenta-Montrose flood. To withstand such forces in steep mountain canyons will require structures quite different from a dam consisting of loosely piled rock wrapped with triangular wire netting.

The conclusion is reached that in order to be permanent a 6-ft check dam must be constructed to withstand strains and forces out of proportion to its size, and, therefore, if properly built, will prove likely to be the most ζ

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The discussions of the paper necessarily centered on conditions in the arid Southwest. The writer is indebted to Mr. Matthes for his comparison of the problem in Eastern and Western streams. Attention is called to a paper by Mr. Matthes, which bears on certain phases of the physiographical balance manifested in stream dynamics.<sup>64</sup>

It was the purpose of this paper to awaken the consciousness of the Engineering Profession to the dangers accompanying the disturbance of the physiographic balance. The interest thus aroused is gratifying.

<sup>&</sup>lt;sup>64</sup> "Floods and Their Economic Importance", National Research Council, Transactions, Am. Geophysical Union, Pt. II, 1934, p. 427.

### AMERICAN SOCIETY OF CIVIL ENGINEERS

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### DISCUSSIONS

# AN APPROACH TO DETERMINATE STREAM FLOW

### Discussion

By R. L. GREGORY AND C. E. ARNOLD, ASSOC. MEMBERS, AM. Soc. C. E.

R. L. Gregory And C. E. Arnold, Assoc. Members, Am. Soc. C. E. (by letter)220.—Based on the assumption that certain statements contained, and procedure outlined, in a paper<sup>23</sup> by L. K. Sherman, M. Am. Soc. C. E., are correct, the author has presented an ingenuous method for the determination of stream flow, which utilizes some of the factors occurring in the writers' formulas.24 The method constitutes an approach to the construction of hydrographs at points on streams for which adequate flow records are not available. Engineers in general, and the writers in particular, fully appreciate the value of any thoughts, data, or methods that tend to advance the solution of this problem.

Previously, in his discussion of the writers' paper, the author had separated and combined the run-off factors pertaining strictly to the drainage area from those influenced more directly by rainfall. This combination, Equation (1), omits the three remaining run-off factors, C, A, and  $R_H$ , contained in the general run-off equation.26

There can be no doubt that Equation (1) may serve as a convenient instrument for aiding in the analyzation and presentation of drainage data. The author, through its use, has already presented valuable data for consideration by the profession. There has arisen in the minds of the writers, however, a doubt as to the wisdom of using Equation (1) in a procedure

Note.—The paper by Merrill M. Bernard, M. Am. Soc. C. E., was published in January, 1934, Proceedings. Discussion in this paper has appeared in Proceedings, as follows: March, 1934, by C. S. Jarvis, M. Am. Soc. C. E.; April, 1934, by LeRoy K. Sherman, M. Am. Soc. C. E.; May, 1934, by W. W. Horner, M. Am. Soc. C. E.; and September, 1934, by Messrs. C. H. Eiffert and Charles S. Bennett.

<sup>&</sup>lt;sup>21</sup> Chf. Insp., County of Los Angeles, Storm Drain Div., Los Angeles, Calif.

<sup>22</sup> Los Angeles, Calif. 226 Received by the Secretary July 30, 1934.

<sup>23 &</sup>quot;Streamflow from Rainfall by Unit Graph Method", Engineering News-Record, April 7, 1932, p. 501.

<sup>24</sup> Transactions, Am. Soc. C. E., Vol. 96 (1932), p. 1038.

<sup>25</sup> Loc. cit., p. 1150.

<sup>26</sup> Loc. cit., p. 1059, Equation (24).

based on hypotheses that inherently prohibit consideration of changes in the hydrograph due to differences in the magnitudes of storm intensities.

In his paper,<sup>28</sup> Mr. Sherman states, "for the same drainage area, however, there is a definite total flood period corresponding to a given rainfall, and all one-day rainfalls, regardless of intensity, will give the same length of base of the hydrograph"; that is, the same total period of run-off. As far as the writers have been able to determine, data have not been presented to substantiate the truth of this unqualified assertion. The statement could not be true, since a difference in the magnitude of intensity for a given time period would alter the quantity of water flowing and, consequently, the time of concentration, and the relative shape and length of the graph for the total period of run-off.

For like reasons, and others, inspection leads to the conclusion that Mr. Sherman's Fig. 1 and the equations immediately following convey erroneous conceptions of the manner in which water combines in a drainage area to cause run-off.<sup>23</sup> Therein exists a disregard of the fundamental principle that the velocity of flow of water in streams and channels is a function of the quantity flowing.

The author's method embodies the unit-graph procedure as exemplified in his Table 3.

It is comparatively easy to make or to deny assertions, but sometimes difficult and tedious to prove their truth or falsity. The purpose of this discussion is to test the fundamentality of the procedure that the author follows in his method and to arrive at some measure of its departure from the truth in the construction of hydrographs.

To ascertain the effect on a stream hydrograph due solely to a difference in the quantity of water running requires the complete elimination of all variables with the exception of intensity of precipitation. Due to the many and varying factors and conditions contributing to flow of a drainage area, it is almost impossible to find a single experiment wherein all variables are definitely known.

For their purpose the writers have chosen a hypothetical drainage area; and have stripped it of all pondage, channel constrictions, and other features, which tend only to confuse the issue.

Consider a triangular water-shed<sup>27</sup> with streams concentrating along lateral lines to the main channel of flow, to be divided, as in Fig. 7, into time-contours, all points on which are equi-distant in time from the outlet.

Assume any definite proportions for the water-shed (say, ratio of length, L, to bottom width is 5 to 3). Then (all computations by slide-rule) since  $L \propto A^{\frac{1}{2}}$ , or  $L = KA^{\frac{1}{2}}$ , K = 380.8, in which, A =area, in acres, and L =length, in feet.

In a formula derived by the writers,28

28 Loc. cit., p. 1094, Equation (50).

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<sup>27</sup> Transactions, Am. Soc. C. E., Vol. 96 (1932), p. 1068, Fig. 5(a).

Let  $v = K_1 Q^{\frac{1}{2}} = 0.3944 Q^{\frac{1}{2}}$  (which is the equivalent of assuming that F = 4.02, with S = 0.5, or other combinations of these factors).

It has been shown that for a triangular water-shed of which Fig. 7 is a special case, subjected to a uniform intensity, the value of P=0.5,  $Q \propto A$ , and  $v \propto t$ , the run-off coefficient being assumed as constant. Since  $v \propto t$  and  $v \propto Q^{\dagger}$ , then  $t \propto Q^{\dagger}$ , or  $Q \propto t^{\dagger}$ . To simplify computations and eliminate confusion, the run-off coefficient is herein assumed as equal to 1; that is, all rain that falls runs off.

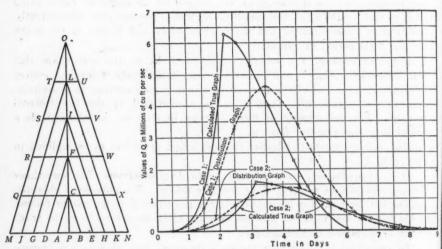


FIG. 7.—WATER-SHED. FIG. 8.—COMPARATIVE HYDROGRAPHS, CASE 1 AND CASE 2.

For a given intensity of precipitation, the water from Area ACB, Fig. 7, will be first to contribute its maximum rate of run-off. If it rains long enough, Areas DFE, GIH, JLK, and MON, Fig. 7, will reach their maximum contributions in sequence as time increases.

Case 1.—Assume a uniform intensity of  $\frac{1}{4}$  in. per hr throughout the period of concentration of the entire area, and assign definite values to the area and its subdivisions. The hydrograph for the period of concentration is formed by Table 6(a), the rate, in cubic feet per second, and the time, in days, being shown in the part of the graph to the left of the peak discharge point in Fig. 8 ("Case 1, Calculated True Graph").

Case 1(a).—If the rain ceases when the full area concentrates, much water will be left on the shed in transit to the outlet. Its measure is easily found for this case. Since (as shown previously),  $Q \propto t^*$ ,

$$Q = K_2 t^4 \dots (9)$$

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K2 being a constant. The volume of water that has passed the outlet at the

<sup>2</sup> Transactions, Am. Soc. C. E., Vol. 96 (1932), p. 1068,

time the full area concentrates, is,

$$\int K_2 t^4 = \frac{K_2 t^5}{5} \dots (10)$$

in which, t = time of concentration. Since  $Q_{\text{max}} t = (K_2 t^4) t = K_2 t^5 = \text{the volume of all rain that fell, one-fifth of the water has passed the outlet and four-fifths remains on the shed. Thus, using the data opposite the area, <math>MON$ , of Table 6(a), the quantity remaining on the shed, in millions of cubic feet, is:

$$\frac{4}{5} Q_{\text{max}} t = \frac{4}{5} \times 6250000 \times 193200 = 966000$$

TABLE 6.—Values for Points on Hydrograph from Beginning of Rain to Maximum Rate of Run-Off

pile of		Length of travel,	Flow, Q, in	Velocity, $v = P K_1 Q^{\frac{1}{4}}$ .	TIME, $t = \frac{L}{v}$ :		
Area (see Fig. 7)	Values of area, A, in acres	$L = 380.8 A^{\frac{1}{2}}$ in feet (3)	cubic feet per second	in feet per per second (5)	In seconds	In days	
		(a)	CASE 1				
ACB DFE GIH JLK MON	1 000 000 4 000 000 9 000 000 16 000 000 25 000 000	380 800 761 600 1 142 400 1 523 200 1 904 000	250 000 1 000 000 2 225 000 4 000 000 6 250 000	4.41 6.24 7.64 8.82 9.86	86 400 122 000 149 500 172 700 193 200	1 1.414 1.73 2.00 2.236	
		(b)	CASE 2				
ACB DFE GIH JLK MON	250 000 1 000 000 4 000 000 9 000 000 16 000 000 25 000 000	190 400 380 800 761 600 1 142 400 1 523 200 1 904 000	15 625 62 500 250 000 565 000 1 000 000 1 562 500	2.205 3.12 4.41 5.40 6.24 6.975	86 400 122 000 172 700 211 400 244 000 272 800	1 1.414 2 2.45 2.83 3.1623	

The distribution of the water remaining on the shed at the time of concentration of the entire area may be ascertained by the following procedure: Find the quantities that have passed the various time-contour lines during the time of the rain. From the total rain, falling on the area above a given time-contour during the period, deduct the quantity passed, the remainder being the quantity left on the area.

For example, consider the time-contour, DFE (Fig. 7). At the end of the first day of the rain, Area GIHEFD ( $A=5\,000\,000$  acres;  $Q=1\,000\,000$  cu ft per sec) was contributing its maximum quantity to the contour. At the end of 1.414 days of rain, Area JLKEFD ( $A=12\,000\,000$  acres;  $Q=3\,000\,000$  cu ft per sec) was contributing its maximum. The entire area ( $A=21\,000\,000$  acres;  $Q=5\,250\,000$  cu ft per sec) above the time-contour was contributing its maximum after 1.73 days of rain. The times of concentration, to the time-contour, of the three areas are determined from, and are the same as, those for the respective parts of the areas contributing to the main channel between FI, FL, and FO (see Fig. 7). In Table T(a), showing times and quantities to the time of concentration to this time-contour, DFE, the values of Q' correspond to the time-rendering areas, the time having been calculated from Equation (9) with substitution

of data opposite Area ACB, of Table 6(a) or, the time of concentration, in days, equals:

$$t = 0.04472 (Q')^{\frac{1}{2}}....(11)$$

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TABLE 7.—EXPLANATORY DATA

- Table - 1	(a) Case 1			(b) Case 3	
	, in Millions of Cubic Feet per Second Time,		Flow, in Million per S	Time,	
Q	Q'	in days	n Q	Q'	in days
0.44 1.25 3.00 5.25	0.04 0.25 1.00 2.25	0.633 1.000 1.414 1.73	0.21 0.44 0.69 0.96 1.25	0.01 0.04 0.09 0.16 0.25	0.4475 0.6325 0.775 0.8945 1.000

In Fig. 9 the area (under the curve formed by plotting the data of Table 7(a)) designated ABC, represents the volume of water that had passed the time-contour, DFE (Fig. 7), to the time (1.73 days) the area above it had contributed its maximum run-off. This maximum rate of flow

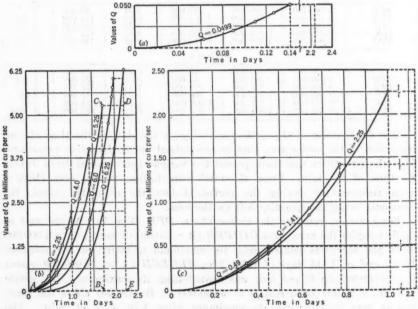


FIG. 9 .- EXPLANATORY GRAPHS, CASE 1.

continues to pass the time-contour until the end of the rain, or to the time of concentration of the entire area. Hence, the total quantity of water passing the time-contour during the period of rain (2.236 days) is equal to the summation of the area (ACB) under the curve and the rectangle, BCDE. In like manner data were calculated for other time-contours and plotted in

Fig. 9. The various contours are represented by their respective, tributary, maximum Q-values. In Table 8(a) these maximum Q-values are shown opposite the quantities, passed beyond and left on the water-shed above, the various time-contours represented.

TABLE 8.—Distribution of Water Left on a Water-Shed at the

Flow, in		LL AND RUN ONS OF CUBI		Flow, in	RAINFALL AND RUN-OFF, IN MILLIONS OF CUBIC FEET			
millions of cubic feet per second (1)	Total rainfall (2)	Quantity passed (3)	Quantity left on water-shed (4)	millions of cubic feet per second (1)	Total rainfall (2)	Quantity passed (3)	Quantity left on water-shed (4)	
	(a) C	ASE 1			(b) C.	ASE 2		
6.25 6 5.25 4 2.25 1.41 0.49 0.0499	1 207 500 1 159 000 1 016 000 774 000 435 000 273 000 94 600 9 650	241 500 377 000 446 000 431 000 302 500 209 300 81 900 9 250	966 000 782 000 570 000 343 000 132 500 63 700 12 700 400	1.5625 1.5 1.3125 1.0 0.5625 0.3525 0.1225 0.012475	426 900 410 000 359 000 273 000 153 600 96 500 33 500 3 410	85 400 134 400 158 600 152 000 106 900 73 800 29 000 3 260	341 500 275 600 200 400 121 000 46 700 22 700 4 500 150	
	(e) C	ASE 3			(d) C	ASE 4		
0.25 0.75 1.25 1.75 2.25 1.41 0.49 0.0499	540 000 518 400 453 600 345 600 194 400 121 800 42 350 4 310	4 300 18 400 32 600 47 100 61 400 58 200 29 700 3 900	535 700 500 000 421 000 298 500 133 000 63 600 12 650 410	0.015625 0.046875 0.078125 0.140625 0.203125 0.265625 0.296875 0.1225 0.012475	135 000 133 650 129 600 113 400 86 400 48 600 25 650 10 580 1 078	270 1 190 2 090 3 870 5 690 7 430 8 400 6 100 937	134 730 132 460 127 510 109 530 80 710 41 170 17 250 4 480 140	

When a given value of Q (Column (1), Table 8(a)) has reached the outlet, its corresponding quantity (Column (4) Table 8(a)) will remain on the water-shed. If, therefore, a quantity (Column (4), Table 8(a)) is subtracted from the total quantity left on the entire water-shed at its time of concentration (shown hereinbefore to be 966 000 millions of cubic feet), the remainder will represent the quantity that has subsequently passed the outlet when the corresponding Q-value arrives.

These quantities, together with their corresponding Q-values, were used to construct the outflow curve as plotted to the right of the peak discharge in Fig. 8 ("Calculated True Graph"). This curve of Fig. 8 represents a true hydrograph of the water-shed for the assumptions used, the area under the curve to the left of the peak discharge being one-fifth the total outflow of water and that to the right, four-fifths.

Case 2.—Assume a uniform intensity one-fourth that of Case 1, or  $\frac{1}{16}$  in. per hr throughout the period of concentration of the entire area for this intensity. The hydrograph of this lighter intensity on the same area for its period of concentration is also shown in Fig. 8 ("Case 2, Calculated True Graph") as plotted from Table 6(b). Note that the time of concentration of the entire area (with the light intensity) is approximately 1.4 times as long as that for the higher one.

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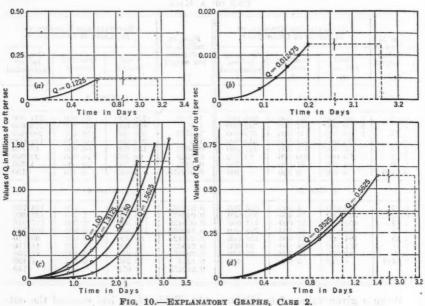
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Values of Q, in Millions of cu ft per sec

Co

Case 2(a).—If the rain ceases when the full area concentrates, the same process is used in computing the data as for Case 1(a). The difference in results is due solely to the use of a lower intensity. Table 8(b) and Fig. 10 are to be compared with Table 8(a) and Fig. 9, respectively, of Case 1(a). The hydrograph is plotted in Fig. 8 and is labeled "Case 2, Calculated True Graph".



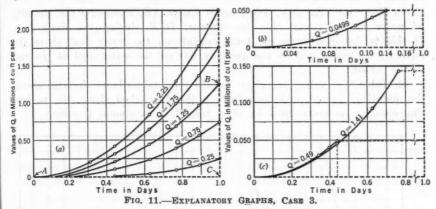
Equation (12) replaces Equation (11) of Case 1(a) since substitution of the data of Table 6(b) in Equation (9) renders:

$$t = 0.08944 \ Q^{\frac{1}{2}}.....(12)$$

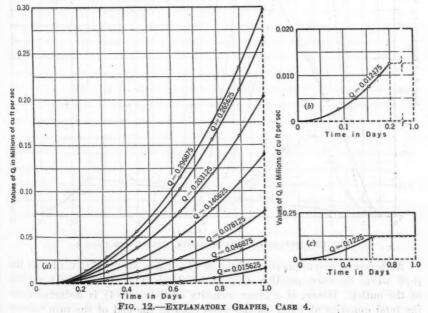
Case 3 .- One-Day Duration of Rain; All Other Assumptions Identical with Case 1.—The procedure used in the solution for this case differs sufficiently from that for Case 1 to warrant a brief explanation. Note (see Table 6(a) and Fig. 7) that the area, ACB = 1000000 acres, concentrates to a maximum rate of run-off of 250 000 cu ft per sec at the end of the first day of rain. During this period one-fifth the water that fell on this area had passed the outlet and four-fifths was left on the water-shed at the end of the day-from Equations (9) and (10). Thus, the total rainfall on Area ACB = Q  $t = 250\,000 \times 86\,400 = 21\,600$  millions of cubic feet, of which 4300 and 17300 millions had passed the outlet and remained on the water-shed, respectively; but, the total rainfall on the entire water-shed dur-

ing the 1-day period (see Table 6(a))  $= 6250000 \times 86400$ = 540 000 millions of cubic feet. Therefore, the quantity remaining on the entire water-shed at the end of the first day of rain  $= 540\,000 - 4\,320 = 535\,680$  millions of cubic feet.

At the instant the rainfall ceases, the same rate of run-off,  $250\,000$  cu ft per sec, will prevail at all points between L and P of Fig. 7. At this instant



the maximum Q-values tributary to the time-contours, ACB, DFE, GIH, and JLK, are due to contributions from Areas DACBEF, GDFEHI, JGIHKL, and MJLKNO, respectively.



The quantity of water that has passed a given time-contour during the 1-day rain may be ascertained as illustrated by the example, which follows: Consider the time-contour, *DFE* (Fig. 7). Divide the tributary area

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(5 000 000 acres) into sub-contours, and determine the respective values of Q, Q', and t as illustrated under Case 1(a). As before, the time is found from Equation (11). These values are given in Table 7(b) and are plotted in Fig. 11(a) (see Curve AB).

In Fig. 11(a) the area, ABC, under Curve AB, represents the quantity of water having passed the time-contour, DFE, during the day's rain. If this is deducted from the total rainfall on the water-shed above the contour, the result will be the quantity left on the water-shed at the end of the period.

In Table 8(c) values are given for the total rainfalls on the area above, the quantities passed, and those left on the water-shed above, the various time-contours as represented by their respective maximum Q-values.

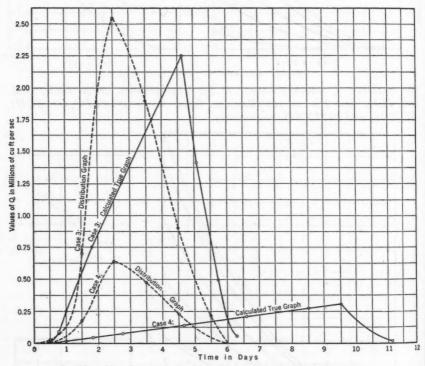


FIG. 13.—COMPARATIVE HYDROGRAPHS, CASE 3 AND CASE 4.

As before, a given quantity (Column (4), Table 8(c)) will still be on the shed when its corresponding Q-value (Column (1), Table 8(c)) arrives at the outlet. Hence, if a given quantity of Column (4) is deducted from the total quantity of water on the water-shed at the end of the rain (shown hereinbefore to be 535 700 millions of cubic feet), the result will be the quantity that has subsequently passed the outlet when the corresponding flow, Q (Column (1), Table 8(c)), arrives.

These quantities, with their corresponding Q-values, are plotted in Fig. 12 (see Case 3, "Calculated True Graph") which represents a true hydrograph for the assumptions of Case 3.

Case 4.—One-Day Duration of Rain; All Other Assumptions Identical with Case 2.—Following the procedure outlined for Case 3, Table 8(d) and Fig. 13 were constructed, due consideration being given to the effects of the lower intensity. These data are to be compared with Table 8(c) and Fig. 11 of Case 3, respectively. The hydrograph (see Case 4, "Calculated True Graph") platted in Fig. 12, is to be compared with that for Case 3, Fig. 12.

Comparisons.—The hydrograph (see "Calculated True Graph"), for Cases 3 and 4, may be compared directly through a study of Fig. 12. The two graphs differ radically both in length and in shape. They may be used to construct graphs following Mr. Sherman's procedure as outlined for Fig. 1 of the "Unit-Graph Method". Marked differences in results will be noted, for the two cases, as to total length of graphs, times to maximum rate of run-off, and shapes of graphs. If these graphs, so constructed, are compared with the two hydrographs of Fig. 8 (see "Calculated True Graphs"), a more complete idea as to the magnitude of errors resulting from disregard of fundamentals may be gained. Conversions to the unit-graph method are omitted herein in order to conserve space.

The distribution graph method, as proposed by the author, is more pertinent to this discussion; and for the purpose of making comparisons, data for constructing a distribution graph were selected from the hydrograph of Fig. 8 (see Case 1, "Calculated True Graph"). These data are shown in Table 9.

TABLE 9.—DISTRIBUTION GRAPH FOR CASE 1, Fig. 8 (Total Discharge = 1 207 500 Millions of Cubic Feet)

Day	Discharge, in millions of cubic feet	Approximate percent- age of total discharge (distribution graph)	Day	Discharge, in millions of cubic feet	Approximate percent- age of total discharge (distribution graph)
1	4 300	0.4	4	364 500	30.2
2	133 500	11.1	5	173 000	14.3
3	492 000	40.7	6	39 800	3.3

The distribution graph of Table 9 was then applied to Cases 1, 2, 3, and 4, using the data for rainfall assumed herein and following the author's method, as exemplified in his Table 3. The results are shown in Table 10 and the reproduced hydrographs are plotted in Figs. 8 and 12, as represented by the dashed curves. Little comment is necessary. Comparisons may be made directly with the calculated true hydrographs as platted on the same diagrams. In each case the variation is due to solely to the complete disregard (which is inherent in the method) of the effects of a difference in intensity.

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TABLE 10.—Application of Distribution Graphs to the Water-Sheds for Cases 1, 2, 3, and 4

Day No:	Daily				Effect- ive rain-	Com- puted flow, Q,	Daily	B	Effect-	Com- puted flow, Q.	
	fall, in inches	fall, Day:* 1 2 3 4 5 6 de	fall depth,	in millions of cubic feet per second	rain- fall, in inches	Graph data	oh fall depth, in inches	in millions of cubic feet per second			
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
*	MC46	,	(a)	CASE 1	- Contra		luit all		(c)	CASE 3	
1 2 3 4 5 6 7 18	6.000 6.000 1.417	0.024 0.666 2.442 1.812 0.858 0.198	0.024 0.666 2.442 1.812 0.858 0.198	0.006 0.157 0.577 0.428 0.202 0.047	2000	0.024 0.690 3.114 4.411 3.247 1.484 0.400 0.047	0.025 0.720 3.250 4.600 3.390 1.546 0.417 0.049	6.00	0.024 0.666 2.442 1.812 0.858 0.198	0.024 0.666 2.442 1.812 0.858 0.198	0.025 0.695 2.546 1.890 0.895 0.204
TIMA			(b)	CASE 2		,		CHERO. I	(n)	CASE 4	
1 2 3 4 5 6 7 8 9	1.500 1.500 1.500 0.244	0.006 0.167 0.611 0.453 0.214 0.050	0.006 0.167 0.611 0.453 0.214 0.050	0.006 0.167 0.611 0.453 0.214 0.050	0.001 0.027 0.099 0.074 0.035 0.008	0.006 0.173 0.784 1.231 1.304 0.815 0.338 0.085 0.008	0.006 0.180 0.816 1.284 1.360 0.850 0.352 0.089 0.008	1.500	0.006 0.167 0.611 0.453 0.214 0.050	0.006 0.167 0.610 0.453 0.214 0.050	0.006 0.174 0.636 0.472 0.225 0.052

\* Derived from Fig. 8 (see, Case 1, "Calculated True Graph.")

The variation incidental to the choice of the time-unit may be obviated by plotting the ordinates of the calculated true graphs in terms of the average flow, Q, per day. The resulting curves (plotted by the writers, but not published herein) still show marked variations from the distribution hydrographs.

Conclusion (a).—The water-shed selected, its size, shape, and manner of concentration, together with assumptions for intensity and characteristics, which rendered the foregoing variations, was chosen merely for the purpose of arriving at definite results for use in making comparisons. Another water-shed of any size and with other uniform intensities of the same ratio, but with the same shape, manner of concentration, and remaining assumptions, will render similar variations for comparison. Any given water-shed, similarly subjected to two different uniform intensities, will show results varying in the same general direction. Pondage, channel constrictions, and the existence of water in the channels immediately before the rains would tend to "iron out" the peaks and generally to make the variations less marked. On the other hand, perviousness of the area, causing a greater difference in the ratio of resulting run-offs than that of applied intensities, would increase the variations above those obtained for the completely impervious area assumed for the foregoing cases.

Any method or system, proposed for devising hydrographs, should at least embody within its scope the opportunity for designers to use their judgment in allowing for the effects on run-off of all fundamental factors and relations =

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Conclusion (b).—The procedure, outlined and followed in the foregoing computations for the calculated true graphs of Figs. 8 and 12, although utilized for special cases, for the purpose of obtaining results to be used in making comparisons with those of the author's method, may serve as a guide in the determination of hydrographs for points on streams where adequate flow records are not available. A few more comments may serve further to clarify the applicability of this procedure to any water-shed.

Usually, it will be desired in such cases to consider a rain that lasts as long as the time of concentration of the area. The time of concentration to the maximum rate of run-off and the resulting average intensity for the assumptions may be ascertained through use of the writers' formulas and methods.<sup>24</sup>

Any alterations of these times and intensities, due to pondage or other delays, will depend, of course, on the judgment of the designer, as guided by any information that he may possess. These formulas and methods will also be of service in dividing the water-shed into time-contours. The distribution of the water left on the shed at the end of the rain (being the total estimated run-off less the area under the hydrograph from the beginning to the end of the rain) may be determined through the procedure outlined under Case 1.

The ordinary water-shed, of course, is irregular in shape and manner of concentration, as are also the time-contours by which it may be divided. Instead of a simple equation (as Equation (11), for Case 1) for use in conjunction with time-rendering areas in determining the quantities that have passed a given time-contour, resort should be made to the special tables<sup>30</sup>

of the factor P, previously introduced by the writers. Since  $P=\frac{v}{V}$ , and

since the value of V can be computed for the known quantity of water and average slope, the average velocity, v, is readily obtained. The known length divided by v will render the required time.

The detail required for a given problem and any abridgment of the method may well be left to the judgment of the engineer.

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<sup>20</sup> Transactions, Am. Soc. C. E., Vol. 96 (1932), p. 1048, Tables 3 and 4.

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### DISCUSSIONS

# LOSS OF HEAD IN ACTIVATED SLUDGE AERATION CHANNELS

### Discussion

BY DARWIN WADSWORTH TOWNSEND, M. AM. SOC. C. E.

DARWIN WADSWORTH TOWNSEND, M. AM. Soc. C. E. (by letter). —Contributions to the subject-matter of his paper by Messrs. Thackwell, King, and Klegerman are gratefully acknowledged by the writer. Commenting generally upon these discussions, attention might well be directed again to the velocity-retarding effect attributable to air-bubble induction and the subsequent coalescence encountered in practice, as differentiated from the assumed hypothesis based upon laboratory observations made in connection with air bubbles rising through clear and quiescent water contained in glass cylinders.

That reduced cross-sectional area obtains due to the continuous presence of diffused air throughout the liquid medium, there can be little doubt. There also can be little doubt that the continuous and irregular swirling of an aerated mass results in cross-currents, up-and-down currents, and diametrically opposed currents, which would vary, continuously, the degree and character of the flow in a cross-section. For this obvious reason the writer elected not to attempt to state increased frictional resistance in terms based upon reduced cross-section and consequent increased velocity. In the writer's judgment a roughness or retarding factor, most prominent in character, is present in the flowing liquid mass.

The air bubbles contained in the aerated mass do not merely float along in the stream current in an undisturbed state as a log of wood might be expected to float along on the surface of a stream; they are decidedly and irregularly active in their continuous ascent, through expansion and coalescence, and the combination of both. If small logs instead of air bubbles were liberated in a continuous stream from a channel bottom, the flow-retarding effect would be quite dissimilar to that which might be expected from the same logs floating horizontally in the current.

Note.—The paper by Darwin Wadsworth Townsend, M. Am. Soc. C. E., was published in January, 1934, Proceedings. Discussion on this paper has appeared in Proceedings, as follows: March, 1934, by H. L. Thackwell, M. Am. Soc. C. E.; and May, 1934, by Messrs. Henry R. King, and M. H. Klegerman.

<sup>&</sup>lt;sup>9</sup> Cons. Engr. (Consoer, Townsend, Older & Quinlan, Inc.); Cons. Engr., Milwaukee and Met. Sewerage Comms., Milwaukee, Wis.

<sup>94</sup> Received by the Secretary September 29, 1934.

It is true that the friction loss per unit of aerated channel length may be relatively small under conditions of low velocity. These losses on the other hand may be relatively large under conditions of high velocities. Furthermore, the accumulation of many relatively small friction loss increments may, and do, represent a substantial percentage of the total friction head in the design of a sizable activated sludge plant.

The conditions that obtain in a flowing aerated stream do not lend themselves ideally to head-recording accuracy. This fact the writer attempted to make clear in his discussion relative to pulsations; the results he obtained, and those encountered in practice, are sufficiently accurate to warrant their

subsequent use with safety in problems of design.

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It is obvious why the *n*-value increases as flow velocity decreases. If the upward or vertical velocity of the air-bubble stream, for instance, were greater than that of the horizontal liquid flow velocity, a curve indicating the degree of resistance would more nearly approach the vertical than would be the case if the velocities were applied in the reverse order. In other words, the same general theory of head loss and velocity resultant which applies to two horizontally flowing streams uniting with each other at an angle, applies in a somewhat modified degree in the case of the problem under discussion. In both cases it becomes necessary to build up sufficient head to overcome the resistance encountered. The trend curve (Fig. 5), which was based somewhat upon chance projection is the best illustration of the relationship between *n*-values and velocities.

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Founded November 5, 1852

# DISCUSSIONS

# INVESTIGATION OF WEB BUCKLING IN STEEL BEAMS

### Discussion

By INGE LYSE, M. AM. SOC. C. E., AND H. J. GODFREY, ESQ.

INGE LYSE, M. AM. Soc. C. E., AND H. J. GODFREY, Esq. (by letter). The data on aluminum alloy beams presented by Messrs. Moore and Hartmann are valuable additions to the results obtained on steel beams by the writers. Unfortunately, the data on the aluminum beams give only the ultimate load with no indication of the load at which the beam would become useless due to excessive deflections. As already stated in the paper, the load at failure has no significance except that it is a measure of the toughness of a beam after it has passed its usefulness. In structural design, the load at which the deflection exceeds the maximum permitted by the usefulness of the building must be taken as the basis for estimating the factor of safety. Since all the aluminum alloy beams had depth-thickness ratios of only 25 and less, buckling of the web would not take place at stresses less than the yield-point stress of the material.

No information is given as to the stress in the web at the yielding of the beam and, consequently, Messrs. Moore and Hartmann give little support to their criticism of the writers' recommendation that the average web shear be computed on the net area  $(h\ t)$  rather than on the gross area  $(D\ t)$ . The observed stresses presented in Fig. 24(b) do not necessarily represent the stresses that cause yielding of the beam. H. M. Westergaard, M. Am. Soc. C. E., has shown that the concentration of shearing stress at the fillet between the web and the flange of the beam may become significant for beams having relatively small fillets. Fig. 21 also shows that the computed stresses at the yielding of the beam, instead of being greater (as they should be according to Messrs. Moore and Hartmann) are less than the yield-point stresses of the web material.

Note.—The paper by Inge Lyse, M. Am. Soc. C. E., and H. J. Godfrey, Esq., was published in February, 1934, Proceedings. Discussion on this paper has appeared in Proceedings, as follows: August, 1934, by R. L. Moore, Esq., and E. C. Hartmann. Jun. Am. Soc. C. E.,

<sup>8</sup> Research Associate Prof. of Eng. Materials in Chg., Fritz Eng. Laboratory, Lehigh Univ., Bethlehem, Pa.

Former Research Fellow in Civ. Eng., Lehigh Univ., Bethlehem. Pa

<sup>96</sup> Received by the Secretary June 18, 1934.

<sup>10</sup> Publication pending.

One-half the beams reported by Messrs. Moore and Hartmann failed by what has been termed web crippling. While web buckling is a failure produced by lateral instability of the web as a whole, the web crippling is a local failure produced by excessive compressive stresses. An investigation of web crippling was also conducted at Lehigh University with the co-operation of the Bethlehem Steel Company and its subsidiary the McClintic-Marshall Corporation, at the time of the tests of web buckling. The results were not included in the paper, in order to make a definite distinction between the two types of stress condition. They are presented herewith.

Web crippling is principally a local failure produced by excessive compressive stresses, and the problem of preventing its occurrence is most common in the design of structural beams supported on seat angles. The aim of the investigation was to establish the stress at which yielding due to web crippling

took place.

The program included the testing of six 22-in., 58-lb, rolled, Bethlehem beams, four of which were cut from the same section and two from another section. The information for these beams which had an  $\frac{h}{t}$  ratio of about 52, is given in Table 3. Three of the beams were designed to fail at the point of application of the load and the other three, at the supports. The nominal bearing lengths were 7 and 11 in. for the center failures, and  $3\frac{1}{2}$  and  $5\frac{1}{2}$  in. for the end failures.

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TABLE	3.—WEB	CRIPPLING	OF	BEAMS	WITH	-	=	52
					19	t		210

Beam	Web thickness, in inches, t.	Bearing length, in inches, $A+2N$	Bearing ares, in equare inches	Yield-point load, in pounds	Compressive yield-point stress, in pounds per square inch	Tensile yield-point stress of material, in pounds per square inch	Ultimate load, in pounds
CT-1 CT-2 CT-3 CT-4 CT-5	0.397	4.74 8.24 6.74 12.24 4.69 8.17	1.88 3.27 2.68 4.86 1.91 3.33	190 000 160 000 220 000* 210 000* 160 000 150 000	50 500 49 000 41 000* 43 200* 41 900 45 000	49 000 49 000 50 000 50 000 44 660 44 660	202 000 223 000 231 500* 264 400* 205 000 209 500

<sup>\*</sup> Doubtful, due to thin bearing plates.

In order to prevent failure due to end twisting, steel plates were welded to the bottom flange at each end of the beam. In each end plate, at a height even with the top flange, there was a slot which served as a guide for bars welded to the center of the top flange. This arrangement, as shown in Fig. 26, allowed the top flange to deflect vertically, but restrained it from moving laterally.

All the beams were supported by rollers and loaded at the center of the span. A roller was also used for the application of the load for Beams Nos. 1 and 2, but a spherical bearing block was used for this purpose in the testing of the remaining four beams. Steel bearing plates of the proper length were used to transfer the load from the rollers and bearing block to the beam.

Vertical deflections and strain-gauge observations were taken on all beams. Except for Beam No. 1, all beams were whitewashed before testing.

Strain lines in the web appeared at both supports at a load of 115 000 lb, and, at the center, at a load of 200 000 lb in Beam No. 1. At a load of 190 000 lb, the strains increased greatly, indicating that the actual yielding

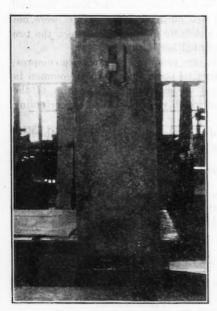


FIG. 26.—BEAM CT-5, SHOWING END PLATE FOR PREVENTION OF END TWISTING.



FIG. 27.—BEAM CT-1, SHOWING FAILURE AT THE SUPPORT DUE TO WEB CRIPPLING.

of the beam occurred. The strains observed at a point immediately above the flange indicate that the yield point of the material in the web was reached at considerably lower loads. However, this local yielding did not have any effect on the beam as a whole, which continued to take load until a maximum of 202 000 lb was reached, at which time the web crippled at the end, as shown in Fig. 27.

In computing the actual bearing length at the root of the web it was assumed that the stress was distributed through the flange on an angle of 45 degrees. The total bearing length thus equals the length of the bearing plate plus twice the thickness of the flange at the root of the web. The thickness of the flange was measured by micrometers at a point next to the fillet, as indicated in Table 3. The length of the bearing plate was  $3\frac{1}{2}$  in. at the supports where the beam was designed to fail. The compressive stress at the root of the web at the yield point of the beam was 50 500 lb per sq in., which compares very well with the average tensile yield-point stress of 49 000 lb per sq in. for the web material. The full yield-point stress of the web was thus utilized in this beam.

Beam No. 2 was designed to fail at the loading point where the length of the bearing plate was 7 in. Strain lines appeared at the supports at a load of 100 000 lb and at the loading point at 140 000 lb. Since the failure of this beam occurred at the loading point no definite indication of yielding could be obtained from the deflection curves. The strain-gauge results showed that the strains near the root of the web increased at a high rate above a load of 120 000 lb. The strains measured at the center of the web indicated a yielding at a load of 160 000 lb, which was taken as the yield-point load of the beam. The beam continued to take load until a maximum of 223 000 lb was reached, at which time the web crippled at the loading point.

At the yield point of the beam the maximum compressive stress at the root of the web was 49 000 lb per sq in., or the same as the tensile yield-point stress of the web material.

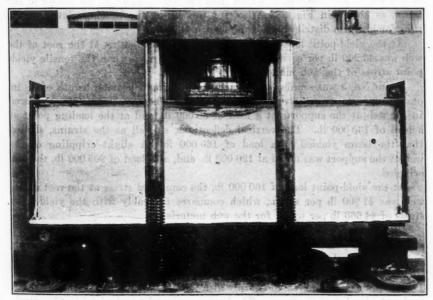


FIG. 28.—BEAM CT-4, SHOWING FAILURE AT THE CENTER DUE TO WEB CRIPPLING.

Beam No. 3 was designed to fail at the supports where the length of the bearing plates was  $5\frac{1}{2}$  in. To prevent failure at the center, stiffeners were welded to both sides of the web at this point.

The first strain lines appeared in the web near the center at a load of 60 000 lb. The strain lines continued to form and, at a load of 110 000 lb, they appeared in the web at the supports. The observed strains indicated yielding at a load of 220 000 lb, which was taken as the yield point of the beam, while the deflection curves indicated yielding at a load of 230 000 lb. At the maximum load of 231 500 lb, the web crippled at one of the supports. The bearing plate used for this beam was too thin for effective distribution

of the load from the roller to the flange of the beam and, consequently, contributed to a concentration of stress at the center of the plate, causing local failure at low average stress.

The maximum compressive stress at the root of the web was 41 000 lb per sq in. at the yield point of the beam. This is considerably less than the tensile yield-point stress of 50 000 lb per sq in. for the material in the web.

As Beam No. 4 was designed to fail at the center, stiffeners were welded to the web at the supports. The length of the bearing plate at the center of this beam was 11 in.

The first strain lines appeared in the web at the supports at a load of 90 000 lb and, at 120 000 lb, they appeared under the loading point. The observed strains indicated a yielding at a load of 210 000 lb which was taken as the yield-point load. The beam continued to take load until a maximum of 264 400 lb was reached, at which time the web crippled at the center of the beam, as shown in Fig. 28. Also, for this beam, the bearing plate was too thin for uniform distribution of the load.

At the yield-point load the maximum compressive stress at the root of the web was 43 200 lb per sq in., which is considerably less than the tensile yieldpoint stress of the web material.

Beam No. 5 was similar to Beam No. 1, having a bearing length of 31 in. at the supports where it was designed to fail. The first strain lines appeared in the web at the supports at a load of 60 000 lb, and at the loading point at a load of 130 000 lb. The vertical deflections, as well as the strains, showed that the beam yielded at a load of 160 000 lb. A slight crippling of the web at the support was noted at 190 000 lb, and, at a load of 205 000 lb, the web crippled.

At the yield-point load of 160 000 lb, the computed stress at the root of the web was 41 900 lb per sq in., which compares favorably with the yield-point stress of 44 660 lb per sq in. for the web material.

Beam No. 6 was similar to Beam No. 2, having a bearing length of 7 in. at the loading point. As this beam failed at the center, the vertical deflections indicated that there was no yielding of the beam as a whole. The strain curves, however, indicated a bending tendency in the web at a load of 80 000 lb. The rate of strains increased sharply at a load of 150 000 lb, which was taken as the yield point of the beam. The beam continued to take load until a maximum of 209 500 lb was reached and, at this load, the web crippled under the center.

At the yield-point load of the beam the maximum compressive stress at the root of the web was 45 000 lb per sq in., which is close to the yield-point stress of 44 660 lb per sq in. for the web material.

Both the flexural and shearing stresses were low in all these beams, so there was no indication of yielding due to these stresses.

Since only six beams were tested in this investigation, no general conclusions can be drawn. However, the results indicate that:

1.—The appearance of the first strain lines has no relation to the yielding of the beam as a whole, but is an indication of high local stress.

2.—The compressive stress at the root of the web at the yield point of the beam corresponds quite well with the tensile yield-point stress of the material for properly designed bearing plates.

3.—The yielding was caused by the compressive stresses at the root of the web.

4.—The following formula may be used in computing the compressive stress at the root of the web:  $f_c = \frac{R}{t(A+2N)}$ , in which, f = compressive stress; R = load on bearing plate; t = thickness of web; A = length of bearing plate; and N = thickness of flange at edge of fillet.

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# DISCUSSIONS

# ANALYSIS OF SHEET-PILE BULKHEADS

### Discussion

# By Dr. Ing. E. h. O. Franzius

Dr. Ing. E. h. O. Franzius<sup>30</sup> (by letter). <sup>30a</sup>—That present design methods are incomplete has been correctly emphasized in this paper. Time and time again even engineers of note resort to irrational methods as soon as they encounter difficulties in the design of bulkheads. One of the most favored "tricks" has been the assumption of restraint at the bottom of the sheetpiling, without an analysis of the forces producing such restraint. As long as there is no proof that such forces occur, the introduction of a restraint is equivalent to the appearance of a *Deus ex machina*, who is expected to deliver the designer from embarrassment. The fact that bulkheads designed in this manner have not failed is not due to the quality of the design, but to the fact that the active forces are smaller than assumed, owing to cohesion.

An attempt is made in the paper to determine the forces that act on a sheet-pile wall from the observed deflections and, finally, a new method of analysis is presented. This method of analysis is an ingenious, progressive step, and will materially advance designers in this field of engineering in their struggle for cognition.

Evidently, the principal objective of the tests was to observe the elastic line of a sheet-pile wall under load and to determine from this line the forces causing it. As it was not possible to measure the earth pressures directly, it was necessary to determine them through calculation in such a way as to satisfy the observed deflections. In doing so two errors did occur which are of decisive importance in the evaluation of these forces:

1.—In computing the active earth pressure in the tank by means of Coulomb's formula, the author neglects the friction on the side walls. The writer's experiments with large earth-pressure testing apparatus in the Laboratory for Foundation and Hydraulic Tests of the Institute of Technology, of

Note.—The paper by Paul Baumann, M. Am. Soc. C. E., was published in March, 1934, Proceedings. Discussion on this paper has appeared in Proceedings, as follows: In May, 1934, by Jacob Feld, M. Am. Soc. C. E.; August, 1934, by Messrs. R. L. Vaughn, M. A. Drucker, and Raymond P. Pennoyer; and October, 1934, by D. P. Krynine, M. Am. Soc. C. E.

<sup>30</sup> Prof., Inst. of Technology, Hannover, Germany.

so Received by the Secretary, October 8, 1934.

Hannover, Germany, showed this side-wall friction to be of decisive importance. In some cases the active earth pressure was reduced to one-half, due to this side-wall friction. In fact, the latter is equivalent to a lateral anchorage of the sliding wedge. Furthermore, the distance between the front and the back wall of the test tank is too small for the active sliding wedge to develop fully. Both these effects result in a reduction of the active pressure. On the other hand, the sand contains some silt which tends to increase the active pressure beyond the value obtained by Coulomb's formula. It is not possible, therefore, to determine the effective, actual pressure without direct and exact test.

In his tests with two large testing apparatus, the writer found it necessary to lubricate the side walls with soap paste after first covering them with several layers of paper. The side-wall friction was reduced thereby to about 10% of its original value so as to render its effect on the total earth pressure quite small.

A further uncertainty is inherent in the angle of internal friction of soil under water. The author conducted three tests to determine this angle, two of which gave 31° and the third, 30 degrees. As the latter test called for the greatest movement of sand particles, prior to finding their equilibrium position, the writer would consider the greatest angle (that is, 31°) as closer to the true one. However, the difference is too small to be of decisive influence, although combined with other values it may assume a certain significance.

That the angle of 31° for the material under water is much smaller than the angle for the material "in the dry" is due to silt in the sand. The writer's tests showed that the angle of friction of clean sand under water is exactly the same as in dry sand.

2.—If these uncertainties affecting the active pressure were of slight importance the actual forces due to passive resistance in front of the wall could be found with fair approximation. The earth-resistance values obtained by the writer in his tests at Hannover (and which the author uses as a basis of his derivations) are due to a wall width of 2 m (6.56 ft), which means that the resistance values found to establish equilibrium according to the author's new method of analysis would be about four times as great. The values as measured by the writer are for clean, granular sand with practically no cohesion. On the other hand, the soil tested by the author had ingredients which, conditions permitting, will produce cohesion, although with the material under water the cohesion would be almost negligible. However, as the soil used in the author's tests has constants that differ from that used by the writer, an immediate comparison is impossible. One conclusion is certain, however, the earth resistance values as determined by the author are not due entirely to the prism directly in front of the wall; they are also due to the wedges that fan out laterally beyond a line through the side walls. The writer has had the influence of these side wedges investigated through tests on anchor-plates. The top of these anchor-plater was some distance below the

<sup>31 &</sup>quot;Erdwiderstand auf Ankerplatten", von Dr. Ing. Wilhelm Buchholz, Pre-Print from the Yearbook of the Hafenbautechnische Gesellschaft, Vol. 12, 1930-31.

ground surface. The tests showed that the passive resistance was more than twice the value reported by Krey and more than three times that based on the Coulomb theory.

The same must be true of the author's tests. The influence of side friction is great. If the test wall had been twice or three times as wide as it actually was, the values of passive resistance would have been quite different because of the reduction in the influence of side friction to one-half and one-third, respectively. The relative magnitude of side friction and passive resistance can only be determined through tests with specially constructed apparatus.

It is much to the writer's regret to conclude that the passive resistance values, as established by the author's tests, do not truly represent the passive resistance value of that soil per unit width, of a wall of infinite width. This is also reflected in the permanent deformation of the sheet-piles (Fig. 6), as the outside piles show smaller deflections than the inside ones, due to the influence of the lateral fanning out of the resisting wedge.

As the deflections below the ground surface could not be measured, a considerable part of the elastic line and, in fact, the part subjected to the greatest loads, was not established. The results to date merit an extension of these tests by the installation of such apparatus in laboratories as will permit measuring the passive resistance of soil directly.

Naturally, the new method of analysis proposed in the paper is entirely independent of the magnitude of the forces as far as theory is concerned. This method of design will always give better results than the present method for one and the same system of forces; but just because this new method is valuable, the true set-up of force should be determined more accurately, and to accomplish this the continuation and extension of the author's tests, or perhaps the introduction of new tests, is necessary.

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# DISCUSSIONS

# FLEXIBLE "FIRST-STORY" CONSTRUCTION FOR EARTHQUAKE RESISTANCE

## Discussion

By H. A. WILLIAMS, ASSOC. M. AM. Soc. C. E.

H. A. WILLIAMS, ASSOC. M. AM. Soc. C. E. (by letter). The assumption is introduced in this paper that, if the first story of a building is made flexible, the remainder of the superstructure can be considered a rigid mass in so far as the dynamic analysis is concerned. The writer has made a number of shaking-table experiments in the Vibration Laboratory at Stanford University with two modifications of a dynamic model of a 17-story building (originally designed and built by Professor L. S. Jacobsen) to ascertain to what extent the author's assumption is valid.

For brevity in the discussion, the nomenclature will be given at once:

e = elastic or spring constant (the same as that used by the author); e1 is the constant for the first story; e2, that for the second story; etc.

 $\gamma = \frac{e_2}{} =$  ratio of flexibility.

 $T_n =$  fundamental period of vibration of model, in seconds, when the superstructure is not considered rigid. It is approximately equal to:

$$T_n = 2 \pi \sqrt{\frac{\sum W \Delta^2}{g \sum W \Delta}} \dots (35)$$

in which, W is the weight of one floor of the model, in pounds, and  $\Delta$  is the horizontal deflection of that floor from the position of static equilibrium when the entire model is subjected to a horizontal force equal to the pull of gravity.12

 $T_r =$  fundamental period of model, in seconds, when superstructure is considered rigid. It is equal to:

$$T_r = 2 \pi \sqrt{\frac{m}{e_1}} \dots (36)$$

in which, m is the mass of the entire superstructure.  $T_t = \text{period of the shaking-table, in seconds.}$ 

Note.—The paper by Norman B. Green, Esq., was published in February, 1934, Proceedings. Discussion on this paper has appeared in Proceedings, as follows: In May, 1934, by Messrs, Lee H. Johnson, Edward J. Bednarski, and Merit P. White and Paul L. Kartzke; and August, 1934, by Howard G. Smits, Esq.

12 Instructor in Civ. Eng., Stanford Univ., Stanford University, Calif.

12 Received by the Secretary October 15, 1934.

13 "Vibration Problems in Engineering", by S. Timoshenko, p. 63.

The first model was dynamically similar, as far as shear distortions are concerned, to a symmetrical 17-story steel frame office building of conventional design. The 8-story model was dynamically similar to the same building with the upper nine stories removed. Frictional effects in the models were not dynamically similar to those in the actual buildings. The weight per floor for Floors 2 to 13, inclusive, was 2 650 500 lb. The next three floors averaged approximately 2 500 000 lb, and the roof, 2 120 000 lb. The elastic constant,  $e_2$ , was 57 000 000 lb per in.; the constant,  $e_{10}$ , was 27 000 000 lb per in. The intermediate constants varied approximately as a straight line between these two values. The approximate ratio of height to width was 3 to 2 for the 17-story building and 2 to 3 for the 8-story building.

The shaking-table on which the model was placed, weighed more than  $3\frac{1}{2}$  tons. Hence, the motion of the model did not affect the motion of the table, which was anchored at one end by a set of springs, in such a manner that it would be set in motion by dropping a pendulum against a bumper spring on the other end. After the impact, the table had a damped

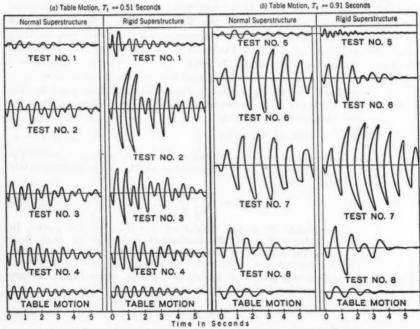


FIG. 13 .- TESTS RESULTS FOR A MODEL OF A 17-STORY BUILDING.

harmonic motion, as shown by the lower curve in Fig. 13. The period of of motion was changed for some of the tests by changing the anchor springs. The amplitude was varied by changing the height of the pendulum drop.

The apparatus was arranged so that one record giving the relative motion of the second floor of the model with respect to the table and another giving

the motion of the table with respect to the laboratory floor, were obtained simultaneously. In terms of an actual building, these records correspond to the relative motion of the second floor with respect to the ground and the absolute motion of the ground, respectively. In the test records, the table amplitude should be divided by 2 when compared quantitatively to the model amplitude.

For Test No. 1, the value of  $e_1$  for the model corresponded to an elastic constant of 60 800 000 lb per in. in the actual building. Hence, the flexibility ratio was  $\gamma = \frac{e_2}{e_1} = 0.95$  (see Table 3(a)). This ratio of flexibility would

correspond to that found in some conventional buildings of this height.

TABLE 3.—COMPUTED PERIODS OF VIBRATION OF BUILDING MODELS

17-Story Building (See Fig. 13)						8-STO	ORY BUIL	DING		
11		I	Periods of	Vibration	1		1	Periods of	Vibration	1
m4	Ratio	Normal S	tructure	Rigid S	tructure	Test	Normal Structure		Rigid Structure	
Test No.	of flex- ibility, γ	$T_n$ , in seconds	Ratio, $\frac{T_n}{T_t}$	$T_{7}$ , in seconds	Ratio, $\frac{T_T}{T_t}$	No.	Tn, in seconds	Ratio, $\frac{T_n}{T_t}$	T <sub>7</sub> , in seconds	Ratio,
		(a) F	ERIOD OF	TABLE	MOTION,	Tt, EQUAL	s 0.51 SE	CONDS		
1 2 3 4	6.10 9.60	0.75 0.94 1.07 1.82	1.47 1.84 2.10 3.57	0.30 0.67 0.85 1.65	0.59 1.31 1.67 3.23	9 10 11 12	0.56	0.63 1.10 1.18 2.16	0.18 0.43 0.55 1.00	0.35 0.84 1.08 1.96
		(b) P	ERIOD OF	TABLE I	MOTION,	Ti, EQUAL	s 0.91 SE	CONDS		
5 6 7 8	6.10 9.60	0.75 0.94 1.07 1.82	0.82 1.03 1.18 2.00	0.30 0.67 0.85 1.65	0.33 0.74 0.93 1.81	13 14 15 16	0.56	0.35 0.62 0.66 1.21	0.18 0.43 0.55 1.00	0.20 0.47 0.60 1.10

The computed fundamental period of the model for this value of  $\gamma$  was  $T_n=0.75$  sec. The computed period of the second mode of vibration was approximately 0.25 sec. The table was then given the motion indicated by the record at the bottom of Fig. 13, and the corresponding motion of the second floor of the model was recorded with the superstructure in the normal condition of flexibility. The superstructure of the model was then braced so that it acted as a rigid mass, and the same test was repeated. The motion of the second floor for this condition is shown by the right-hand record for Test No. 1.

The first story was then made more flexible and the same procedure was followed for Test No. 2, etc. Since the table motion was the same for all tests in Fig. 13(a), it is shown only once, at the bottom.

Repetition of the same tests for the 17-story model, using a different table motion, gave the results shown in Fig. 13(b). The upper nine stories were then removed and the same procedure was followed for the 8-story model. It should be noted that an 8-story building with such large elastic constants would be quite stiff for the height involved.

The test records in Fig. 13 indicate that the second-floor motions with the two types of superstructure are not alike for this particular 17-story building when y is less than approximately 40; and, even then, they are not exactly alike. The second mode of vibration whan y was 38.8 was approximately 0.36 sec. It is quite probable that, if the table motion happened to have the same period as the second mode of vibration of the model, the favorable comparisons obtained in Tests Nos. 4 and 8, Fig. 13, would not hold.

The test records for the 8-story model are not shown, but they also give little evidence in favor of assuming a rigid superstructure in the 8-story building when y is much less than 40.

Tests Nos. 1 to 4 might lead one to conclude that the assumption of a rigid superstructure is on the side of safety, because all the curves on the righthand side of Fig. 13(a) have larger amplitudes than those on the left-hand side. Tests Nos. 6, 10, and 15 indicated that such a conclusion is erroneous.

In general, if the ratio,  $\frac{T_n}{T_n}$ , is approximately 1.00 (exact resonance for the

fundamental mode of vibration) and, at the same time, is closer to unity than

 $\frac{T_r}{T_r}$  , the amplitude of the second-floor motion for the normal superstructure will be larger than when the superstructure is assumed to be rigid.

The experiments have covered a comparatively narrow range. Definite conclusions applying to all types of structures cannot be drawn from these few tests, or from any theoretical step-by-step method of analysis. In general, it would appear that if the elastic constants and floor weights are of the order of those given herein, there is little reason to believe that the author's method of analysis should apply to buildings higher than eight or ten stories unless the flexibility ratio, y, is at least 40. This ratio can probably be somewhat less for buildings of fewer stories if the superstructure is fairly rigid. It probably should be increased if the building exceeds fifteen stories.

The writer understands that Mr. Green has in mind flexibility ratios as large as 50 or 60. The period of 3.58 sec for the building which he used in his illustration would indicate as much. The practicability of using a flexibility ratio of even 40, of course, is open to debate. Observation of the model on the shaking-table makes one dubious of the success of such a building. A small movement of the ground can set up a rather large relative motion of the structure even though the system is considerably removed from the resonance condition. Hence, certain practical difficulties must be overcome to prevent damage to the flexible story from every slight earth shock.

Some engineers believe it is practical to construct the first-story walls and ceiling so that the motion of the superstructure will result in no damage to the flexible story. If such a building has a flexibility ratio of 40, or more, its behavior in wind storms would have to be determined. It has also been suggested that hollow tile walls, for instance, could be installed in the flexible story to prevent damage from small ground motions and also to stiffen the building against gusts of wind. In a severe quake, these walls would soon shatter and allow the flexible story to come into full play. Until the tile walls are badly shattered, it is quite possible that vibrations will be set up in the superstructure and, also, that the elastic constant for the flexible story will be non-linear. These factors should be borne in mind when interpreting any mathematical analysis of such a building.

· If it is granted that large flexibility ratios are practicable, Mr. Green's method of analysis, when used by one thoroughly familiar with the dynamic principles involved, should give some indication of the action of the building in an earthquake. Obviously, any quantitative results of such an analysis should be accepted with strong reservations. Even though the designer is skilful in simulating probable earth motions, there are several important factors which he would usually neglect because of lack of time or lack of reliable information.

For example, if a building is tall and narrow, direct stress in the columns and load-bearing walls will result in a certain amount of flexibility in the superstructure. This factor can be included when computing the elastic constants. If it is neglected, the flexibility ratio will be too high. Moreover, the rotation of the ground at the foundation line affects the motion of any building, the effect being dependent on the width and height of the building and on the nature of the ground below the foundation line. Another factor is damping friction which decreases the amplitude of motion. known at present about the magnitude of these two factors as far as buildings are concerned.

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# DISCUSSIONS

# A GENERALIZED DEFLECTION THEORY FOR SUSPENSION BRIDGES

# Discussion

By Messrs. Fredrick Vogt, Leon S. Moisseiff, and A. Mitchell and G. T. Parkin.

FREDRIK VOGT, <sup>41</sup> Assoc. M. Am. Soc. C. E. (by letter). <sup>41</sup> —A reference to the studies <sup>42</sup> of the late Hans H. Rode, M. Am. Soc. C. E., is pertinent to this paper.

Following Equation (9), the author states that "in the Deflection Theory, influence lines (in the ordinary sense) cannot be used". Professor Rode proved that such lines can be used for computation of the additional cable stress due to live load and the other effects of live loads, such as bending moments, etc. No doubt, the use of influence lines is limited to the case of proportionality between load and effect, and no exact proportionality exists for suspension bridges. However, on long suspension bridges, the dead load is large as compared with the live loads, and within the range from zero to full live load the proportionality is rather close, whereby the use of influence lines is made possible. Strictly speaking, one influence line should be computed for each particular value of the horizontal cable stress, H, between maximum and minimum, but Professor Rode found that sufficient accuracy was obtained by the use of two influence lines, one for a maximum, and one for a minimum, value of H (Tension H depending on temperature and load), between which a linear interpolation can be applied.

The importance of using influence lines, of course, is that the load lengths for maximum positive and negative moments, etc., can be determined directly instead of by trial as used by the author. Furthermore, it should be mentioned, that the method developed by Professor Rode can be applied for

Note.—The paper by D. B. Steinman, M. Am. Soc. C. E., was published in March, 1934, Proceedings. Discussion on this paper has appeared in Proceedings as follows: May, 1934, by E. Pavlo, Esq., August, 1934, by Messrs. Jonathan Jones, A. Müllenhoff, H. Cecil Booth, Jacob Feld, and Glenn B. Woodruff, Howard C. Wood, and Ralph A. Tador; and September, 1934, by Messrs. L. J. Mensch, A. A. Eremin, Hans H. Bleich, F. H. Frankland, Gustav Lindenthal, Julian W. Shields, A. W. Fischer, and J. M. Frankland.

<sup>41</sup> Prof. of Mechanics, Norwegian Univ. of Technology, Trondhjem, Norway.

sic Received by the Secretary August 15, 1934.

<sup>42 &</sup>quot;New Deflection Theory", by the late Hans H. Rode, M. Am. Soc. C. E., Transactions, Det Kgl. Norske Videnskabers Selskab (1930), No. 3. (In English.)

systems of any shape, statically indeterminate in any degree, and the stiffness may vary arbitrarily from panel to panel. Professor Rode takes into account the effect of introducing the deflection theory for the elastic theory by means of a "replacement system", which is identical with the original, except for the addition of certain elastic restraints, some or all of which may be statically indeterminate. This replacement system can be analyzed by the ordinary methods; that is, by the elastic theory. Since the replacement system is statically indeterminate to a high degree and the analysis, consequently, is rather complicated, Professor Rode also developed methods for numerical computations.

LEON S. Moisseiff, <sup>43</sup> M. Am. Soc. C. E. (by letter). <sup>43a</sup>—The Deflection Theory has been known to American bridge engineers for some time and has formed the basis of the design of almost all important suspension bridges in this country for the last twenty-five years. It will be of interest to relate herein some of its early history in the United States.

In the summer of 1901, due to a combination of causes, a number of suspension rods in the main span of the Brooklyn Bridge failed. At that time this was the only crossing over the East River and carried most of the passenger traffic from Brooklyn, N. Y., to New York City. The Williamsburg Bridge was then in the process of construction. The uninterrupted travel over the Brooklyn Bridge was then of vital importance to the inhabitants of New York. Great public interest was aroused by the incident and an engineering investigation and report was made at the direction of the City's Corporation Counsel by the late Edwin Duryea, Jr., and Joseph Mayer, Members, Am. Soc. C E." During the controversy on the behavior and safety of the Brooklyn Bridge which followed the publication of the engineering report, the writer worked on an analysis of the stresses and deformations of that bridge. He found that while there were no official measurements of the deflection of the bridge under load, such deflections as could be observed daily were of much less magnitude than would result from computations based on the Elastic Theory. Further consideration showed that, neglecting altogether the effect of the stiffening trusses on the deflection of the bridge and going back to the simple computations of the equilibrium polygons under dead load and under dead and live load, much closer agreement with the actual behavior of the bridge would result. It became apparent that the tacit neglect by the elastic theory of the effect of the dead load on the deformation of the bridge under live load was a serious error for large bridges. This is explained by the fact that the Rankine-Ritter theory was based on a rigid stiffening truss and thus logically introduced the error. It was later taken over without further scrutiny by the "fathers" of the elastic theory. Due to this, the latter theory is grossly in error for suspension bridges.

While working on the development of a more correct analysis, the writer directed his attention to the short treatment given by Melan to what he called

<sup>48</sup> Cons. Engr., New York, N. Y.

<sup>486</sup> Received by the Secretary September 24, 1934.

<sup>&</sup>quot; Engineering News, October 10, 1901.

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"The More Exact Theory." 45 Strangely, Melan did not put much emphasis on the practical results of the theory. The writer found that Melan's analysis of a one-span suspension bridge, taking into account the effect of the dead load on the deformation of the bridge under live load, gave solutions which closely approached actual conditions.

The Manhattan Bridge, as built, has a center span and two symmetrical side spans. To make a practical application of the theory to the design, it became the task of the writer to develop it for a three-span bridge and to establish the equations for the various loadings and temperature variations causing greatest stress. Bearing in mind the importance of the bridge which was designed for a congested live load of 16 000 lb per lin ft, the analysis was made with much hesitation and caution, and various methods were devised to furnish verifications of the computed results. Realizing that there can be no theory which, applied to a practical structure, will be absolutely exact, the writer subsequently denoted the developed theory by the name of "The Deflection Theory," having in mind that it is based on the deflections of the cable and of the truss. Thus, the Manhattan Bridge was designed in 1904 by the deflection theory, and may be considered the first modern suspension bridge.

Previous to that date, the writer in a discussion of the paper by the late Joseph Mayer, M. Am. Soc. C. E., entitled "The Stiffening System of Long-Span Suspension Bridges for Railway Trains," presented an application of the deflection theory to determine the temperature stresses in a three-hinged stiffening truss.<sup>46</sup>

In the beginning of 1909, when the Manhattan Bridge was approaching completion, the Commissioner of Bridges appointed Ralph Modjeski, M. Am. Soc. C. E., to report on the design and construction of the bridge. Mr. Modjeski engaged F. E. Turneaure, Hon. M. Am. Soc. C. E., for the analytical work. The writer submitted to the latter the fully developed theory and formulas used in the design of the main structure.

In the "Final Report of the Board of Engineers on the Bridge over the Delaware River" in 1927 (see Appendix D), the writer presented the deflection theory as applied to that bridge.

As developed and published the deflection theory was adapted for single-span, and three-span, suspension bridges with stiffening trusses discontinuous over their supports, and all long-span suspension bridges built during the last twenty-five years have been so constructed. The engineers who designed the several bridges with continuous trusses, mentioned by the author, evidently did not think it worth while to utilize the deflection theory.

Attention is called to the fact that Professor Turneaure, whose work is cited in the paper, states: "For this case [suspended side spans] the constants

<sup>&</sup>lt;sup>45</sup> "Eiserne Bogenbrücken und Hängebrücken, von J. Melan, 1888, Wilh. Engelmann, Leipzig, Germany.

<sup>46</sup> Transactions, Am. Soc. C. E., Vol. XLVIII (1902), pp. 422 et seq.

<sup>&</sup>quot;In Mr. Modjeski's report, the theory is given in Appendix B. In the Ninth Edition, 1911, of "Modern Framed Structures," by J. B. Johnson, C. B. Bryan, and F. E. Turneaure, it can be found in the Chapter on "Suspension Bridges" under "Exact Methods of Calculation."

<sup>&</sup>lt;sup>43</sup> "Modern Framed Structures," by J. B. Johnson, C. W. Bryan, and F. E. Turneaure, Ninth Edition, Pt. 2, John Wiley & Sons, 1911.

of integration are determined by equating the moments at the towers for main span with those for side spans, and the deflections at the towers equal to zero." This is the same method used in the paper.

The author shows that some saving in materials and cost, or increased stiffness, could be realized by making the trusses continuous over the tower supports. He, therefore, has extended the formulas of the deflection theory to include continuous stiffening trusses and multiple tied spans. The work principle which is utilized in the derivation of the equations of the deflection theory lends itself well to expansion over these types. The author has succeeded in preparing a presentation of the theory which elegantly embraces the common types of suspension bridge as well as the one with continuous trusses and multiple tied spans.

In generalizing a theory which in practice has been found workable and sufficiently accurate for the required purposes, it is important to scrutinize the original assumptions on which the theory has been based. Usually, some of the assumptions are apparent and have been explicitly stated and some are implied and must be brought out by a trenchant analysis. It is in the character of science to guard its steps. The verity of deduced applications which are extended beyond common practice must be checked by quantitative studies and by physical observations. The application of the deflection theory to continuous stiffening trusses may serve to illustrate the limitations of general theory.

The deflection theory assumes that the effect of the elongation of the suspenders on the total work of the structure is negligible and that its effect on the value of the cable pull is insignificant. This assumption has been justified by computations in several instances as well as by observations on models. The effect of suspender elongation cannot, however, be neglected locally. Near the towers, where the suspenders are longest, the effect of their lengthening under live load on the stiffening truss cannot always be neglected and in long-span bridges it may seriously affect the stresses in the panels nearer the towers. Careful and extensive studies of the effect of suspender elongation on long spans have shown that the moments and shears in the trusses will increase considerably toward the tower ends and, in some panels, will require an increase of as much as 25% in sectional area of the chord members and diagonals. In shorter spans, this effect, of course, will be less, but it will not decrease proportionally. This has a pertinent bearing on the design of continuous trusses.

In the case of trusses hinged at the towers, the chord sections in the panels nearer the ends commonly over-run and the excess of section is in most instances sufficient to take care of the hanger effect. The writer has followed the practice of designing the rockers and diagonals near the ends for an excess stress of one-third to one-half. In the case of continuous trusses the heaviest chord stresses are at the towers, and an excess of section, due to over-run, will scarcely be available. The effect of suspender elongation, because of the stiffness of the truss due to continuity and heavy chord sections, will here be much more conspicuous and will require still larger sections.

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Much of the theoretical saving may be nullified by it. It will be found desirable to study the effect of suspender elongation and tower shortening before reaching conclusions concerning continuous stiffening trusses.

In considering the behavior of continuous trusses, it should not be forgotten that the trusses are suspended from the cables for their dead load and that they must follow the deflections of the cable. The cable curve does not reverse its direction near the towers; the continuous truss, on the contrary, tends to do so. Such behavior must result in straining the truss unduly.

Another instance in which the assumptions of the deflection theory for the case of hinged trusses are sufficiently close is the use of a constant equivalent moment of inertia for each individual span. For discontinuous trusses, simple methods, based on various loadings, are used to complete the equivalent moment of inertia. These methods give close results. For continuous trusses the accurate determination of an equivalent moment of inertia is much more difficult and involved.

The writer does not wish to imply that practical problems will not be encountered in which continuity of the stiffening truss will be desirable. Small and light spans which commonly have an over-run of materials because of practical considerations may be given increased stiffness by continuity, and special conditions may make it advisable to resort to continuity in other instances.

To avoid misunderstandings, the writer calls attention to the fact that in the original publication of the deflection theory the values of the constants, C, represent lines or distances, while in the paper they represent moments, distance times H. The writer finds that the original notation is more helpful for the physical interpretation of the various terms.

For purposes of comparison the moment curves as computed by the elastic and the deflection theories shown in Fig. 3 are instructive. They prove again how much in error the elastic theory is for suspension bridges. It is timely to point out that the elastic theory may well be abandoned for suspension bridges and that attempts to tie it to the deflection theory, or any other advanced analysis, are of an atavistic nature.

In conclusion, the writer wishes to express his appreciation of the fine work done by Mr. Steinman in extending the deflection theory for continuous stiffening trusses and multiple tied spans.

A. MITCHELL<sup>40</sup> AND G. T. PARKIN,<sup>50</sup> JUNIORS, AM. Soc. C. E. (by letter).<sup>50a</sup>—A major contribution to the mathematical treatment of suspension bridges is contained in this paper. New developments in construction, together with the practical form of the author's method of designing, should bring about an increasing use of short-span highway suspension bridges of the continuous type.

Since "stresses producible by combinations of loadings cannot be found by adding algebraicly the respective stresses producible by the component

50a Received by the Secretary September 24, 1934.

<sup>40</sup> Senior Draftsman, State Highway and Public Works Comm., Raleigh, N. C.

<sup>50</sup> Designer, State Highway Comm., Bridge Dept., Raleigh, N. C.

loadings" (see following Equation (9)), it is desirable to have general formulas for the load functions, A, B, and G. Equations of the suggested form are readily reducible to the special cases treated by the author by noting that  $e^{-at}$  (1+d)=1-d and  $e^{at}$  (1-d)=1+d. Thus, for G:

in which, in addition to the notation of the paper, the subscripts, z, m, or k, are added to P and G to indicate the portion of the span to which they apply (see Fig. 1).

 $G_{2k} = P_k \dots \dots$ 

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# DISCUSSIONS

# SAND MIXTURES AND SAND MOVEMENT IN FLUVIAL MODELS

### Discussion

By Messrs. V. V. Tchikoff, Morrough P. O'Brien and BRUCE D. RINDLAUB AND HERBERT D. VOGEL.

V. V. Tchikoff, S. M. Am. Soc. C. E. (by letter) Soc.—A good example of laboratory investigation is offered in this excellent paper. There are serious doubts, however, as to the theory of tractive forces, or "drag" theory, itself, as well as the quantitative transferability of experimental results. The "drag" force is simply a component, parallel to the slope, of the weight of a vertical column of water of height, d, in contact with a unit area of bed of a channel with uniform flow as expressed by Equation (3). This formula is considered by the "drag" theory as a constant relation between the slope and the depth for the same bed-load material. This theory is not generally recognized. "The imperfection in this concept is evident, and it is clear that the phenomena as conceived by du Boys was a scheme somewhat lacking in the real course of things", states Professor Francesco Marzolo.36 Professor Reynold considers the force exerted by the current on sand as the function of the velocities. Professor A. H. Gibson states that the erosive power of water varies as the square of its velocity.37 This "drag" theory has not even been mentioned in many important books. The theory has the following limitations:

1.—It presupposes infinite width of channel and, according to Schoklitsch,39 an additional coefficient is required for channels in which the ratio of width to depth is less than thirty. The "drag" theory does not take into consideration the type and nature of the cross-section of the channel.

Note.—The paper by Hans Kramer, Assoc. M. Am. Soc. C. E., was published in April, 1934, Proceedings. Discussion on this paper has appeared in Proceedings, as follows: August, 1934, by Messrs. John Leighly, Paul W. Thompson, and Gerard H. Matthes; and September, 1934, by Messr. R. H. Keays, and F. T. Mavis.

<sup>85</sup> Cons. Engr., New York, N. Y.

<sup>356</sup> Received by the Secretary August 11, 1934.

<sup>\* &</sup>quot;Hydraulic Laboratory Practice", p. 755.

"Hydraulics and Its Application', Fourth Edition, p. 340.

<sup>38 &</sup>quot;Hydraulisches Rechnen", von Weyrauch und Strobel (1930), p. 79.

2.—Schaffernak<sup>30</sup> considers the du Boys law only applicable for certain sizes of grain, namely, for homogeneous materials with a grain size up to about 10 mm.

3.—According to the author the slopes must be "usual moderate slopes", as he stated in establishing his law of constant critical tractive forces.

4.—The type of the flow does not affect the "drag" theory, and it is considered applicable for laminar, turbulent, shooting, or streaming flows.

These four limitations cover practically every phase of hydraulic phenomena of flow and are so serious, in fact, that they annul the entire theory. There are direct contradictions between the requirements for hydraulic similitude of channels and those fulfilling the "drag" theory. As the writer had occasion to state in another connection, the first requirement for similitude of turbulent flow is the same kinetic factor. This is nothing but the fulfillment of Froude's law. The kinetic factor, or twice the ratio of kinetic energy to the hydraulic radius, gives only the physical and quantitative state of turbidity. Expressing the velocity through the kinetic factor:

$$V = \sqrt{gK_r R}....(15)$$

Comparing with Chezy's equation:

$$SC^2 = gK_r.....(16)$$

in which, C= Chezy's coefficient and  $K_r=rac{V^2}{g\,R}=$  the kinetic factor. The

right-hand part of Equation (16) is constant for the same hydraulically similar channels.

Equation (16) gives an important relation between the slope and elements of the cross-section. The same relation is expressed in Equation (3):

$$Sd = a constant....(17)$$

To meet the requirements for hydraulic similitude and the "drag" theory, both Equations (16) and (17) must hold, or:

$$C = \text{constant} \times d.....(18)$$

This is the new and non-existent expression for Chezy's coefficient, C. The search for the relation between the slope and other elements in some stable alluvial channels which are hydraulically similar, led Dr. H. E. Hurst to the following equation for the Lower Chenab Irrigation Project<sup>4</sup>:

$$S = 116 \times 10^{-6} \left( 1 + \frac{2.12}{R} \right) \dots (19)$$

<sup>39 &</sup>quot;Hydraulic Laboratory Practice", p. 428.

<sup>40</sup> Proceedings, Am. Soc. C. E., April, 1934, p. 557, et seq.

<sup>41</sup> Minutes of Proceedings, Inst. C. E., Vol. 229, Session 1929-30, Pt. I, p. 328.

If Equation (19), with  $K_r = 3.98\%$  (its value for the Lower Chenab Irrigation Project, see Table 5) is substituted in Equation (16):

$$C = \frac{105.4}{\sqrt{1 + \frac{2.12}{R}}} \dots (20)$$

TABLE 5.—General Hydraulic Factors; British Indian Irrigation Projects

Name of irrigation	Numbers of obser-	Mean kinetic	Coefficient of hydraulic	Hydraulic number,	Difference from mean		E FORCE, MS PER METER
(1)	vations (2)	(percent- ages) (3)	tude, Y	H (5)	(percent- ages) (6)	Maxi- mum (7)	Mini- mum (8)
Upper Bari Doab Lower Chenab Godaveri West Delta	22 35 15	4.15 3.98 2.04	7.20 8.86 5.55	35.3 44.4 38.8	-12.8 + 9.6 - 4.2	381 537 264	58 112 88
Mean weighted				40.5	0.0		

This new type of equation for the Chezy coefficient is most correct compared with all existing formulas, such as, those of Kutter, Bazin, Manning, etc. All of the latter are entirely different from Equation (18) expressing the "drag" theory. In other words, the channel fulfilling the "drag" law will not be hydraulically similar. (A formula of the same type as Equation (20) has been suggested by the late W. M. Penniman, M. Am. Soc. C. E. Equation (20) has numerical coefficients corresponding to the coefficient of roughness, n = 0.0225.)

The idea of the kinetic factor facilitates the judgment of the state of turbulency of flow. Table 6 gives the kinetic factor for the lower limit of

TABLE 6.—General Hydraulic Factors; Sand, Series II, FROM AUTHOR'S DATA

Slope	Reading number	Tractive force, in grams per square meter	Kinetic factor (percent- ages)	Coefficient of hydraulic similitude	Hydraulic number	Ratio of width to depth
1:400	4 40	38.1 41.0 49.5	80 81 77 43	1 263	1 413	49
1:600	4a 5 5 5a	49.5 40.5 41.7 44.2	43 42 40	501	759	32
1:800	4 4a 5	33.7 35.8 37.9	42 40 36 39 40	405	675	28
1:1 000	4 4a 5	36 37.2 39.6	40 34 34 34	264	455	22

tractive force and the adjacent readings (Column (4)) for Series II of the author's data. The kinetic factor varies from 34% for a slope of 1:1000 to 80% for a slope of 1:400, being more constant for smaller slopes.

<sup>42</sup> Engineering News-Record, May 10, 1934, p. 608.

Mr. Gerald Lacey gives the approximate equation for the relation between his silting factor and the diameter of the predominant type of sand, which expressed through the kinetic factor, is:

$$D = 8.6 K_r^2 \dots (21)$$

in which, D, is the diameter of the sand grains, in inches. Sand of Series II had the maximum diameter of 1.77 mm = 0.07 in. and a median diameter of 0.51 mm = 0.02 in. Substitution of these diameters into Equation (21) gives the corresponding value of the kinetic factors as 9.0 and 4.8%, respectively. Comparing this value of the kinetic factor with that of the flume in the paper, it is seen that the latter is several times greater. In other words, maintaining hydraulic similitude, the bed-load material in the prototype corresponding to the "geschiebe" in the flume, must be considerably coarser. Its size of grain, calculated according to the kinetic factor in the flume, will be, for  $K_r = 0.80$ , -D = 5.5 in., and for  $K_r = 0.34$ , -D = 1 in.

TABLE 7.—General Hydraulic Factors; Alluvial Canals and Mississippi River

Reference No.	Name	Description of channel	Discharge per second, in feet	Hydraulic radius, in feet	Mean velocity per second, in feet	Hydraulic grade; 5 x 10-4	Kinetic factor (percentage)	Coefficient of by- draulic similitude	Hydraulic number	Tractive force, in grams per square meter
123a	Bear River	Silt	109.56	1.86	2.36	2.7	9.30	17.0	56	160
146a 168a 169a	Hyde Park Louden Mesa lateral	Sand	23.55 62.00 40.32	1.40 1.52 1.66	1.08 1.66 1.47	1.5 3.8 2.6	2.59 5.63 4.04	. 8.6 17.7 8.8	53 75 44	101 173 116
204 170a	Fullerton Rio Grande lateral	Loose sand bed Gravel	15.72 146.60	1.03	1.14 3.86	4.93	3.92	14.4 51.2	73 90	980
210	Parley's Ditch lateral Rocky Ford	Sand bed Loose sand bed	4.44 41.20	0.66 1.52	1.20 1.68	11.7 5.8	6.78 5.74	15.5 11.7	60 49	264 299
214a	Rio Grande lateral	Gravel	380	1.87	4.66	36.6	36.1	58.2	- 97	2 087
Mississip- pi River Vogel's model			1 125 000 0.0828	51.00* 0.255*	4.76	0.44	1.38	8.5	72	684 82

<sup>\*</sup> Mean denth.

To give a concrete idea as to the value of the kinetic factor in canals. Table 7 is given, based on some alluvial canals studied by Fred C. Scobey. M. Am. Soc. C. E. The last two lines of Table 7 give data on the Mississippi River and its model according to Herbert D. Vogel, Assoc. M. Am. Soc. C. E.

<sup>48 &</sup>quot;Stable Channels in Alluvium", by Gerald Lacey, Minutes of Proceedings, Inst. C. E., Vol. 229, Pt. I, p. 283.

<sup>&</sup>quot; Bulletin No. 194, U. S. Dept. of Agriculture.

<sup>45 &</sup>quot;Geometric Versus Hydraulic Similitude", by Herbert D. Vogel, Assoc. M. Am. Soc. C. E., Civil Engineering, August, 1932, p. 471.

Comparison of Tables 6 and 7 in relation to the kinetic factors and tractive forces shows:

1.—Only two cases (Nos. 170a and 214a in Table 7), the kinetic factor being 32.6 and 36.1, more or less approach the same value in the flume. There is gravel in both cases. This proves again that the bed-load material in the prototype must be considerably coarser in order to correspond to the same material in the flume.

2. —The tractive forces in Table 7 are higher in general than in the flume, but all channels are not scouring. Three instances are especially interesting. Two are referred to the same channel with a gravel bed, in which, T = 980 and 2 087 g per sq m, and the third is the Mississippi River, with T = 684. All three values are much greater than the tractive forces in the paper.

The author suggests, as the most practical procedure, that the bottom silt taken from the prototype be tested in the flumes, but such "geschiebe" in a model flume will correspond to a much coarser material in the prototype. In designing the model of a channel with a different kinetic factor, it is necessary to take the corresponding bed-load material and, if Equation (21) is more or less correct, the ratio of the diameters of the "geschiebe" must be equal to the kinetic factor, squared.

Columns (7) and (8) of Table 5 show the maximum and minimum values of tractive forces. These three stable alluvial channels, as already stated, are hydraulically similar. Each of them transports its own specific sand corresponding to its kinetic factor. The tractive forces vary greatly, usually having a greater value in the larger channels. The maximum values are again considerably larger than in the flume, but scouring has no place.

The author referred to Gilbert's conclusion that with equal width-depth ratios, the result of experiments with a flume are, in general, quantitively transferable to channels of different trace. This means that if the crosssections of the model and the prototype are a rectangle, they are geometrically similar; but the cross-sections of models of hydraulically similar channels should be distorted<sup>40, 45</sup> and this distortion must be given consideration because the preservation of hydraulic similitude depends not only on the same kinetic factor, but also on the form of the cross-section. To express this dependence the writer suggests the following equation to:

$$Q = Y R^{2} \dots (22)$$

in which, Y is a constant for hydraulically similar channels and may be termed the "coefficient of hydraulic similitude".

Another interesting relation between the kinetic factor,  $K_r$ , and the coefficient, Y. is:

$$H = \frac{Y}{K_{\bullet}^{0.5}} \dots (23)$$

Of course, Y and  $K_r$  being constant, the coefficient, H, is constant, too, for the same hydraulically similar channels. However, this last coefficient (termed the "hydraulic number") presents an interesting parameter.

Table 5 gives the value of H for three British Indian irrigation projects in which the channels are hydraulically similar. The hydraulic numbers for these three different projects with stable alluvial channels are about the same (approximately 40.0). This naturally suggests the idea that it is quite probable that all stable alluvial channels have the same hydraulic number. Stable alluvial channels are understood to be non-silting and non-scouring, ideal channels with a uniform flow of water and a full silt load. The value of the hydraulic numbers is computed for channels given in all the tables. It is of special interest to note that Lieut. Vogel's model has the same exact value of hydraulic number (40), while all others in Table 7 have larger values. The value, 40, appears to be a limit. All channels in Table 7 are non-scouring, and if the value of the hydraulic number in the alluvial stable channel is less than 40, it may be assumed that they have scouring tendencies when the kinetic factor corresponds with the silt material.

In data concerning the scouring of some drainage channels observed by Charles E. Ramser, M. Am. Soc. C. E. (Table 8), the hydraulic number

TABLE 8.—General Hydraulic Factors; Eroding Drainage Channels

No.	ion No.	ne me	tion of	ge per in cubic	c radius,	locity, in	× 10-4	KINI FAC (PI CENT	TOR R-	COE CIEN HYDR SIMIL	TOF	Hydra	ULIC	Tractive force, in grams per aquare meter
Stream N	Observation	Name	Description channels	Discharge 1 second, in c feet	Hydraulic ra	Mean velocity, feet per second	Slope, 5	Actual	Mean	Actual	Mean	Actual	Mean	Tractiv in gra
1	1*234		Alluvial, sandy, wax-like clay.	794 914 1 221 1 280	5.6	3.6 3.6 4.0 3.8	3,98	7.2 7.6 7.4	7.4	5.2 4.5 5.9	5.2	16.1	19.1	904
2	1*23	Creek, near	Wax-like clay, loam, contain- ing considerable sand.	1 758	7.2	3.5 5.8 4.7	11.6	14.3 7.4		4.7	4.7	12.5		2 996
3	1* 2 3 4	Creek, near	Sandy loam at top to wax-like clay at bottom.	1 354	6.6	3.5 4.35 4.1 4.0	9.29	8.7	8.3	6:1	6.0	17.2		
11	1* 2 3	South Fork, Deer River, near Jackson, Tenn.	Firm, wax-like	1 620 1 740 2 342	7.1	4.0 4.1 4.5	5.15	7.3	7.	4.9	4.5	18.0		1 388
13	1* 2 3 4		Alluvial silty loam at top, heavy silty clay at bot- tom.	1 512	6.6	3.9 4.6 4.5 4.8	5.02	79.8 9.75 10.1	9.	6.4	6.0	. 20.4		1 176
15	14 2 3 4	Sugar Creek, near Hender- son, Tenn.	Light-yellow clay very tenacious and much less easily eroded than soil of Stream No. 11.	400 473 513	3.8	7 3.2 3 3.3 2 3.5 3 3.55	8.38	9.1	9.	6.4	6.7	24.8 21.1 21.3		4 1 23

<sup>\*</sup>Original cross-sections at time of construction computed from dimensions of channels given in specifica-ons. Mean values were computed without considering original cross-sections.

The phenomena of scouring does not occur in Nature as in a rectangular flume. First, it is known that the upper parts of the channel's banks, even

changes from 14.9 to 22.4 (less than 40) and the author's data differ completely from Tables 5, 7, and 8.

<sup>46 &</sup>quot;Erosion and Silting of Dredged Ditches", by Charles E. Ramser, M. Am. Soc. C. E., Technical Bulletin No. 184, U. S. Dept. of Agriculture, June, 1930.

under normal conditions, have a tendency to wash out, become round, and settle. The depths of water in the upper parts, and tractive forces, are less; but scouring occurs and settlement of washed material also occurs where the depth and tractive forces are greater.

Scouring and silting on a bank do not depend on the depth of the water, but on its velocity. Increased velocity will scour the banks of the channel and make it wider. A deep narrow stream has a tendency to widen itself, but the shallow wide stream will deepen some part of the channel to become narrower by silting the remainder. In both cases the stream inclines to adjust itself in a stable channel. Two critical conditions for erosion and silting, in the writer's opinion, depend upon the condition that the kinetic factor must correspond to the transporting material and hydraulic number. For any particular kinetic factor and silt there will be two values of the hydraulic number between which the channel will be stable. For channels having a non-cemented or non-packed bed of the same silt, carried by fully charged water, there will be the same hydraulic number (equal probably to about 40). In the case of a settled bed the difference may be considerable. The cohesion between the particles has to be overcome. The finer the settled materials, the larger the molecular bonds and skin friction will be; but the gravity action increases with the size of the particles. Therefore, clay and sand both need higher velocities to cause erosion than the coarse silt, which gives minimum erosion-velocity conditions."

There is no turbulent flow with parallel filaments of water. The distribution of velocity over the cross-section is the all-important factor. Cross-currents greatly affect the phenomena of silting and scouring. Velocities at any point are constantly changing. Scouring and silting depend on the distribution of velocity along the cross-section (especially at the bottom) and not so much on their absolute value as on their relative changes. If a model is built correctly these relative changes of velocities should be about the same as in the prototype. This explains why hydraulically similar, alluvial, channels are capable of transporting the same material.

In studying any phenomena of flow in channels by the method of models, the first requirement is the hydraulic similitude of flow. Failing to fulfill this requirement and basing conclusions on the doubtful "drag" theory, the author's type of experiments seems to differ from the actual condition in Nature; they may have only a qualitative meaning. No doubt, however, the author's work (especially his new formula for tractive forces based on the silt graduation curve) is very important in laboratory practice.

Morrough P. O'Brien, 46 Assoc. M. Am. Soc. C. E., and Bruce D. Rindlaub, 46 Esq. (by letter) 46a.—The rate of movement of bed-load in channels is known to increase rapidly with tractive force and, for this reason, a visual determination of the critical tractive force is probably sufficiently

<sup>4&</sup>quot; "Problems in the Theory of River Engineering", by Herbert Chatley, Inst. C. E., Selected Engineering Papers No. 71, p. 17.

<sup>48</sup> Assoc. Prof. of Mech. Eng., Univ. of California, Berkeley, Calif.

<sup>49</sup> Berkeley, Calif.

<sup>400</sup> Received by the Secretary August 25, 1934.

accurate for model work; but for establishing a general law, the more precise weighing method appears desirable. In this connection it should be mentioned that there is quantitative evidence indicating that each fraction of a mixture behaves approximately as it would if present alone, at least in the region of general movement. If this statement is true of a mixture acted upon by a tractive force too small to move the larger fractions, the critical tractive force for each fraction can be obtained approximately by analyzing the material caught in the weighing pan. For each sample, the tractive force acting is approximately the critical value for the largest particles caught.

The use of depth times slope as the tractive force is perhaps sufficiently accurate for model work; but it is not a sound procedure since some resistance to flow is exerted by the side walls of the channel. The average tractive force on the side walls and bottom is:

$$T = w R s \dots (24)$$

in which, s is the slope of the energy gradient (not the slope of either the bottom or the water surface); and R is the hydraulic radius. The tractive force on the bottom exceeds the average value in most cases and approaches, but does not equal, w D s.

In regard to the slope to be used in computing the tractive force, if sufficient data are not available to compute the slope of the energy gradient, the slope of the bottom is more nearly correct than that of the water surface, if the bottom is inclined downward in the direction of flow.

The author mentions a paper by Leighly<sup>5</sup> which describes a method of estimating the distribution of tractive force over the wetted perimeter of a channel. Another method that appears to be more sound can be developed from von Karman's theory of turbulent flow near a flat boundary surface. The essence of the theory underlying this method is that the velocity distribution, at a distance from the boundary greater than the thickness of the laminar layer, depends only upon the shearing or tractive force within the fluid. The equation for the tractive force is:

$$T = \rho \left[ \frac{c \left( u - u_0 \right)}{\log_e \frac{z}{z_0}} \right]_i^2 \dots (25)$$

in which,  $\rho$  is the mass density; u and  $u_0$  are the velocities at distances, z and  $z_0$ , from the boundary; and c is a coefficient found from experiment to have a value of 0.4. In order to apply Equation (25), velocities must have been measured at distances from the boundary which are small as compared with the dimensions of the cross-section. Application of this method involves the construction of velocity profiles along lines perpendicular to the bottom at each point.

An interesting possibility of this method is that it may be sufficiently precise to compute the value of the friction coefficient from the velocity dis-

<sup>&</sup>lt;sup>5</sup> "Toward a Theory of the Morphologic Significance of Turbulence in the Flow of Water in Streams", by John B. Leighly, Univ. of California Publications in Geography. Vol. 6, No. 1, pp. 1-22.

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tribution alone without measuring the slope of the energy gradient. The advantage of this method is that it would give the average value of n at one cross-section rather than the average over a finite reach.

Assuming that T has been computed for a number of points around the wetted perimeter, the total resistance per unit length of channel is,  $\int_0^p T \, dp$ , in which, p is the wetted perimeter, and dp is an infinitesimal length along the perimeter. The total resistance is obtained by measuring the area under the curve of T as a function of p. The resistance as computed by the Manning equation is,  $w = \frac{v^2 n^2}{(1.49)^2 R^{\frac{1}{5}}}$ . Equating the two expressions for the re-

sistance, and solving for n,

$$n^{2} = \frac{(1.49)^{2} R^{\frac{4}{3}} \int_{0}^{p} T dp}{w A v^{2}}.....(26)$$

in which, A is the area of the cross-section, and v is the average velocity. Comparison of the value of n computed by this method with that obtained in the usual way will give a check on the validity of von Karman's theory as applied to open channel flow.

Returning to the critical tractive force and its relationship to the characteristics of a sand mixture, the writers are not convinced that the modulus, M, brings about an improvement in the correlation of the existing data. An analysis of the data of Gilbert and others indicated that the critical tractive force can be related to the median diameter alone, with the same or less deviation of individual experimental points, and the relationship is much simpler to apply.

No quantitative theory of bed movement yet advanced adequately represents all the factors involved and, for the present at least, the characteristics of each sand to be used in a movable-bed model must be determined independently. A general theory is needed, but much additional experimental work will be required to develop one that can be applied with confidence. In the meantime, engineers designing models should use present equations with caution.

HERBERT D. Vogel,<sup>51</sup> Assoc. M. Am. Soc. C. E. (by letter)<sup>51</sup>.—The work of Captain Kramer in Germany, as reported in his paper, has served the past few years as no inconsiderable aid to all experimenters interested in the performance of model streams. Prior to the release of his data much conjecturing was needfully resorted to each time it became necessary to design a movable-bed river model; more recently, it has been possible to approach each problem from a standpoint of reason and logic.

Two statements of the author appear worthy at this time of special repetition and emphasis: (1) "\* \* \* strict compliance with the laws of

sae Received by the Secretary September 21, 1934.

<sup>&</sup>lt;sup>20</sup> "The Transportation of Bed-Load by Streams", by M. P. O'Brien, Assoc. M. Am. Soc. C. E., and B. D. Rindlaub, *Transactions*, Am. Geophysical Union, 1934.

<sup>51</sup> Lieut., Corps of Engrs., U. S. Army, Fort Leavenworth, Kans.

similitude must be waived in fluvial models in which bed movement is of predominating importance;" and (2) "since it [Equation (10)] was derived empirically and from limited data, its scope of application and probable accuracy are subject, of course, to obvious limitations."

Referring to the first of these considerations it is evident that the requirements for adequate bed movement in a fluvial model are at variance with those indicated for preservation of strict Froudian relationships. This is true because for any fixed model depth it is generally necessary to apply steeper slopes in order to produce a movement of the bed material similar to that of Nature, whereas to secure a velocity scale equal to the square root of the vertical scale, a model must be provided, in nearly every case, with flatter slopes than would result from normal distortion. Similarly, a large degree of distortion is conducive to greater bed movement, whereas little or no distortion is desirable from the standpoint of satisfying the Froudian law. Thus, the experimenter is faced with contradictory requirements, and the only solution is by way of deciding from an estimate of the situation the line of attack to pursue, keeping in mind the mission to be accomplished. This is generally an easy task.

The second point emphasized by the author, may cause some doubt in the minds of a few as to the reliability of his uniformity modulus. This is relatively unimportant, however. because future investigations will serve to reveal better values for it from time to time. The important fact is that a start has been made in the right direction and a line thus indicated for further research.

Investigations are being conducted currently in different parts of the world to determine specifically the effects on movement resulting from changing the specific gravity or the mixture of the bed material. Tests are also being made to determine volume rates of movement and the effects of turbulence, roughness, etc., on movement. All these have followed from the original investigation conducted and reported upon by Captain Kramer.

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Founded November 5, 1852

# DISCUSSIONS

# THE RESERVOIR AS A FLOOD-CONTROL STRUCTURE

## Discussion

BY C. MAXWELL STANLEY, JUN. AM. SOC. C. E.

C. Maxwell Stanley, Jun. Am. Soc. C. E. (by letter). — Much information of a basic nature is assembled in this paper concerning the function and the design of reservoirs as flood-control structures. A number of methods of operating reservoirs and, correspondingly, of design, are presented, together with outlines of various manners of combined reservoir usage for flood control and other purposes. The methods of operation, and, hence, of design, of reservoirs for flood control are numerous. The ingenious methods which have been and will be developed to solve the mass of routine and tedious computations involved in the study of a reservoir system are equally numerous.

This paper has been written with a background largely of the Mississippi River, which, as the author points out, is undoubtedly the "No. 1" floodcontrol problem of this country. The size and scope of so large a flood-control project, as that required in the case of the Mississippi, create many situations and points of view which are not strictly applicable to projects of lesser size and scope. As an instance, consider the numerous references, in the paper, to the use of selected maximum floods of record in designing the controlling structures. While a considerable reliance on past records of stream flow may be justified when the flow comes from large areas and diversified sources, as in the case of the Mississippi, an equal reliance on past streamflow records may cause grave error with drainage areas of only a few hundred or a few thousand square miles. In such instances, careful investigation of the rainfall probabilities must be made, as a single, heavy downpour may result in a run-off much greater than anything that has been experienced in the past. From the results of such an investigation, assisted, of course, by data on flood discharges of the past, a design flood may be determined

Note.—The paper by George R. Clemens, Assoc. M. Am. Soc. C. E., was published in May, 1934, *Proceedings*. This discussion is published in *Proceedings* in order that the views expressed may be brought before all members for further discussion.

<sup>7</sup> Cons. Engr. (Young & Stanley, Inc.), Muscatine, Iowa.

<sup>76</sup> Received by the Secretary August 13, 1934.

which will form a basis for the proportioning of the controlling structures. Past records cannot be used blindly on any occurrence as far beyond the control of Man as rainfall and run-off.

What would have been the standards of design of controlling structures and the criterion of flood discharge on the Mississippi to-day, had the floods of 1927 been delayed until 1937 by some combination of hydrological circumstances beyond the control of Man?

Furthermore, small drainage areas do not offer the opportunities of predicting and forecasting run-off and river stage which are possible on a system the size of the Mississippi where reasonably accurate predictions of conditions may be made days and, sometimes, weeks in advance. In contrast, the floods on the small areas may develop within 24 hr and may come without warning as a result of a peculiar combination of rainfall and run-off conditions. The likelihood of sudden and sharp floods tends to rule against the intricate and completed schedules of reservoir operation which may be designed and used on a larger system where more time is available and where there is a competent staff to carry out the work of predicting the flood and scheduling the operation of the reservoirs. Indeed, the probability of the sudden and sharp flood peak on the small drainage area seems to demand, in most cases, a structure the operation of which is automatic and is not dependent upon the human element. This tends to eliminate the reservoir with an outlet controlled by gates and to favor the use of the retarding type of reservoir, or the complete elimination of reservoirs in favor of levees, channel improvements, etc.

Considerable controversy has raged between those advocating the use of reservoirs to limit the flood discharge and those advocating the use of structures, such as levees, floodways, etc., which increase the carrying capacity of the channel. Much of such controversy might be avoided by giving careful attention to the purpose of economical flood control.

The purpose of flood control, of course, is to prevent damage to property, and loss of life. This purpose is accomplished by constructing the necessary structures to assure that the maximum flood discharge at the point to be protected is within the carrying capacity of the channel through which the flood must pass. Obviously, this end may be obtained by decreasing the size of the flood peak, by increasing the channel capacity, or by a combination of these two methods.

The function of a reservoir is to decrease the flood peak passing a given point, or points, and the function of channel improvements, levees, floodways, etc., is to increase the carrying capacity of the channel. Theoretically, suitable protection might be obtained by the use of either reservoirs alone or by channel improvements alone, provided, of course, that suitable reservoir sites are available. The reservoirs must be sufficiently large to limit the flood flow to the capacity of the unimproved channel, or the channel must be of sufficient magnitude to provide a channel capacity capable of carrying the maximum unregulated flow. In many cases, one of these solutions may pro-

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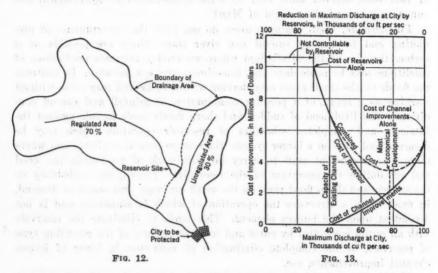
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vide the most practical and most economical answer to the problem, but in many cases a combination of the two methods (that is, the use of both reservoirs and channel improvements) may provide a more economical solution.

The proportion in which they should be combined is largely an economic problem which must be solved for each project. As an example, assume the very simple hypothetical case shown in Fig. 12 of a flood-control project to protect



a single city from a river of relatively small drainage area. The maximum flood discharge from this area is assumed to be 100 000 cu ft per sec. On the water-shed of this river, it is possible to develop a single reservoir that will regulate the flow from 70% of the drainage area. The existing channel through the city is capable of carrying 40 000 cu ft per sec, or 40% of the designed flood peak for the project without further improvements.

If reservoirs alone are used to hold the peak flood within the capacity of the existing channel, an expenditure of \$10 000 000 may be required. If, on the other hand, the reservoir is not developed and flood protection is obtained solely by improvements to the channel, construction of the levees, etc., the cost to care for the maximum flood may be only \$6 000 000. On the face of this, it would indicate that the use of channel improvements alone might be the most economical solution.

However, there are possibilities of combined development which will provide a more economical arrangement. Suppose, for instance, that the channel is improved to increase its carrying capacity to 50 000 cu ft per sec of the maximum flood peak for which the system is being designed and that the reservoir is developed to limit the flood flow in the channel at the city to 50 000 cu ft per sec, or 50% of the maximum flood. As 30% of the drainage area is unregulated, this will mean that the reservoir must be capable of reducing the flow from the area controlled to 20 000 cu ft per sec, thus

\$5 400 000

reducing the discharge at the city to 50 000 cu ft per sec. With such a development the costs would be as follows (taken from curves of Fig. 13):

Cost of reservoir	\$4 950 000 450 000
_	

This represents a saving of \$600 000 over protection by channel improvements alone.

A study of further combinations of reservoir development and channel improvements (made from the curves of Fig. 13) indicates that a minimum cost of flood control will be obtained with a channel capacity of 78% of the maximum flood peak, or 78 000 cu ft per sec, and a reservoir capacity sufficient to reduce the flow at the city to 78 000 cu ft per sec. Under this condition the reservoir must reduce the flow from the regulated area from 70 000 cu ft per sec to 48 000 cu ft per sec, or by 22 000 cu ft per sec. With this arrangement the costs are as follows:

Cost of	channel improvement	2 200 000 \$3 500 000
Cost of	reservoir	\$1 300 000

This simple example is illustrative of the results that may be obtained, by an intelligent combination of reservoirs and channel improvements. Naturally, the usual flood-control project will not be as simple as the hypothetical one considered herein, but the method illustrated is capable of application. Such methods were developed and used in the design of the Miami Conservancy District<sup>8</sup> which, of course, presented a much more complicated plan.

Reservoir and channel improvements both have their places in flood-control work; both have their advantages; and both have their limitations. The design of any given flood-control project should not be concerned solely with the relative merits of reservoirs alone or channel improvements alone, but should be concerned with obtaining the most economical plan, which may often be a combination of reservoirs and channel improvements.

<sup>&</sup>lt;sup>8</sup> "Hydraulics of Miami Flood Control Project", by Sherman M. Wood, Technical Repts., Miami Conservancy Dist., Pt. 7, Chapter 12.

# AMERICAN SOCIETY OF CIVIL ENGINEERS

Founded November 5, 1852

# DISCUSSIONS

# FLOW OF WATER AROUND BENDS IN PIPES

# Discussion

By Messrs. D. Benjamen Gumensky, Wallace M. Lansford, and F. T. Mavis.

D. Benjamen Gumensky, Assoc. M. Am. Soc. C. E. (by letter). —The explanation of the phenomena of flow around bends, contained in this paper, is very elucidating. Particularly clear and useful are the sections, "Velocity Conditions Within the Bend" and "Pressure Changes Within the Bend." The section on "Loss of Head in Bends" is of extreme interest to the designer of large pipes where the cost of head is high. In such cases the loss of head due to bends may have considerable influence on the selection of the most economical size for the pipe.

The loss of head due to bends was a subject of study in connection with the design of large siphons in the Colorado River Aqueduct. This aqueduct, now under construction (1934) by The Metropolitan Water District of Southern California, has in its main part 150 siphons, aggregating 27 miles in length. In these siphons, head losses due to bends are computed by the empirical formula:

$$h_b = K\left(\frac{V^2}{2g}\right)....(4)$$

in which,  $h_b$  is the loss in one bend; V, the mean velocity in the pipe; and g, the acceleration due to gravity; and,

$$K = C \sqrt{\frac{\Delta}{90}} \dots (5)$$

in which, C is a coefficient depending on the ratio of pipe diameter to radius of bend; and  $\Delta$  is the deflection angle, in degrees.

Equation (4) was devised several years ago by Julian Hinds, M. Am. Soc. C. E., in an arbitrary manner, after a study of the extremely discordant literature on the subject available at that time.

Note.—This paper by David L. Yarnell, M. Am. Soc. C. E., and the late Floyd A. Nagler, M. Am. Soc. C. E., was presented at the Joint Meeting of the Power Division of the Society and the Hydraulics Division of the American Society of Mechanical Engineers at the Annual Convention, Chicago, Ill., on June 29, 1933, and published in August, 1934, Proceedings. This discussion is printed in Proceedings in order that the views expressed may be brought before all members for further discussion.

<sup>&</sup>lt;sup>7</sup>Asst. Engr., The Metropolitan Water Dist. of Southern California, Los Angeles, Calif. <sup>76</sup>Received by the Secretary September 24, 1934.

Although the total head allowed in siphon bends on the aqueduct is appreciable, the effect of bends is small in comparison with other factors, and it was considered safe to proceed with Equation (4) without attempting to substantiate it experimentally. However, the writer and others were interested in the problem and attempted to set up a small-scale experiment on their own initiative. R. R. Proctor, Assoc. M. Am. Soc. C. E., and members of his staff, made water and facilities available and assisted with the experiment. It is described herein in order to supply additional experimental data, and in the hope that the several points of discussion will merit Mr. Yarnell's attention in the closing discussion.

The experiment consisted in measuring the bend losses in a 2 by 2-in. square pipe for different angles of bend and different radii of curvature. Measurements were made on bends of 180°, 135°, 90°, 45°, and 20° for radii of curvature of 20, 8, and 4 in. Velocities varied from 5 to 16 ft per sec.

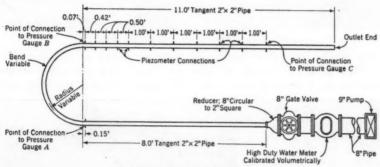


FIG. 10 .- EXPERIMENTAL SET-UP

The experimental set-up is shown in Figs. 10, 11, and 12. The water was pumped from a well through a calibrated meter and a reducer into an 8-ft tangent of 2 by 2-in. square pipe; then it was passed through a bend, an 11-ft tangent, and discharged into the air. The outlet end of the straight tangent had to be constricted in order to build up back pressure. The same two tangents were used for all set-ups; and each bend was carefully fitted and aligned between the tangents. The connections were made by soldering the seams from the outside and being careful that no solder would project into the section of the pipe and form an obstruction.

With a differential pressure gauge the loss of head was measured from a point 2 in. "up stream" from Bend (A) to a point 1 in. "down stream" from the end of Bend (B), and from the latter point to a point 8 ft farther along the tangent to Point (C). Then, as a check on the two measurements, an over-all loss was measured from the point above the bend to the point near the outlet end, Gauge (A) to Gauge (C). This measured total loss of head was compared with the experimentally determined loss of head in the identical lengths of straight pipe for the same velocity. The difference was considered to be the loss due to the bend.

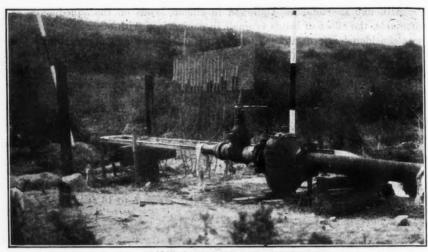


FIG. 11 .- SET-UP FOR 180 DEGREE BEND

The results reduced to coefficients of velocity head in Equation (4) are shown in Fig. 13. Although the work was done with rather crude equipment the results are reasonably consistent. The general trend of variation and the

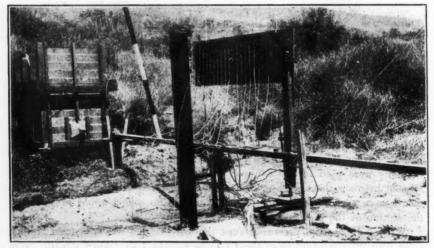


FIG. 12.—SET-UP FOR 10 DEGREE BEND

actual values of losses seem to coincide quite definitely with those reported by the authors. The solid, horizontal lines denoting values of C  $\sqrt{\frac{\Delta}{90}}$  were defined by the results of the test. The curve for K by Equation (5) (with C=0.25) is that used by The Metropolitan Water District of Southern California.

All the observed losses are smaller than those computed from Equation (4). Ignoring the observations for curves of 180° deflection, the average of all readings falls almost exactly on the line:

$$K = 0.16 \left(\frac{\Delta}{90}\right)^{0.845} \dots (6)$$

The coefficients of bend loss for 180° fall out of the line with others and proportionately are much smaller. No satisfactory explanation of this devia-

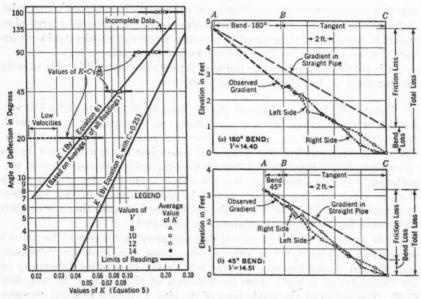


FIG. 14.—TYPICAL BEND LOSS MEASUREMENTS

tion can be offered. No regular variation of the value of K with radius was discovered. If the observations are segregated as to velocity, it is found that the value of K increases with increasing velocity. This would indicate that the bend loss is proportional to a power of V greater than two, which is contrary to Conclusion (7) of the paper. The character of the experiment and the results obtained do not warrant an attempt to determine the exact value of this power.

Actual observations have shown that the pressure on both sides of the straight pipe below the bend varied, changing from the position above the average value to that below it, as if the water were bouncing from one side of the pipe to the other. This was disclosed by observation on piezometers connected to both sides of the tangent below the curve, which can be seen on Figs. 11 and 12. Fig. 14 shows the typical measurements and the losses. The curves shown are not smoothed out, but are drawn through points of individual measurements.

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The loss of head due to bend was measured not entirely in the bend, but also in the straight pipe following. This is well shown on Fig. 14. Similar results were found by Mr. A. W. Brightmore's in his experiments on elbows and bends in 3-in. and 4-in. pipe. Examining the authors' Fig. 8, it is readily seen that conditions were similar to those described herein. The energy gradient in a tangent following the bend is steeper than that for the straight pipe and does not become parallel to it for a distance varying between 5 and 15 ft from the end of the bend.

It is a regrettable fact that all the observations made thus far have been on pipes of small diameters. Application of principles of similitude to the existing experimental data in order to determine the probable losses in large pipes would be uncertain and speculative, although in actual practice engineers are forced to assign definite values to bend losses in large pipes.

It is sincerely hoped that in the near future some one will be able to make measurements of bend losses in large pipes.

WALLACE M. LANSFORD, ASSOC. M. AM. Soc. C. E. (by letter). -- The suggestion of the authors to use pipe bends as flow meters is a valuable one, although they are not the first to propose such a possibility. The writer first heard of this method of measuring the flow of water in the discussion of this paper by the late Professor Nagler following its oral presentation.1 In the summer of 1933 the writer made a series of tests which seem to verify two conclusions reached by the authors, first, that an elbow in a pipe line could be used as a flow meter; and, second, that where great accuracy is required, each elbow should be calibrated.

Since relatively few experimental data are given in the paper, the writer's experiments will be stated in some detail. Tests were made on three castiron, flanged elbows located in a pipe line in the Hydraulics Laboratory of the University of Illinois, under the direction of M. L. Enger, M. Am. Soc. C. E. The radius of the inside bend of the elbows and the nominal diameter of both pipe and elbows were 4 in. The length of straight pipe preceding each elbow was 150 ft 2 in.; 8 ft 6 in.; and 128 ft, respectively. The pressure connections, 1 in. in diameter, were made on both the inside and outside bends of each elbow at points approximately 45° from each flange in the plane of symmetry of the bend. An individual differential gauge was used for each elbow. The fluid (carbon tetrachloride and gasoline dyed red) used in all three gauges was taken from one mixture, thereby assuring identical co-

<sup>8</sup> Minutes of Proceedings, Inst. C. E., Vol. 169, pp. 315 et seq.

<sup>9</sup> Assoc., Theoretical and Applied Mechanics, Unv. of Illinois, Urbana, Ill.

<sup>96</sup> Received by the Secretary October 8, 1934.

New Method of Water Measurement by Use of Elbows in a Pipe Line," Gaskell S. Jacobs and Francis A. Sooy, Journal of Electricity, Power, and Gas, July 22, 1911, Vol. 27; "Die Turbinen für Wasserkraftbetrieb," von A. Pfaar, 1912. (He gives the following references: Isaachsen in Zivilingenieur, 1886, p. 338, and 1896, p. 352; Kankelwitz (Stuttgart), about 1870); "A Flow Metering Apparatus," by A. M. Levin, Journal, A. S. M. E., September, 1914; "The Hyperbo-Electric Flow Meter," Power, June 26, 1923; and "The Flow in Curved Pipes and its Stability," by Otogoro Miyagi, Vol. XI, No. 1, Technology Repts., Tohoku Imperial Univ.

<sup>&</sup>lt;sup>1</sup> At the Joint Meeting of the Power Division of the Society and the Hydraulics sion of the American Society of Mechanical Engineers at the Annual Convention, Division of the American Soci Chicago, Ill., on June 29, 1933.

efficients. The velocity in the pipe was controlled by a valve at the outlet end. The discharge was measured by letting the water flow into a calibrated pit tank which had a cross-sectional area of 28.20 sq ft, and noting the rise of the water and the elapsed time of each run. The water could be turned quickly into the pit tank or diverted from it by means of a swinging pipe.

During any one run all three gauges were read when the water was flowing into the pit tank, thus assuring the same discharge through each elbow for any one set of readings. Time was measured by a stop-Water was taken from a watch. stand-pipe, 6 ft in diameter and 65 ft high, near the top of which was an overflow weir approximately 15 ft long. Water flowed over this weir continuously, thereby maintaining constant pressure throughout all the tests. Data were taken in several runs with velocities varying from 0.77 ft per sec to 5.72 ft

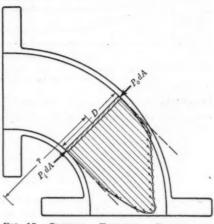


FIG. 15.—SECTION THROUGH CENTER OF ELBOW SHOWING VELOCITY DISTRIBUTION

Using a small prism of water of length, L, and of cross-sectional area, dA, as shown in Fig. 15:

$$(p_o - p_i) dA = \left(D \frac{V^2}{r}\right) \frac{w}{q} dA \dots (7)$$

and,

$$h = \left(\frac{p_o}{w} - \frac{p_t}{w}\right) = \left(\frac{2D}{\overline{r}}\right) \frac{V^2}{2g} = k \frac{V^2}{2g} \dots (8)$$

in which, V = mean velocity of water in pipe, in feet per second;  $p_i =$  unit intensity of pressure at inside of bend, in pounds per square foot;  $p_o =$  unit intensity of pressure at outside of bend, in pounds per square foot;  $\overline{r} =$  radius of the mass center of the prism, in feet; and D = diameter of elbow, in feet.

Equation (8) shows that the difference in pressure head between the outside and inside of an elbow through which water is flowing, is a constant times the velocity head (based on the average velocity), provided the value of  $\overline{r}$  does not change for different rates of flow. Ordinarily, the radius,  $\overline{r}$ , is less than the radius of the center line of the elbow, because the velocity of flow is highest near the inside of the bend. However, with abnormal distribution of velocity at the entrance of the elbow, the radius,  $\overline{r}$ , might be increased or decreased.

The curves in Fig. 16 show the relation between  $c_k$  and the average velocity in the pipe. It can be seen from these curves that  $c_k$  is a constant for each

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elbow when the velocity of the water in the pipe is approximately 1.5 ft per sec, or greater. This agrees with the conclusion of the authors that the elbow

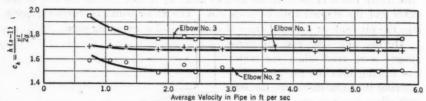


FIG. 16.—RELATION BETWEEN C. AND VELOCITY IN PIPE FOR THREE 4-INCH ELBOWS (RADIUS OF INSIDE BEND, 4 INCHES)

is valuable as a meter, and that each elbow should be calibrated for accurate use. The more constant value of  $c_k$  for each bend was, as follows (see Fig. 16):

Elbow	N	0	).																Value of c
1																			1.68
2																			1.51
3																			1.77

Later, all elbows were interchanged in all positions in the pipe line, but the direction of flow through them was not changed. Values of  $c_k$  for the elbows, when in the latter positions, deviated about 3% from those shown in Fig. 16. This difference could be due to the effect of changing gaskets, or to the eccentricity of the elbows caused by a large clearance of the bolts in the holes through the flanges. The length of straight pipe preceding each position of the elbows seemed to be sufficient not to affect the value of  $c_k$ .

From Equation (8) the theoretical value of  $c_k$  for the elbows tested would

be 
$$c_k = \frac{2D}{r} = 1.33$$
, if  $\overline{r}$  is taken as the radius to the center of the elbow. In

order to investigate the discrepancy between the actual and theoretical values of  $c_k$ , a Pitot tube traverse was made of Elbow No. 2 when in the southeast position where it was preceded by 150 ft 2 in. of straight pipe. The measured velocity curve is shown in Fig. 15. This curve is quite different from that assumed in the theoretical analysis. A rough calculation of  $\bar{r}$  for this velocity distribution, assuming the water to flow in stream lines, shows it to be about

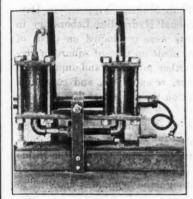
5.72 in. instead of 6 in. Therefore, 
$$c_k$$
, would be  $\frac{2D}{5.72} = 1.40$ . It will be noted

that a small variation in  $\overline{r}$  changes the value of  $c_k$  materially; thus, when  $\overline{r}$  is 5.33 in.,  $c_k = 1.50$ . This would probably account for some of the difference between the actual and theoretical values of  $c_k$ .

On the basis of the information obtained from the tests herein reported, a useful device known as a flow indicator has been built and is being used successfully in the Hydraulics Laboratory of the University of Illinois. The centrifugal pumps that supply the water are on the basement floor, approximately 5 ft above the level of the water in the supply channel. The control switches for the motors that drive the pumps are on the floor above. When a

pump is started it is convenient and important to know whether or not it is actually delivering water. The device is shown in Figs. 17 and 18. It consists essentially of two closed steel cylinders approximately  $1\frac{3}{4}$  in. in inside diameter

and 3 in, long, mounted end-wise on a steel bar and balanced on the bolt at



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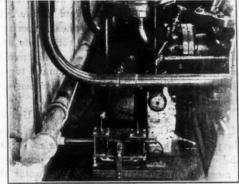


FIG. 17 .- THE FLOW INDICATOR

FIG. 18.—THE FLOW INDICATOR INSTALLED

mid-span as a fulcrum. The cylinders, about one-half full of mercury, are directly connected beneath by \$\frac{1}{8}\$-in. pipe. The \$\frac{1}{16}\$-in. copper tube that connects the left cylinder to the outside bend of the elbow and the right cylinder to the inside is shown in Fig. 18. Water flowing through the elbow produces a high pressure at the outside of the bend and a low pressure at the inside, which causes the mercury to flow from the left cylinder to the right cylinder. The unbalanced weight causes the right end of the indicator to deflect and to make contact with an electric terminal. This closes an electric circuit which, in turn, lights a small electric light above the control switch on the first floor. When the pump is stopped the mercury flows back into the left cylinder, thus equalizing the weight and breaking the electric circuit. Two of these indicators are used on two pumps having a discharge capacity of 1 000 gal per min, each, and two on two pumps having a discharge capacity of 2 000 gal per min, each. All the indicators were installed in January, 1934, and have given good service.

F. T. Mavis," Assoc. M. Am. Soc. C. E. (by letter)."—A valuable summary of a long series of painstaking tests is presented in this paper. The authors deserve much credit for reviving the use of a bend as a flow meter and for their leadership in this particular research, which has also been included in the programs of other laboratories in the United States.

Attention should be called to the work of other investigators who have made significant contributions to the investigations of the hydraulics of bends in pipes. The pioneer work of Weisbach<sup>12</sup> in Germany about the middle of

<sup>&</sup>lt;sup>11</sup> Associate Director in Chg. of Laboratory, Iowa Inst. of Hydraulics Research; and Associate Prof., Dept of Mechanics and Hydraulics, The State Univ. of Iowa, Iowa City, Iowa.

<sup>&</sup>lt;sup>116</sup> Received by the Secretary October 15, 1934.
<sup>12</sup> "Lehrbuch der Ingenieur und Maschinen Mechanik," von J. Weisbach, p. 439.
Leipzig, 1845.

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the Nineteenth Century is often referred to in current hydraulic literature. Twenty-five years or more ago, Alexander<sup>18</sup> and Brightmore<sup>14</sup> were conducting tests in England, and Williams, Hubbell, and Fenkell,<sup>15</sup> and Schoder<sup>16</sup> were making tests in this country. Among the current investigators might be mentioned the names of Hoffmann<sup>17</sup> and Schubart<sup>15</sup> in Munich, Nippert,<sup>15</sup> in Danzig, and Giesecke,<sup>26</sup> and the Staff of the National Hydraulics Laboratory in the United States. Most of these experiments were conducted on pipes of circular cross-section, although some tests were made on pipe of square or rectangular section. Doubtless, there are many other published and unpublished investigations which could be brought together, re-appraised, and correlated to make an exceedingly valuable reference work on the subject of flow of water around bends.

Many tests have been made at the University of Illinois by M. L. Enger, M. Am. Soc. C. E., and W. M. Lansford, Assoc. M. Am. Soc. C. E., to study the properties of bends as flow meters. In 1916, the idea of tapping the inside and outside of a bend and using the pressure difference in these two points as a means of determining the flow of water through the bend, was credited to Mr. Buckner Speed by the late J. C. Trautwine, Jr., Affiliate, Am. Soc. C. E. Mr. Trautwine also referred to tests reported by Messrs. G. S. Jacobs and F. A. Sooy, which led to an equation expressing the relation between the velocity in the pipe, V, the pressure difference, h, in feet of water, the radius of the bend, r, and the diameter of the pipe, D, as follows:

$$V = c \sqrt[n]{h \frac{r}{D}} \dots (9)$$

in which, c=5.6 and u=1.9. Other data and calibration tests of a similar flow-metering apparatus were reported in 1914, by Mr. A. M. Levin.<sup>25</sup>

The problem of the hydraulics of bends has been investigated in some detail from an analytical basis. zur Nedden has presented certain aspects of the

<sup>13 &</sup>quot;The Resistance Offered to the Flow of Water in Pipes by Bends and Elbows," by C. W. L. Alexander, *Minutes of Proceedings*, Inst. C. E., Vol. 159, 1904-05, Pt. I. pp. 341-364.

<sup>14 &</sup>quot;Loss of Pressure in Water Flowing Through Straight and Curved Pipes," by A. W. Brightmore, Minutes of Proceedings, Inst. C. E., Vol. 169, 1907, p. 315.

<sup>&</sup>lt;sup>15</sup> "Experiments at Detroit, Michigan, on the Effect of Curvature on the Flow of Water in Pipes," by the late Gardner S. Williams, M. Am. Soc. C. E., and Clarence W. Hubbell and George H. Fenkell, Members, Am. Soc. C. E., Transactions, Am. Soc. C. E., Vol. XLVII (1902), pp. 1 to 369.

<sup>16 &</sup>quot;Curve Resistance in Water Pipes," by E. W. Schoder, M. Am. Soc. C. E., Transactions, Am. Soc. C. E., Vol. LXII (1909), pp. 67 to 112.

<sup>17 &</sup>quot;Neue Untersuchungen über den Druckverlust in Rohrkrümmern," von A. Hoffmann, Mitteilungen des Hydr. Inst. der Techn. Hochschule, München, Heft 2, pp. 70-71, 1928; also, Heft 3, pp. 45 ff, 1929.

<sup>&</sup>lt;sup>18</sup> "Der Energieverlust in Kniestüchen bei glatter und rauher Wandung," von W. Schubart, Mitteilungen des Hydr. Inst. der Techn. Hochschule, München, Heft 3, pp. 121-144, 1929. ("Energy Loss in Smooth and Rough Bends and Curves in Pipe Lines," tr. by F. T. Mavis, Assoc. M. Am. Soc. C. E.)

by F. T. Mavis, Assoc. M. Am. Soc. C. E.)

19 "Uber den Strömungsverlust in gekrümmten Kanälen," von H. Nippert, Forschungsarbeiten, Heft 32, 1929.

<sup>&</sup>lt;sup>20</sup> "Friction of Water in Elbows," by F. E. Giesecke, M. Am. Soc C. E., *Transactions*, Am. Soc. of Heating and Ventilating Engrs., Vol. 32, 1926, pp. 303-314.

n Transactions, Am. Soc. C. E., Vol. LXXX (1916), p. 911.

Journal of Electricity, Power, and Gas, San Francisco, Calif., July 22, 1911.

<sup>2 &</sup>quot;Flow Metering Apparatus," by A. M. Levin, Transactions, A. S. M. E., Vol. 36. 1914, pp. 239-254.

problem which merit the mention of his paper<sup>24</sup> in particular. He calls attention to the fact that a bend may perform quite differently, depending on whether the flow of the fluid through it is laminar or turbulent. He cites specifically the case of a bend of rectangular cross-section the inner and outer curves of which were hyperbolic, as causing a lower head loss than a circular bend as long as the flow remained laminar; as soon as the flow became turbulent, the hyperbolic bend caused a greater head loss than the circular bend. This behavior would be apparent, of course, if the coefficients of velocity head, representing the excess head loss in the bend, were plotted as a function of Reynolds' number.

To-day, it is generally recognized that in flowing around a bend under turbulent flow conditions, a liquid moves in a so-called "spiral" or "helical" path, and that the induced currents and attendant impact are largely responsible for excess losses of head in bends. In 1902, the late H. W. Brinckerhoff, M. Am. Soc. C. E., discussing the paper by Messrs. Williams, Hubbell, and Fenkell, explained the fact that a bend offers greater resistance than an equal length of straight pipe on an hypothesis of spiral flow which he described in its essentials precisely as other writers have done. In their closing discussion, Messrs. Williams, Hubbell, and Fenkell replied to Mr. Brinckerhoff's comments as follows:

"At one time, one of them [the writers] was disposed to explain certain phenomena on the theory of a spiral motion, but in spite of attempts to locate such motion, no direct experimental evidence of its existence has yet been obtained, and, though the writers consider that Mr. Brinckerhoff's theory is ingenious and possibly correct, they are not prepared to endorse it."

Transparent model bends, such as those used by the authors and C. A. Mockmore,<sup>25</sup> M. Am. Soc. C. E., permit the observer to see this spiral or helical flow. These transparent models have done much to create a better understanding and a more intimate knowledge of the phenomena of hydraulics. To-day, this spiral flow in bends can be observed; three decades ago, it was an hypothesis which eminent hydraulic engineers were then "not prepared to endorse."

25 "Flow in Bends of Quarter-Turn Draft-Tubes," by C. A. Mockmore (Abstract), Civil Engineering, September, 1934, p. 460.

<sup>&</sup>lt;sup>24</sup> "Induced Currents in Fluids," by F. zur Nedden, *Transactions*, Am. Soc. C. E., Vol. LXXX (1916), pp. 844-913.

### AMERICAN SOCIETY OF CIVIL ENGINEERS

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Founded November 5, 1852

## DISCUSSIONS

# STREET THOROUGHFARES A SYMPOSIUM

Discussion

By DONALD M. BAKER, M. AM. SOC. C. E.

Donald M. Baker,<sup>18</sup> M. Am. Soc. C. E. (by letter). <sup>18a</sup>—Just as many thousand miles of steam railroads were built before the economic principles of railroad construction were evolved and put in practice, so thousands of miles of highways were constructed and improved before such principles underlying their development were formulated and used. The various papers in this Symposium well set forth the principles underlying the use, design, and location of street thoroughfares. The definitions contained therein will be of material assistance to those engaged in solving traffic and vehicular transportation problems.

Of these principles, now fairly well recognized, least is known concerning those relating to highway financing, particularly in urban areas. Current practice is, through gasoline and motor-vehicle taxes, to place the major portion of the cost of constructing and maintaining highways located outside urban areas upon the users of such highways, while in urban areas such costs are borne to a large extent by property served, or assumed to be served.

The reasons leading to the development of such practices are of more practical than scientific soundness. It was soon found that values of suburban and rural property were insufficient to support the costs involved, and that the benefits accruing to such property were small in proportion to those accruing to the users of such highways. Therefore, if such highways were to be constructed and maintained to proper standards and in sufficient number to satisfy the growing demand, their costs would have to be borne principally by those using them.

In the case of highways in urban areas, a different situation existed. Urban property values were many times higher than those in outside areas, and such properties at the outset were considered well able to bear construction and maintenance costs. During the decade, 1920–1930, which saw rising

Note.—The Symposium on Street Thoroughfares was published in August, 1934. Proceedings. Discussion on this Symposium has appeared in Proceedings, as follows: October, 1934, by H. Shifrin, M. Am. Soc. C. E.

<sup>18</sup> Cons. Engr., Los Angeles, Calif.

<sup>186</sup> Received by the Secretary October 15, 1934

traffic congestion becoming a serious menace and, during which, many street thoroughfares were developed, rising prices and the general real estate "boom" throughout the country caused, at the outset, an increase in property values in areas served by these new thoroughfares, out of proportion to the general rise in property values. A change in the traveling habits of the public, brought about by the increasing use of the motor vehicle, likewise contributed to this rise.

Sales of property were made at large profit, more thoroughfares were developed, and more profitable sales were made. No objection was raised by property owners to this method of financing thoroughfares because of these increased values or because such costs were largely paid by subsequent purchasers of their property. Gradually, however, the operation of economic laws came into play. The margin of profit between benefits, measured in terms of enhanced property values, and costs charged against the property which paid the costs were reduced and in some cases disappeared. This condition was greatly aggravated by the deflation in property values which took place in the period following 1929.

The need for additional street space persisted. Since local tax revenues, reduced through deflated property values and burdened by unemployment relief measures, were not sufficient to carry the cost of providing this additional street space, a demand arose for a greater allocation of gasoline and motor-vehicle tax revenues to urban highway construction and maintenance.

The problem of highway financing has four phases: (1) The determination of the different interests benefited by the construction and continued operation of the highway; (2) the evaluation of the benefits accruing to each of the interests thus benefited; (3) the allocation of construction and maintenance costs among the benefited interests in an equitable manner; and (4) the development of a method of collecting such costs from such interests.

The following principles should be observed as controlling in any policy of highway financing, whether it apply to urban or outside highways:

(a) The benefits received may be direct or indirect; (b) the benefits must ultimately be expressed in terms of dollars and cents; (c) the costs should be allocated in proportion to, but must not exceed, the benefits derived; (d) the costs should be within the ability of the benefited interests to pay; and, (e) the method of collecting such costs must be simple and practical, yet sufficiently equitable as to meet with popular approval and support.

The problem does not admit of an exact solution, but an approximate one may be developed. The interests benefited fall into the following classifications: (1) Users of the highways, principally passenger and commercial motor vehicles; (2) property served by the highways, including (a) property abutting the highway; (b) property in an area adjacent to the highway, but not abutting thereon; and (c) a larger area within the community which is indirectly served and, therefore, benefited.

The gasoline and motor-vehicle tax appears to be generally accepted as a satisfactory method of financing highways outside urban areas on account

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of its approximate equity and it ease of collection. Unless large inroads are made upon these revenues, for urban highways and for other purposes, this method will probably continue to prove satisfactory for future needs. Because of changed conditions, a new and more equitable method of financing urban highways, particularly street thoroughfares, appears to be necessary. Determination of the interests benefited, and the evaluation of benefits accruing must be made in a more scientific manner. The development and application of sound principles for financing these thoroughfares is the crux of the entire problem. The writer agrees in the recommendation of the Committee that "a new type of street for automobiles is now needed in some cases, and will soon be needed generally", but does not believe that such new type of street can ever be achieved under present or near future economic conditions, until different methods of financing have been developed.

The writer does not agree with the principle presented that right-of-way and construction costs should be considered separately in assessing benefits and damages. This principle appears in the report to be based upon the idea that, since inadequate rights of way were dedicated by the original owners of property, their successors in interest should bear the burden of rectifying this mistake. Such inadequate rights of way were dedicated because no one asked for adequate rights of way at the time of dedication, in the case of the older streets, and probably public authorities at the time had no conception of present traffic congestion, or could have asked or intelligently

requested, such right of way had they so desired.

During the years, 1927 to 1930, the Los Angeles (Calif.) Board of Planning Commissioners reviewed approximately a thousand subdivisions. Practically every subdivider was quite willing to dedicate street space of ample width and in proper location when asked to do so. To place the burden of rectifying past mistakes of previous owners upon existing owners, when such past mistakes were unconsciously made, appears to be an unfair principle. If a fair and equitable method of ascertaining benefited interests and of evaluating benefits accruing is developed, there will be no need of considering, separately, right-of-way and construction costs.

# Report of Tellers on Second Ballot for Official Nominees

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	"October 15, 1934
"To the Secretary,	
AMERICAN SOCIETY OF CIVIL ENG	INEERS:
"The Tellers appointed to canvass the	Second Ballot for Official Nominees report
as follows:	
"Total number of ballots received	1 973
"Deduct:	
Ballots not signed	rears of dues
"Total withheld from canvass	
"Ballots canvassed	1 810
"For Vice-President, Zone II:	"For Vice-President, Zone III:
D. H. Sawyer 443	Henry E. Riggs 698
Frank L. Nicholson 303	
Void	
Total	10(41
"For Director, District 3:	"For Director, District 9:
C. Arthur Poole 113	
Edward H. Sargent 58	
Void	
"For Director, District 5:	
Herman Stabler 168	"For Director, District 12:
Charles W. Kutz 64	
Edwin F. Wendt 73	5 Ross K. Tiffany 74
Blank	- m + 1
"For Director, District 7:	"For Director, District 16:
James L. Ferebee 14	
Blank 1	Thomas D Ass
Total 16	Void 3
"For Director, District 8:	Total
Charles B. Burdick 15	
Void	1

"Respectfully submitted,

"THEODORE REED KENDALL, Chairman,

"R. S. SAUNDERS, ALLEN P. RICHMOND, JR., B. S. VOORHEES, JOHN J. COPE, CHARLES CARSWELL, CHARLES C. ARMSTRONG, F. A. Rossell, "Tellers." JAMES A. DARLING,

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#### APPLICATIONS FOR ADMISSION AND FOR TRANSFER

The Constitution provides that the Board of Direction shall elect or reject all applicants for *Admission* or for *Transfer*, and, in order to determine justly the eligibility of each candidate, the Board must depend largely upon the Membership for information.

This list is issued to members in every grade for the purpose of securing all such available information, and every member is urged to scan carefully each monthly list of candidates and to furnish the Board with data in regard to any applicant which may aid in determining his eligibility. It is the *Duty* of all *Members* to the *Profession* to assist the *Board* in this manner.

It is especially urged, in communications concerning applicants, that a Definite Recommendation as to the Proper Grading in Each Case be given, inasmuch as the grading must be based upon the opinions of those who know the applicant personally as well as upon the nature and extent of his professional experience. If facts exist derogatory to the personal character or to the professional reputation of an applicant, they should be promptly communicated to the Board. Communications Relating to Applicants are considered by the Board as Strictly Confidential.

The Board of Direction will not consider the applications herein contained from residents of North America until the expiration of thirty (30) days, and from non-residents of North America until the expiration of ninety (90) days from November 15, 1934.

#### MINIMUM REQUIREMENTS FOR ADMISSION

Grade	General Requirement	Age	Length of Active Practice	Responsible charge of work
Member	Qualified to design as well as to direct important work	35 years	12 years*	5 years of im- portant work
Associate Member	Qualified to direct work	27 years	8 years*	1 year
Junior	Qualified for sub-professional work	20 years†	4 years*	The Transfer
Affiliate	Qualified by scientific acquire- ments or practical experience to co-operate with engineers	35 years	12 years*	5 years of im- portant work
Fellow	Contributor to the permanent funds of the Society	1000	4 5 4 5 4 4	O/HVStolky

<sup>\*</sup>Graduation from a school of engineering of recognized reputation is equivalent to 4 years of active practice.

<sup>†</sup>Membership ceases at age of 33 unless transferred to higher grade.

The fact that applicants give the names of certain members as references does not necessarily mean that such members endorse.

#### FOR ADMISSION

ANDERSON, LOUIS HAROLD, Palo Alto, Cal. (Age 35.) Director of Public Utili-ties and Chf. Deputy City Engr. Refers to J. F. Byxbee, E. L. Grant, C. D. Marx, D. H. Merrill, C. Moser, W. Putnam, L. B. Reynolds, E. C. Thomas, C. B. Wing.

BESSON, FRANK SCHAFFER, Jr., Cambridge, Mass. (Age 24.) Graduate student in Civ. Eng., Massachusetts Inst. of Technology. Refers to E. L. Daley, C. L. Hall, T. B. Larkin, K. R. Young.

BOYSEN, ALBERT PETER, Elmhurst, Ill. (Age 39.) With American Bridge Co., Chicago, Ill. Refers to F. W. Dencer, H. C. Hunter, F. R. Judd, B. G. Leake, H. Penn, A. F. Reichmann, C. E. Webb.

BRESLIN, THOMAS, Orchards, Johannesburg, South Africa. (Age 37.) Structural Eng. Asst., Rand Water Board. Refers to H. J. Collins, L. A. Mackenzie, W. G. Sutton. (Applies in accordance with Sec. 1, Art. I, of the By-Laws.)

BROWN, ANDREW ROY, Tuscaloosa, Ala. (Age 52.) Chf. Engr. and Gen. Supt., J. W. Gwin Co., Inc., Gen. Contrs. Refers to A. C. Everham, J. P. Ewin, G. Gilchrist, J. V. Hanna, E. E. Howard, H. P. Treadway, N. T. Veatch, Jr., E. P. Weatherly.

BURNS, CHARLES PHILLIPS, Yellow-stone Park, Wyo. (Age 33.) Project Engr., U. S. Bureau of Public Roads. Refers to H. A. Alderton, Jr., A. C. Bux, J. O. Hunt, C. E. Learned, A. C. Stiefel.

CARLSON, FRANK BOWERS, Fargo N. Dak. (Age 27.) Camp Supt., Emer-gency Conservation Works, Williston, N. Dak. Refers to C. Johnson, R. E. Ken-nedy, R. A. Pease, W. H. Robinson, W. E. Smith, L. C. Tschudy, D. L. Yarnell.

CONNELL, HARRY HUBERT, Salina, Kans. (Age 37.) Associate Engr., Wilson Engr. Co., Cons Engrs. Refers to L. E. Conrad, F. F. Frazier, C. R. Hatfield, W. Kiersted, M. C. Nichols, H. A. Stringfellow, M. A. Wilson.

de CHELMINSKI, VLADIMIR, Ocumare de la Costa, Venezuela, S. A. (Age 34.) Engr., Ministry of Public Works of Venezuela. Refers to J. J. Collins, R. E. Colvin, R. A. McMenimen, J. R. Stubbins, M. M. Upson, L. Velez.

DYER, WESLEY HALLIBURTON, Nashville, Tenn. (Age 26.) Estimator, Nashville Bridge Co. Refers to L. C. Anderson, W. A. Coolidge, A. J. Dyer, H. B. Dyer, F. J. Lewis, H. McDonald.

F. J. Leva.,

EARNEST, GEORGE BROUAS,

Heights, Ohio. (Age 32.) Instructor in

Civ. Eng., Case School of Applied Science.

Refers to G. E. Barnes, M. S. Brown, F. L.

Gorman, R. L. Harding, F. H. Neff, F. L.

Plummer, W. E. Rice.

FRANK AUGUSTUS, Ft.

FOEHRENBACH, FRANK AUGUSTUS, Ft. Totten, N. Y. (Age 29.) Asst. Engr., Works Div., Dept. of Public Welfare, Flushing, N. Y. Refers to F. A. Barnes, E. N. Burrows, C. Crandall, J. E. Perry, C. L. Walker.

GAYLORD, CHARLES NELSON, Hampton Va. (Age 26.) Instructor in Steel and Va. (Age 26.) Instructor in Steel and Concrete Design, Dept. of Bidg. Constr., Hampton Inst. Refers to H. W. Brown, L. M. Gram, L. C. Maugh, R. H. Sherlock, J. A. Van den Broek. GLENDENING, PAUL FREDERICK, Globe, Ariz. (Age 24.) Constr. Inspector, Arizona Highway Dept. Refers to E. S. Borgquist, F. C. Kelton, E. V. Miller, J. W. Powers, A. F. Rath, E. R. Stapley.

GRAVES, QUINTIN BRANSON, Knoxville, Tenn. (Age 29.) Instructor, Univ. of Ten-nessee. Refers to N. W. Dougherty, F. W. Epps, B. J. Lambert, E. L. Waterman, Epps, B. J. Lan S. M. Woodward.

GRIFFIN, GUY EBEN, Cos Cob, Conn. (Age 35.) San. Engr., Sewer Comm., Town of Greenwich. Refers to H. P. Burden, E. S. Chase, S. M. Ellsworth, G. M. Fair, A. L. Fales, C. W. Sherman, A. D. Weston.

JONAS, (Age 23.) York FREDERICK, New York C. Refers to R. E. Goodwin, F. McLoughlin.

JORDAN, THOMAS ANDREW, Chicago, Ill. (Age 53.) Chf. Designing Engr., American Bridge Co. Refers to A. A. Casani, F. W. Dencer, C. J. Kennedy, R. Khuen, Jr., H. Penn, A. F. Reichmann, C. E. Webb.

KELLOW, GAYLORD ARMAND, Cresco, Iowa. (Age 23.) Refers to J. W. Howe, R. B. Kittredge, B. J. Lambert, F. T. Mavis, C. T. Watts, C. C. Williams.

KENNEDY, RICHARD ROBERTS, San Francisco, Cal. (Age 24.) Designing Engr., Eng. Office of Clyde C. Kennedy. Refers to C. G. Hyde, E. A. Ingham, J. J. Jessup, E. M. Kelly, L. B. Reynolds.

KETCHUM, DANIEL BEADING, Ft. Peck, Mont. (Age 24.) At Ft. Peck Laboratory, under War Dept., U. S. Engr. Office, Ft. Peck Dist. Refers to J. J. Doland, M. S. Ketchum, J. I. Parcel, N. T. F. Stadtfeld, L. G. Straub L. G. Straub.

KUMPE. GEORGE, Cambridge, Mass. (Age 23.) Graduate student in Civ. Eng.. Massachusetts Inst. of Technology. Refers to P. G. Burton, R. C. Cutting, B. C. Dunn, H. R. Faison, M. C. Tyler.

KURTTILA, GEORGE HENRY, Gladstone, Mich. (Age 29.) Inspector, U. S. Engrs., Duluth, Minn. Refers to H. B. Pettit, W. C. Polkinghorne, R. C. Vogt.

LAKE, IRVING JOSEPH, Brooklyn, N. Y. (Age 38.) Refers to G. Berry, T. B. Brogan, H. P. Hammond, J. C. O'Dea, L. F. Rader, E. J. Squire, W. R. Tenney.

LARSON, EVERETT HARMON, Big Piney, Wyo. (Age 23.) Jun. Topographic Engr., U. S. Geological Survey. Refers to G. D. Clyde, H. H. Hodgeson, O. W. Israelsen, H. R. Kepner, R. B. West.

LEWIN, HAROLD ANDREW, Brooklyn, N. Y. (Age 27.) Computer, Dept. of Com-merce, U. S. Coast and Geodetic Survey. Refers to R. W. Armstrong, H. R. Bouton, H. A. Dibbell, L. H. Lockwood, D. C. Waite.

LOCRAFT, BERNARD FRANCIS, Washington, D. C. (Age 32.) With James Berrell, Washington, D. C. Refers to R. Coltman, Jr., F. F. Gillen, T. W. Marshall, M. S. Rich, A. J. Scullen, G. B. Strickler.

MeMINN, FRED FRANCIS, Cincinnati, Ohio. (Age 48.) Asst. Commr. of Bldgs., City of Cincinnati, Ohio. Refers to J. R. Biedinger, W. W. Carlton, H. H. Kranz, F. L. Raschig, J. E. Root, E. K. Ruth, C. M. Sternes, A. R. Root, E. K. Ruth, F. L. Raschig C. M. Stegner.

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MORSE, REED FRANKLIN, Manhattan, Kans. (Age 36.) Asst. Prof. of Civ. Eng., Kansas State Coll. Refers to T. B. Agg, W. V. Buck, L. E. Conrad, F. F. Frazier, A. H. Fuller, R. B. Wills, M. A. Wilson, C. F. Zeigler.

NEWMAN, ERVIN FRANCIS, Scranton, Pa. (Age 22.) Refers to W. S. Lohr, L. Perry, P. P. Rice, E. H. Rockwell, G. F. Roehrig, F. W. Slantz.

NOYES, JOHN RUTHERFORD, Las Cruces, N. Mex. (Age 32.) 1st Lieut., U. S. Army; Instructor of Engrs., New Mexico National Guard. Refers to H. J. M. Baker, F. A. Barnes, M. Elliott, W. L. Holmes, A. W. Sargent, J. G. Steese.

PALOCSAY, FRANK STEVE, Cleveland, Ohio. (Age 32.) Inspector, U. S. Engrs., Buffalo, N. Y., Dist., Refers to L. L. Davis, C. Y. Dixon, S. C. Hollister, W. E. Howland, G. P. Springer, R. B. Wiley.

PENNA, NICHOLAS, Harrison, N. Y. (Age 30.) Chf. of Party, County Engrs. of Westchester, White Plains, N. Y. Refers to E. Anderberg, J. Barnett, C. A. Garfield, A. G. Hayden, R. M. Hodges, S. Rosenberg.

POPPER, WILLIAM, Oakland, Cal. (Age 25.) Jun. Bridge Designing Engr., State of California. Refers to J. Cherno, H. G. Gerdes, J. W. Green, B. M. Shimkin, C. L. Young.

BHINE, JACK BERTRAND, Houston, Tex. (Age 24.) State Inspector on construction, Texas Highway Dept., Div. 12. Refers to E. C. H. Bantel, P. M. Ferguson, S. P. Finch, J. A. Focht.

ROBINSON, BENJAMIN PERRY, New York City. (Age 20.) Refers to A. Haring, C. T. Schwarze.

SEERY, JAMES DANIEL, Fruitland, N. Mex. (Age 25.) Surveyor, Dept. of Indian Affairs, 5th Irrigation Dist. Refers to J. H. Dorroh, H. C. Neuffer, R. H. A. Rupkey, F. W. Slattery, A. N. Thompson. SMITH, BURTON LYNCH, Santa Fe, N. Mex. (Age 27.) Project Engr., U. S. Indian Service. Refers to P. S. Fox, J. C. Harvey, B. Johnson, G. D. Macy, W. E. Stroky

SMITH, NEAL DEFFEBACH, Banning, Cal. (Age 32.) Asst. to Constr. Engr., Metropolitan Water Dist. of Southern California. Refers to G. E. Baker, J. B. Bond, W. L. Chadwick, R. B. Diemer, B. A. Eddy, J. Stearns, W. E. Whittier.

van LOBEN SELS, MAURITS JUST, Vorden Cal. (Age 24.) Refers to N. W. Magner, E. S. Randolph.

WALTON, JEAN RICHMOND, Shiprock, N. Mex. (Age 28.) Surveyor, U. S. Indian Irrigation Service, 5th Irrigation Dist. Refers to J. H. Dorroh, H. C. Neuffer, F. W. Slattery.

WHITNEY, WILLIAM RESTON, St. Albans, N. Y. (Age 41.) Res. Engr.-Inspector, Public Works Administration, New York City. Refers to L. Costello, D. B. Fegles, S. T. Goldsmith, W. D. Kramer, J. S. Macdonald, H. S. R. McCurdy.

WINFREY, ROBLEY, Ames, Iowa. (Age 35.) Bulletin Editor and Research Engr., Eng. Experiment Station, Iowa State Coll. Refers to R. W. Crum, A. H. Fuller, H. J. Gilkey, A. Marston, M. B. Morris.

WINICK, CHARLES BORIS, Brooklyn, N. Y. (Age 37.) Res. Engr.-Inspector, P. W. A., New York City. Refers to C. L. Crandall, M. E. Gilmore, C. S. Gleim, G. L. Lucas, A. I. Raisman, G. S. Reeves, C. E. Sudler, B. Wilson.

WOFFENDEN, JOHN BERNARD, Portland, Ore. (Age 46.) Senior Draftsman, U. S. Engrs. Refers to L. Brown, W. N. Carey, H. C. Corns, G. M. Garen, S. C. Godfrey, K. V. Jones, H. A. Rands, F. C. Schubert, F. C. Williams, J. Wright.

WORTH, HENRY NORMAN, Colombo, Ceylon. (Age 49.) Chf. San. Engr., Dept. of Medical and Sanitary Services, Ceylon. Refers to G. M. Fair, H. F. Ferguson. (Applies in accordance with Sec. 1, Art. I, of the By-Laws.)

WYATT, WENDELL CHAMBERS, Pittsburg, Kans. (Age 25.) Asst. Engr., Water Conservation, State of Kansas. Refers to E. Boyce, G. W. Bradshaw, J. O. Jones, W. C. McNown, F. A. Russell, J. W. Stewart.

KUKTASEVI VIVATANA, LUANG, Bangkok, Slam. (Age 28.) Asst. Engr. and Constr. Engr., Dept. of Royal State Rys. of Slam. Refers to T. M. Bhiromya, J. Husband. (Applies in accordance with Sec. 1, Art. I, of the By-Laws.)

ZOKOVETZ, NIHKOLAS GEORGIEVICH, Leningrad, U. S. S. R. (Age 34.) Supt. of Constr. on metallurgical works, Industrial Construction Trust (Company). Refers to F. M. Dawson, A. L. Gram, H. F. Janda, F. E. Turneaure, L. F. Van Hagan.

#### FOR TRANSFER

#### FROM THE GRADE OF ASSOCIATE MEMBER

AMES, GEORGE MARSHALL, Assoc. M., Grand Rapids, Mich. (Elected June 7, 1899.) (Age 76.) Vice-Pres. Owen-Ames-Kimball Co., Gen. Bldg. Contrs. Refers to L. E. Ayres, M. E. Cooley, G. H. Fenkell, L. W. Goddard, R. H. Merrill, H. E. Riggs, J. R. Rumsey, C. S. Sheldon.

BORNEFELD, CHARLES FOWLER, Assoc. M., Baltimore, Md. (Elected Junior May 31, 1910; Assoc. M., Jan. 15, 1917.) (Age 47.) Chf. Project Engr., Maryland State C. W. A. Organization and F. D. R. A. in Maryland. Refers to F. H. Dryden, S. L. Fuller, E. P. Hamilton, E. H. Harder, W. Mueser, S. L. Thomsen, G. W. C. Whiting.

CHIPMAN, PAUL, Assoc. M., Highland Park, Mich. (Elected Oct. 2, 1907.) (Age 61.) Office Engr., Pere Marquette Ry. Refers to F. H. Alfred, M. S. Ketchum, W. Michel, H. E. Riggs, A. N. Talbot.

GRANGER, ARMOUR TOWNSEND, Assoc. M., New York City. (Elected July 6, 1925.) (Age 36.) Chf. Draftsman, Ash-Howard-Needles & Tammen, Cons. Engrs. Refers to E. C. H. Bantel, S. P. Finch, E. E. Howard, E. R. Needles, H. C. Tammen, T. U. Taylor, G. G. Wickline.

HARTZOG, JUSTIN RICHARDSON, Assoc. M., Cambridge, Mass. (Elected July 14 1930.) (Age 42.) Associate of John Nolen, City Planner, Cambridge, Mass. Refers to R. C. Allen, R. V. Black, J. L. Crane. Jr., F. E. Everett, F. H. Fay, H. M. Lewis, R. H. Randall.

HEYMAN, WILLIAM, Assoc. M., New York City. (Elected Junior June 30, 1911; Assoc. M. March 4, 1913.) (Age 49.) Pres. and Works Mgr., Heyman & Goodman Co. Refers to C. Goodman, J. P. Hogan, A. I. Raisman, R. Ridgway, J. F. Sanborn, D. C. Serber, L. White.

KEREKES, FRANK, Assoc. M., Ames, Iowa. (Elected Junior June 6, 1921; Assoc. M. March 16, 1925.) (Age 38.) Prof. of Structural Eng., Iowa State Coll. Refers to T. R. Agg, L. E. Conrad, J. K. Finch, P. A. Franklin, A. H. Fuller, F. O. X. McLoughlin, A. Marston, A. F. Reichmann, D. B. Steinman, C. C. Williams,

LEVIN, LOUIS FBANK, Assoc. M., Sault Ste. Marle, Mich. (Elected March 11, 1929.) (Age 43.) County Engr.-Mgr., Chippewa County, Mich. Refers to J. H. Bateman, C. M. Cade, G. C. Dillman, I. De-Young, C. A. Melick, L. J. Rothgery, L. C. Smith.

Gainesville Fla. (Elected Jan. 26 1931.) (Age 38.) Associate Prof. of Civ. Eng., Univ. of Florida. Refers to G. E. Barnes, C. B. Breed, C. C. Brown, F. M. Dawson, W. W. Fineren, H. D. Mendenhall, H. J. Morrison, P. L. Reed. O'REILLY, ANTHONY RAUEN, ASSOC. M. Reading, Pa. (Elected Junior Dec. 6, 1920; Assoc. M. Nov. 14, 1927.) (Age 37.) Chf. Engr., Bureau of Water. Refers to G. S. Beal, R. C. Dennett, I. M. Glace, H. E. Moses, A. L. Reeder, W. L. Stevenson, G. F. Wieghardt.

PATTERSON, DONALD, Assoc. M., Uniontown, Pa. (Elected Junior May 28, 1923; Assoc. M. Oct. 14, 1929.) (Age 36.) Dist. Bridge Engr., Pennsylvania Dept. of Highways. Refers to S. Eckels, T. C. Frame, S. W. Jackson, D. Kippel, R. B. Kittredge, F. M. Masters, R. Modjeski, L. L. Shirey, G. B. Woodruff, S. M. Woodward.

POLLOCK, JAMES RANDALL, Assoc. M., Flint, Mich. (Elected May 8, 1922.) (Age 41.) Director of Public Works and Utilities. Refers to W. Bintz, S. A. Greeley, W. C. Hoad, E. D. Rich, H. E. Riggs, E. C. Shoecraft, J. S. Worley.

#### FROM THE GRADE OF JUNIOR

BRIELMAIEB, ALPHONSE ANTHONY, Jun., Galena, Ill. (Elected July 16, 1928.) (Age 29.) With U. S. Forest Service on Soil Brosion Prevention. Refers to J. Boldt, H. Cross, J. C. Esch, W. C. Huntington, E. G. Kauffmann, A. R. Lord, F. E. Richart.

Yorktown Heights, N. Y. (Elected Nov. 14, 1927.) (Age 32.) Res. Engr. with James C. Harding, Cons. Engr., Mt. Kisco, N. Y. Refers to G. E. Barnes, W. Garett, J. C. Harding, E. G. Manahan, L. G. Rice.

FUNK, LOUIS, Jun., New York City. (Ellected Nov. 23, 1931.) (Age 31.) Asst. Engr. (C. W. A.), Park Dept., New York City. Refers to W. F. Barck, E. J. Carrillo, P. D. G. Hamilton, L. Hussey, G. W. Knight, B. Wuth.

New York City. (Elected Oct. 1, 1928.) (Age 28.) Project Engr. with Alexander Potter, Cons. Engr. Refers to T. R. Camp, S. G. Hess, J. L. Lenox, A. Potter, R. G. Tyler.

KOENIG, EDWARD FRANCIS, Jun., Los Angeles, Cal. (Elected April 23, 1928.) (Age 32.) Jun. Civ. Engr., City of Los Angeles. Refers to F. Bates, R. M. Fox, F. M. Hines, L. C. Mayer, C. J. Shults, E. Van Goens.

LOUCHHEIM, WILLIAM SANDEL, Jun., Philadelphia, Pa. (Elected June 7, 1926.) (Age 29.) Vice-Pres., Keystone State Corporation. Refers to G. H. Biles, P. G. Brown, R. Farnham, H. S. Hipwell, W. I. Lex, C. E. Myers, L. F. Parlette, P. M.

Sam, W. R. Scanlin, R. C. Scott, J. S. Shute, C. H. Stevens, S. M. Swaab, T. P. Watson,

Watson.

McLEAN, WALTER REGINALD, Jun., San
Leandro, Cal. (Elected July 14, 1930.)
(Age 31.) Asst. Engr., East Bay Municipal
Utility Dist., Oakland, Cal. Refers to J.
D. DeCosta, A. D. Edmonston, C. E. Grunsky, Jr., F. W. Hanna, R. C. Kennedy,
J. S. Longwell, E. L. Macdonald.

MURPHY, LAWRENCE PATRICK, Jun., Peoria, Ill. (Elected May 25, 1931.) (Age 32.) Asst. Civ. Engr., U. S. Engr. Office. Refers to C. R. Andrew, E. H. Beechley, D. H. Connolly, J. J. Doland, W. C. Huntington, W. H. Rayner, J. W. Woermann.

RAWHOUSER, CLARENCE, Jun., Denver, Colo. (Elected Nov. 10, 1930.) (Age 32.) Asst. Engr., U. S. Bureau of Reciamation. Refers to R. A. Anderegg, J. A. Beemer, J. J. Hammond, H. B. Luther, A. Ruettegers, J. L. Savage, B. W. Steele, R. D. Welsh, W. S. Winn.

Wess, v. S. Will. S. Scheffelder, Scheffelder, Vash. (Elected Oct. 14, 1929.) (Age 32.) Structural Draftsman, Isaacson Iron Works. Refers to G. E. Hawthorn, R. P. Hutchinson, J. W. Miller, C. C. More, R. G. Tyler.

WINTER, CARROLL CORNELIUS, Jun., San Francisco, Cal. (Elected Oct. 14, 1929.) (Age 29.) Associate Bridge Constr. Engr., Bridge Dept., State of California. Refers to C. E. Andrew, H. J. Brunnier, J. W. Gross, C. R. Harding, I. O. Jahlstrom, F. W. Panhorst, H. M. Smitten, G. D. Whittle.

FATT, Name 3. Chapters (Except) 100 2 Port And First Pres Marchest L. F. H. Alling M. Skelener S. H. Alling M. Skelener

The Board of Direction will consider the applications in this list not less than thirty days after the date of issue.